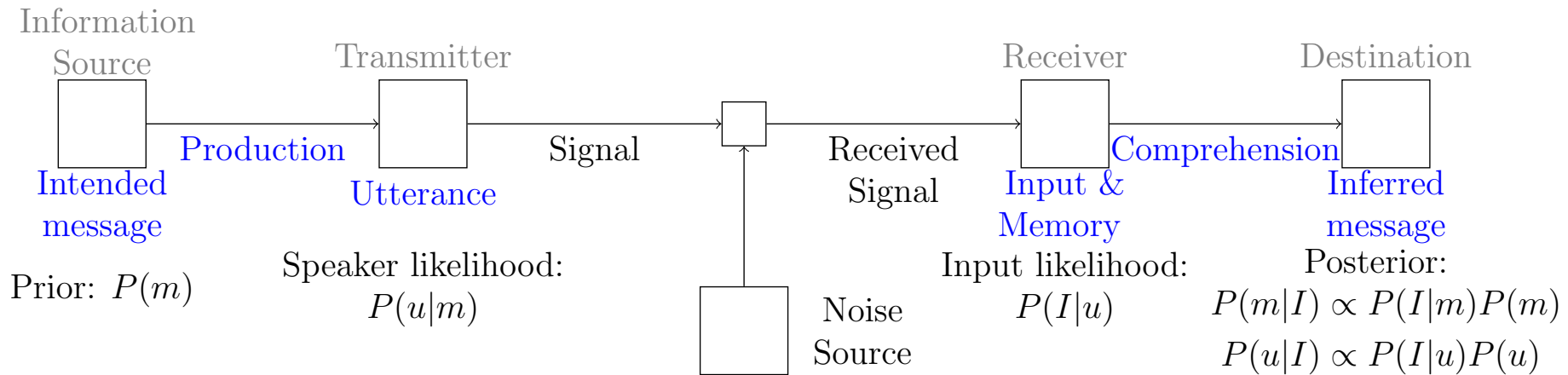


Noisy-channel sentence comprehension theory



Roger Levy

9.19: Computational Psycholinguistics

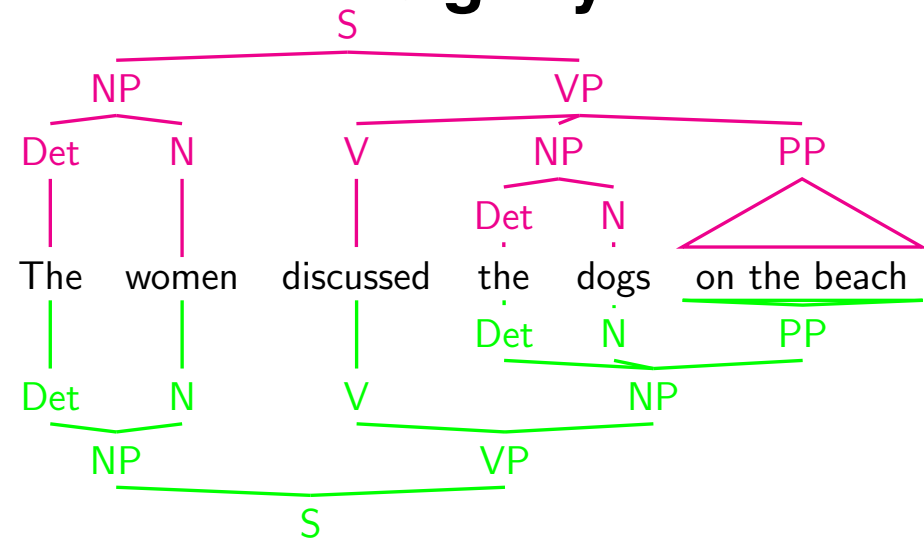
13 November 2023

Today's agenda

- Review principles of rational analysis and its application to theory of language comprehension
- Examine a phenomenon challenging for surprisal theory
- Propose a noisy-channel processing theory, using information theory and probabilistic grammars
- Develop a hypothesis within the theory for the challenging phenomenon
- Empirically test a key prediction of the theory

