Logistic regression, the binomial construction, and a hierarchical regression model

Roger Levy 9.19: Computational Psycholinguistics 30 October 2023

Probing binomial ordering preferences

• In each pair, which phrase sounds more natural?

| hit and | run | run | and | hit |
|--------------|------------|------------|-----|----------|
| gold and | silver | silver | and | gold |
| deer and | trees | trees | and | deer |
| drink and | food | food | and | drink |
| bacteria and | candy | candy | and | bacteria |
| radio and | television | television | and | radio |
| shares and | stocks | stocks | and | shares |
| chanting and | enchanting | enchanting | and | chanting |
| quails and | felines | felines | and | quails |

Ordering preferences in binomials

 Every occurring binomial is result of a speaker's choice about binomial ordering

| (US Google Books ngram counts, 1960–2012; ~340B words) | Count | Count(Rev) |
|---|---------|------------|
| salt and pepper | 568,951 | 32,082 |
| cat and mouse | 26,774 | 367 |
| skirts and sweaters | 1,763 | 1,707 |
| bishops and seamstresses | <40 | <40 |
| few and unfavorable | <40 | <40 |
| principal and interest | 120,034 | 50,032 |

- What is the representation of these ordering preferences?
- Are these preferences also *productive*?

An *n*-grams dataset from millions of books



(image credit Top of the List)

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RESEARCH ARTICLE

Quantitative Analysis of Culture Using Millions of Digitized Books

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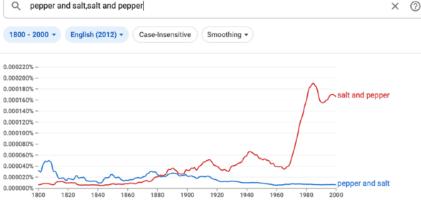
We constructed a corpus of digitized texts containing about 4% of all books ever printed. Analysis of this corgune snakles us to investigate cultural in transk quantitatives. We survey the vesa therain of "culturantics," focusing on linguistic and cultural phenomena that were reflected in the English language between 1800 and 2000. We show how this approach can provide insights about fields as diverse as lexicography, the evolution of grammar, collective memory, the adoption of technology, the pursuit of name, eemosriph, and historical epidemiology. Culturantics extends the boundaries of rigorous quantitative inquiry to a wide array of new plenomenas aparning the social sciences and the humanities.

of 1208 books. The corpus contain 386.434.758 words from 1861: thus, the frequency is 5.5 × 10-5. The use of "slavery" peaked during the Civil War (early 1860s) and then again during the civil rights movement (1955-1968) (Fig. 1B) In contrast, we compare the frequency of "the Great War" to the frequencies of "World War I" and "World War II". References to "the Great War" peak between 1915 and 1941. But although its frequency drops thereafter, interest in the underlying events had not disappeared; instead, they are referred to as "World War I" (Fig. 1C). These examples highlight two central factors that contribute to culturomic trends. Cultural change guides the concepts we discuss (such as "slavery"). Linguistic change, which, of course, has cultural

roots, affects the words we use for those concepts ("the Great War" versus "World War I"). In this

paper, we examine both linguistic changes, such

as changes in the lexicon and grammar, and cul-



(Michel et al., 2011; the Google Books project)

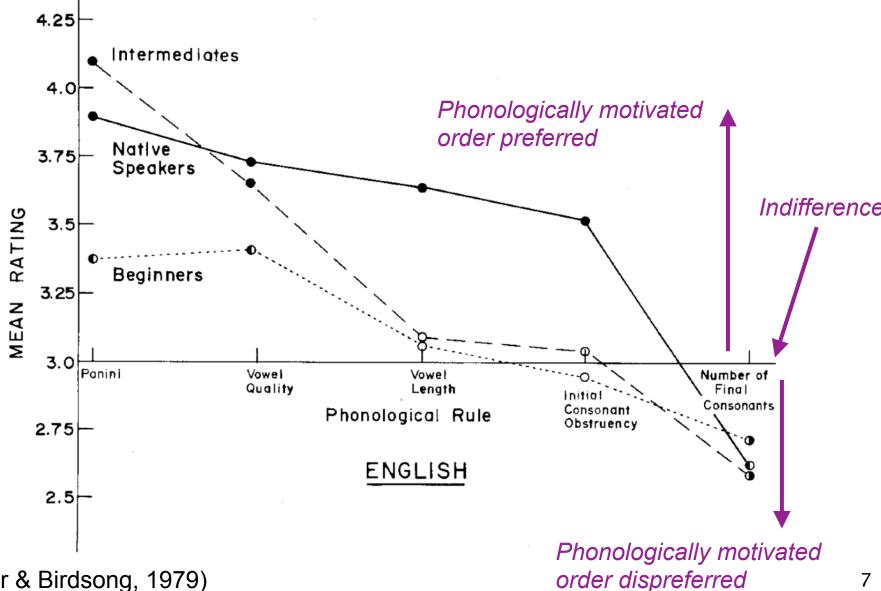
Testing some more intuitions



Testing some more intuitions

| fim | - | fum | fum | - | fim |
|----------|-----|----------|----------|-----|----------|
| begroast | and | begroat | begroat | and | begroast |
| spladilk | or | dilk | dilk | or | spladilk |
| waf | - | paf | paf | - | waf |
| frinning | and | freening | freening | and | grinning |

Ordering preferences for nonce words



(Pinker & Birdsong, 1979)

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Previous work: novel binomials

- Pinker & Birdsong (1979) used nonce-word binomials to test phonological constraints in offline judgments:
 - Length (boof and kaboof; *dadabig and dabig)
 - Vowel Quality: high<low (gligy and glagy; *roppo and reppo)</p>
 - Vowel Length: long<short (smats and smates)</p>
 - Initial Consonant: sonorant<obstruent (haipo and daipo)
 - × # Final Consonants (skalk and skall; *flar and flard)
- McDonald, Bock, and Kelly (1993) tested (mostly) novel binomials in offline judgments and production:
 - ✓ Animacy
 - Length in production
 - Length in offline judgments

Ordering preferences: productive knowledge

What constraints predict relative preference for *X* and *Y* versus *Y* and *X* has been extensively investigated (Malkiel 1959, Bolinger 1962, Cooper & Ross 1975, Gustafsson 1976, Fenk-Oczlon 1989, Benor & Levy 2006)

- Iconic/scalar sequencing
 - what comes first happens first
 - open and read (a book); hit and run (auto); *hit and run (baseball)

Attested but violates constraint

- Perceptual Markedness
 - animate, concrete, positive, ... < inanimate, abstract, negative, ...
 - deer and trees; honest and stupid; *flora and fauna
- Power
 - More culturally prioritized or "powerful" word comes first
 - clergymen and parishioners; food and drinks;
 *clerks and postmasters
 The condiment rule (Cooper & Ross 1975)

Ordering preferences: productive knowledge

- Formal Markedness
 - Words with more general or broader meaning distributions come first
 - sewing and quilting; changing and improving;*roses and flowers
- No final stress
 - The final syllable of Y in X and Y must not be stressed
 - abused and neglected; skirts and sweaters;
 *manufacture and install
- Frequency
 - The more frequent word comes first
 - bride and groom; smile and wink; *psychiatrists and patients
- Length ("Panini's Law")
 - The shorter word comes first (we count in syllables)
 - ask and answer; tense and irritable; *family and friends