Challenges for efficient linguistic communication

Ambiguity



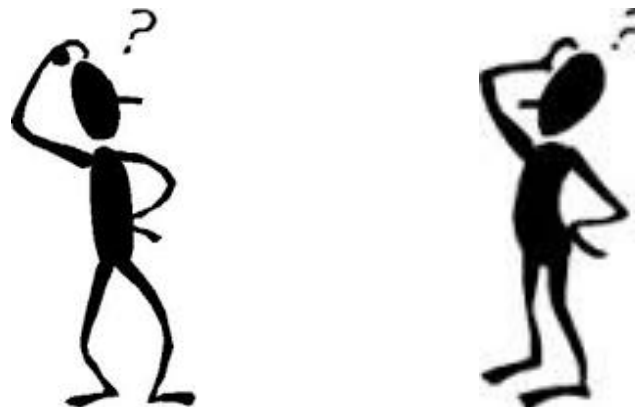
Environmental noise



Memory Limitations



Incomplete knowledge of one's interlocutors



Rational analysis

(Anderson, 1990, 1991)

Rational analysis

- Background assumption: cognitive agent is optimized via evolution and learning to solve everyday tasks effectively

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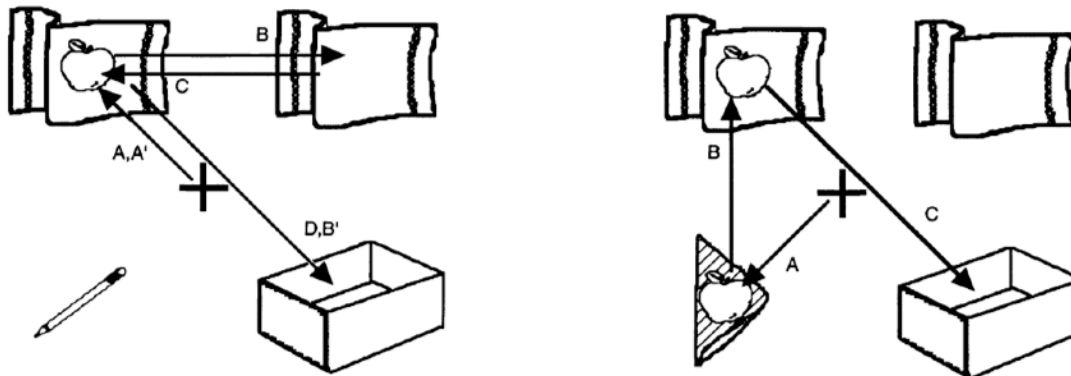
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 4. Derive predicted optimal behavior given 1—3
 5. Compare predictions with empirical data
 6. If necessary, iterate 1—5

Efficient comprehension as rational, goal-driven

- Online sentence comprehension is hard
- But lots of information sources can be usefully brought to bear to help with the task
- Therefore, it would be *rational* for people to use *all information sources available*, whenever possible
- This is what *incrementality* is
- We have lots of evidence that people do this often
- How do we reconcile these information sources?



“Put the apple on the towel in the box.” (Tanenhaus et al., 1995, Science)

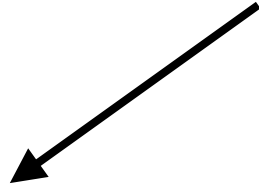
Comprehenders as reverse engineers

Discourse goals [eat tastier food]

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Planned
communicative
acts



[ask dinner partner
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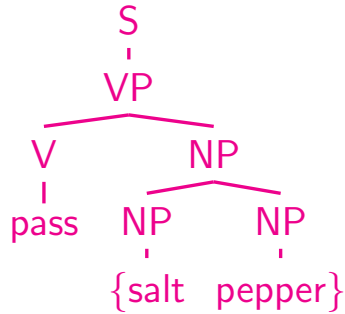
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Lexicalization
& constituency