Formalizing ordering preferences

- Varieties of *probabilistic grammar* for forms *F* and meanings *M*:
 - Grammars over forms: P(F) (word strings, syntax trees, ...)
 - Grammar over possible forms given a meaning to be expressed: $P(F \mid M)$
 - Interpretive grammars of possible meanings given a form: $P(M \mid F)$

$$P("X \text{ and } Y" | \{X, Y\})$$

e.g., $P("pepper and salt" | {salt, pepper})$

A dataset of binomial expressions

Binomials are all over in naturalistic use \rightarrow easy to sample:

| ask | and | answer | right | and | good |
|----------------------|-----|----------------|---------------|-----|----------------|
| knew | and | admired | sit-ups | and | push-ups |
| medicines | and | yeast | fits | and | starts |
| surprised | and | dubious | anxiously | and | eagerly |
| rank | and | file | congressional | and | presidential |
| thick | and | brown | toe | and | fronts |
| understand | and | share | startling | and | skillful |
| consider | and | rate | carefully | and | prudently |
| commoners | and | kings | WordPerfect | and | Lotus |
| always | and | everywhere | milk | and | honey |
| stained | and | waxed | improperly | and | unfairly |
| officially | and | publicly | business | and | government |
| tear | and | inflame | playbacks | and | study |
| Ву | and | large | cold | and | wet |
| linguistic | and | paralinguistic | softly | and | triumphantly |
| further | and | unnecessarily | register | and | vote |
| pie | and | bar | proposed | and | accepted |
| anger | and | anxiety | geographical | and | socio-economic |
| follow | and | understand | welcomed | and | approved |
| crime | and | sports | dwindling | and | diminishing |
| poetry | and | non-poetry | tough | and | dirty |
| immediately | and | directly | eighth | and | ninth |
| (Benor & Levy, 2006) | | | : | | |

Probabilistic models of binomial ordering preferences

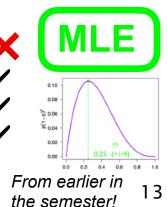
• One-constraint model, e.g.,

 $P([\text{SHORT}] \text{ and } [\text{LONG}]|\{[\text{short}], [\text{long}]\}) = p$

- In our dataset, 65% preference when conjuncts differ in number of syllables
 - We set the relative-frequency estimate of *p* to 0.65
 - Remember: this is the *maximum likelihood estimate!*

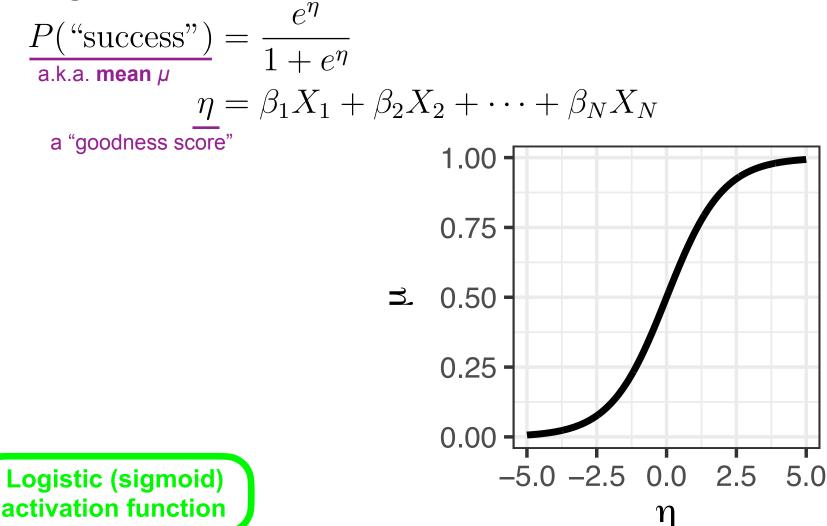
abused and neglected ✓ bold and entertaining ✓ coughed and chattered ✓ medicines and yeast

people and soils surprised and dubious sought and received sharp and rapid



Multiple, cross-cutting constraints

 When we have more constraints, we use *logistic regression*

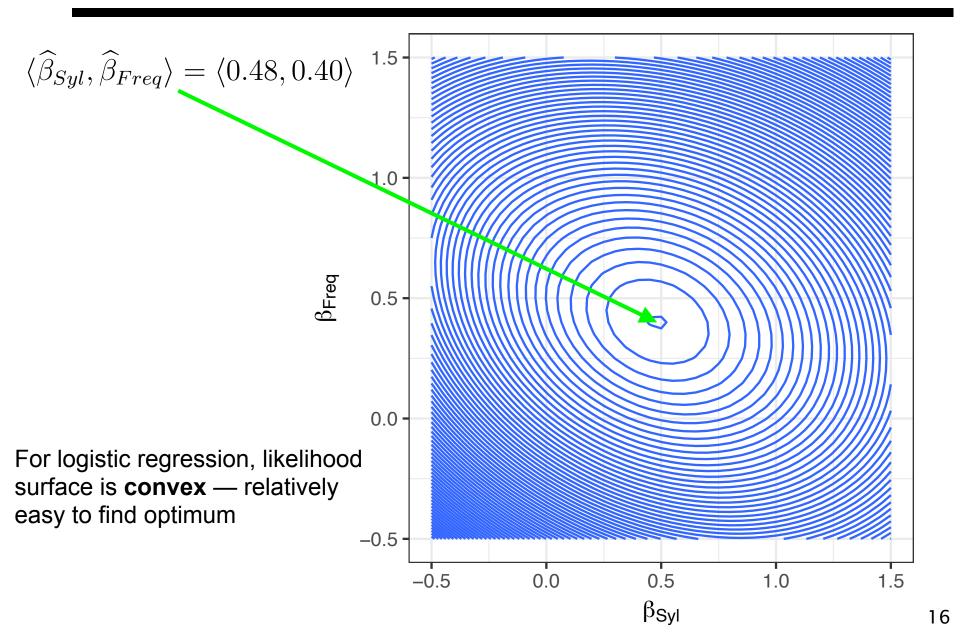


Fitting logistic regression via MLE

- With multiple model parameters, we get a likelihood surface on which we want to find the maximum
- 2-constraint example: word length and word frequency

Short<Long? Freq<Infreq?</pre> new and modern 1 correct and acute n/a down and out n/a Х cruel and unusual Х ~ Х anger and spite Х crochet and knit Х $\eta = \beta_{\mathsf{Syl}} X_{Syl} + \beta_{\mathsf{Frea}} X_{Frea}$ $P(\mathsf{A and } \mathsf{B}|\{A,B\}) = \frac{e^{\eta}}{1+e^{\eta}}$

Maximum of the likelihood surface



Model predictions from fitted parameters

Logistic Regression Model Structure

$$\eta = \beta_{Syl} X_{Syl} + \beta_{Freq} X_{Freq}$$

$$P(A \text{ and } B|\{A, B\}) = \frac{e^{\eta}}{1 + e^{\eta}}$$
a.k.a. mean μ

Fitted model parameters

$$\langle \hat{\beta}_{Syl}, \hat{\beta}_{Freq} \rangle = \langle 0.48, 0.40 \rangle$$