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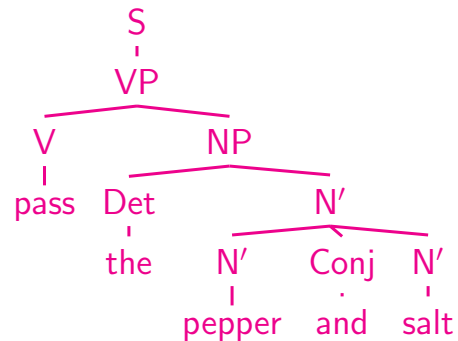
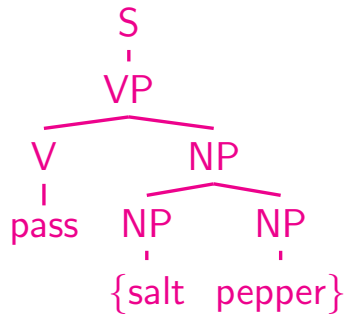
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Lexicalization
& constituency

Linearization
decisions



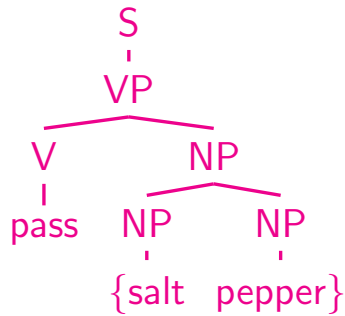
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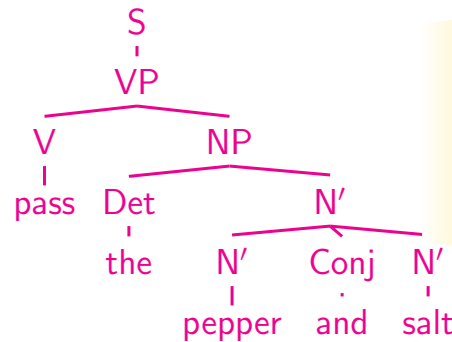
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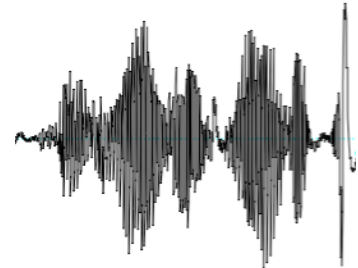
Lexicalization & constituency