Model predictions

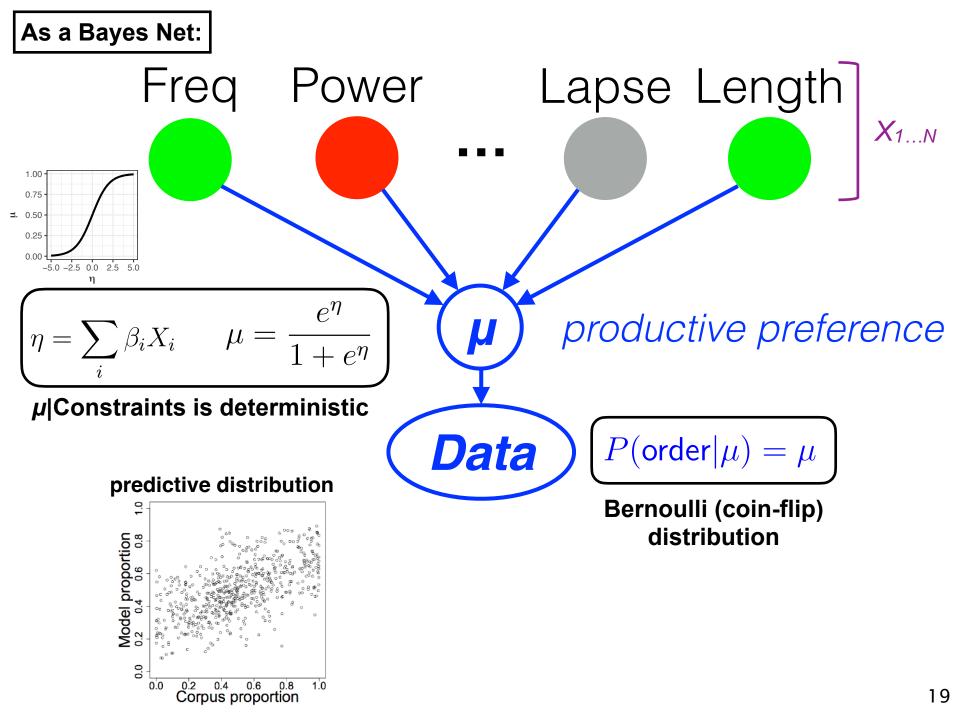
| | | | Short<long< b=""></long<> | Freq <infreq?< th=""></infreq?<> |
|---------|-----|---------|---|----------------------------------|
| new | and | modern | | ✓ |
| correct | and | acute | n/a | ✓ |
| down | and | out | n/a | × |
| cruel | and | unusual | Image: A set of the set of the | × |
| anger | and | spite | X | ✓ |
| crochet | and | knit | × | × |

Multiple, cross-cutting constraints

| Constraint | Example | Strength | |
|--|-----------------------|----------|-----|
| Iconic/scalar sequencing | open and read | 20 | |
| Perceptual markedness | deer and trees | 1.7 | |
| Formal markedness | change and improve | 1.4 | ∫ R |
| Power | food and drink | 1 | (P) |
| Avoid final stress | confuse and disorient | 0.5 | |
| Short <long< td=""><td>cruel and unusual</td><td>0.4</td><td></td></long<> | cruel and unusual | 0.4 | |
| Frequent <infrequent< td=""><td>neatly and sweetly</td><td>0.3</td><td></td></infrequent<> | neatly and sweetly | 0.3 | |

(from Morgan & Levy, 2016)

 $\{X_i\}$



Another source of knowledge

seamstæsses potatoissops OR bishpotatoes seamsteatses ?

corpus prob | {meat, potatoes}≈0.95

corpus prob | {meat, potatoes}≈0.05

You may prefer this because you're biased toward:

- culturally more powerful/central before less powerful/central
- short before long
- frequent before infrequent
- minimizing # consecutive unstressed syllables

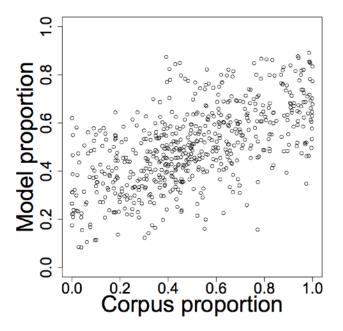
Productive knowledge

OR, you may prefer it before you've heard it far more often!

Direct experience

Productive knowledge and direct experience

• Our logistic regression model isn't perfectly predictive



- Part of this is that it fails to capture idiosyncrasy from direct experience
- A rational learner should...
 - ...apply productive knowledge in novel expressions
 - ...rely more on direct experience when it's plentiful

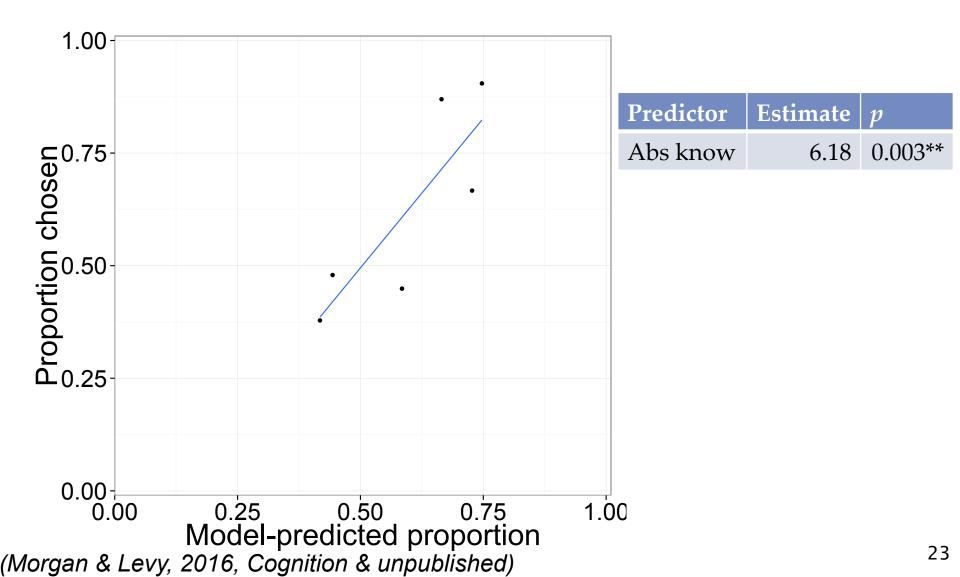
Binary forced-choice experiment

"Which sounds better?"

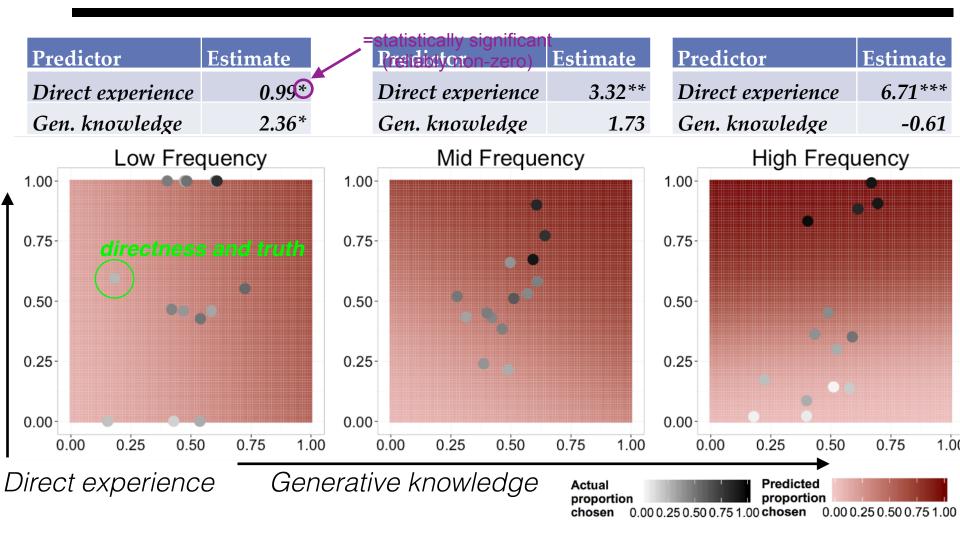
There were many **bishops and seamstresses** in the small town where I grew up.

There were many seamstresses and bishops in the small town where I grew up.

Results: novel binomials



Results: attested binomials



(Morgan & Levy, 2016, Cognition & unpublished)

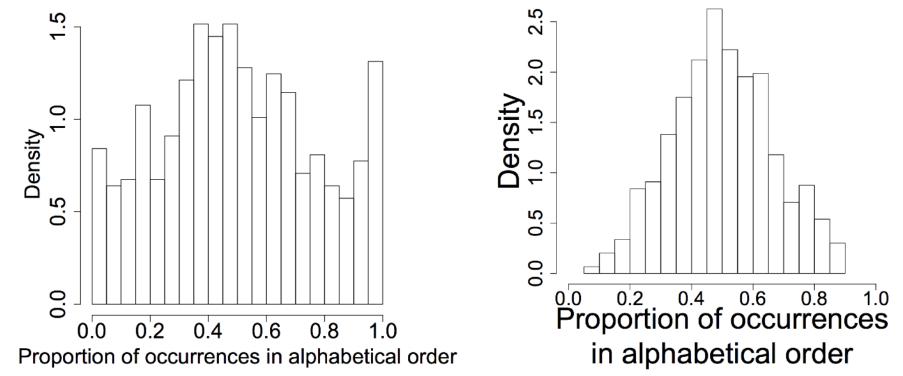
The idiosyncratic and the general

- We've seen evidence that binomial-specific ordering preferences have cognitive reality for speakers
- How dramatically do these preferences depart from the overall generative knowledge?
- How can we model both the generative knowledge and the idiosyncratic preferences simultaneously?

Distribution of ordering preference

Reality

Histogram of binomial types



Ordering preferences depart dramatically from generative knowledge!

(Morgan & Levy, 2015)

Our model

Modeling idiosyncrasy

• Here was logistic regression:

$$P(\text{``success''}) = \frac{e^{\eta}}{1 + e^{\eta}}$$
$$\eta = \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_N X_N$$

• We revise it to include a *beta-binomial* component

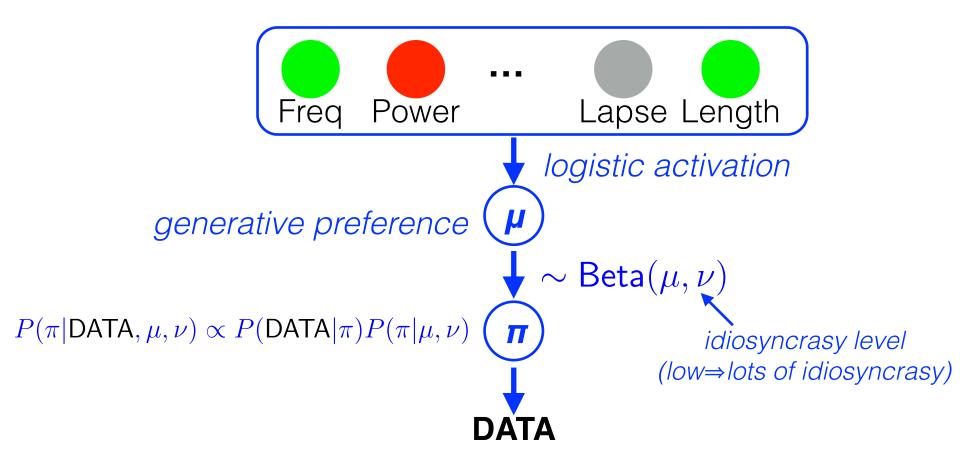
$$P(\text{"success"}) = p$$
$$p \sim \text{Beta}\left(\frac{e^{\eta}}{1+e^{\eta}},\nu\right)$$
$$\eta = \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_N X_N$$

Frequency-sensitivity of binomial idiosyncrasy

Overall unordered frequency $\nu = exp(\alpha + \beta \cdot \log(M_n))$

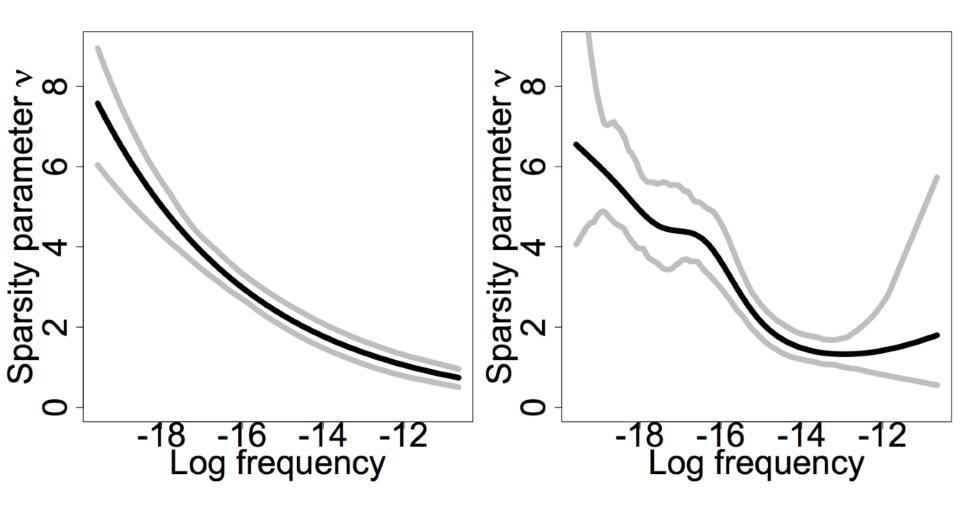
(Morgan & Levy, 2015)

Our complete model



(Morgan & Levy, 2015)

Results: frequency sensitivity of v

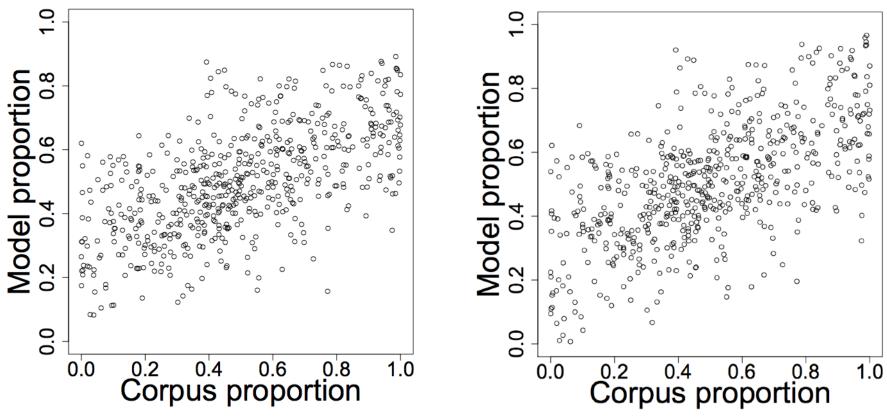


We call this *frequency-sensitive regularization* of binomial ordering preference (Morgan & Levy, 2015)

Results: "best-guess" of preferences



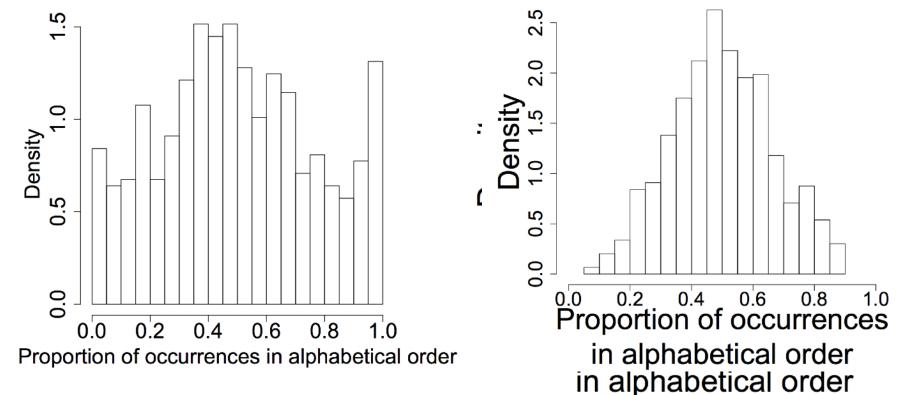
Our NEW model



Results: distribution of binomial prefs.

Reality

Histogram of binomial types



Our NEW model

(Morgan & Levy, 2015)

Summary for today

- In language we must often model multiple, overlapping, defeasible constraints that drive preferences
 - One example: linear ordering preferences
 - e.g., linear ordering preferences in the **binomial construction**
- We can do this with logistic regression
- Viewed as a Bayes Net, logistic regression imposes a parametric form on P(outcome|X_{1...m})
- Logistic regression is extendable with a hierarchical component to handle item-specific idiosyncrasies
 - One version of this: **beta-binomial regression**

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