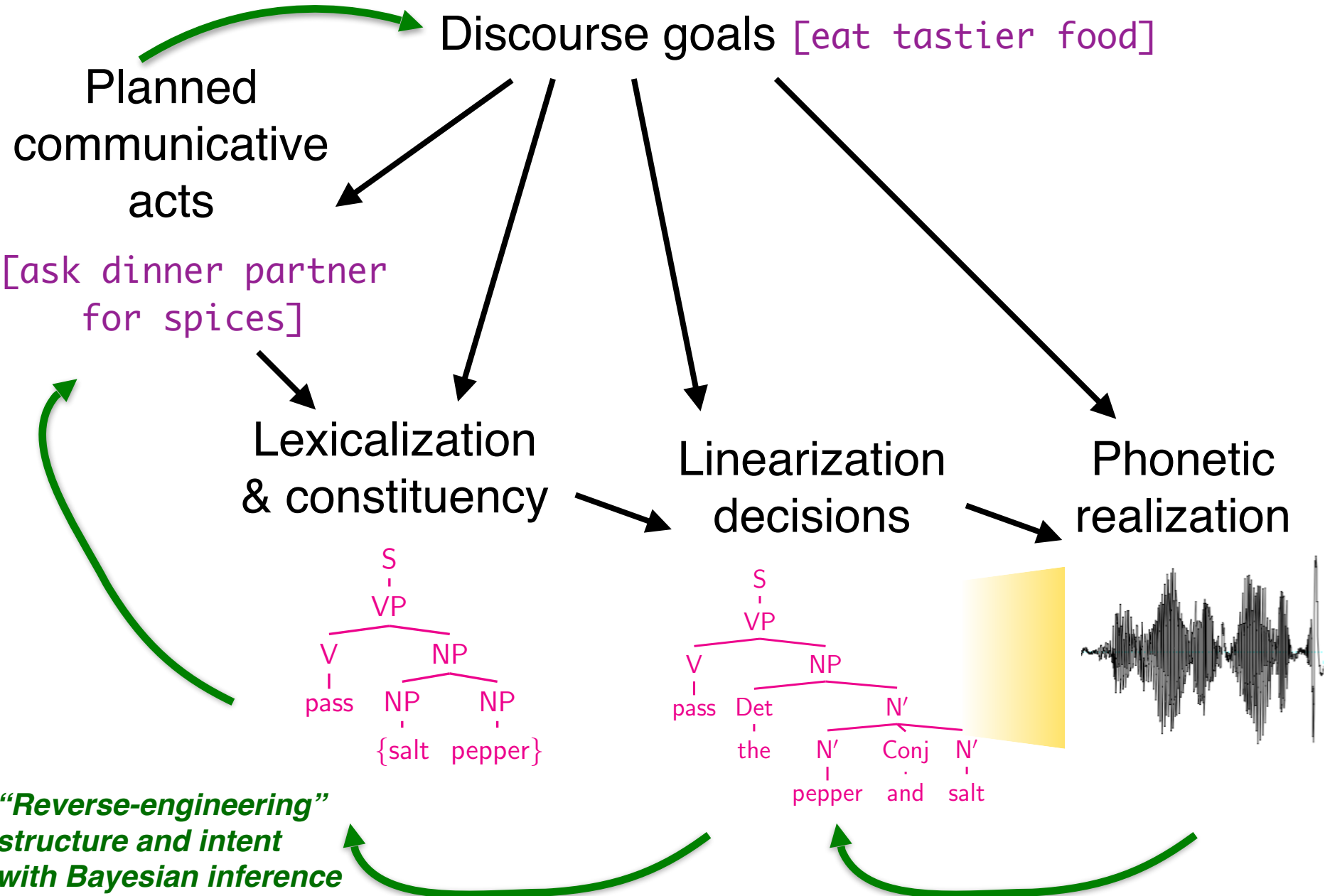
Linearization decisions



Phonetic realization



Comprehenders as reverse engineers



Surprisal summary: psycholinguistic evidence

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Problems addressed by a theory consisting of:

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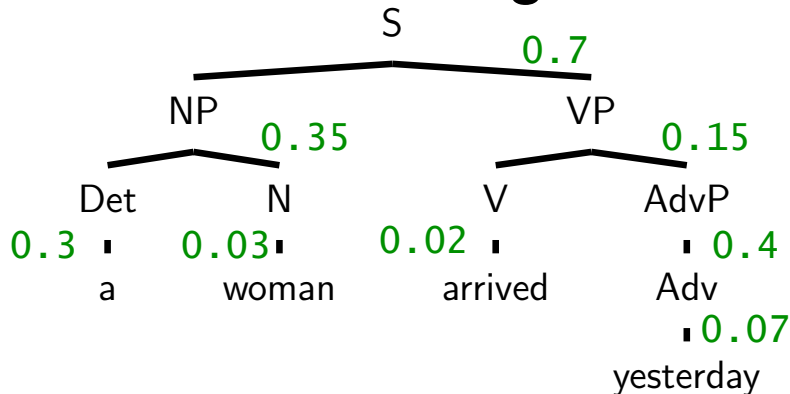
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$$P(T) = 0.7 * 0.35 * 0.15 * 0.3 * 0.03 * 0.02 * 0.4 * 0.07$$
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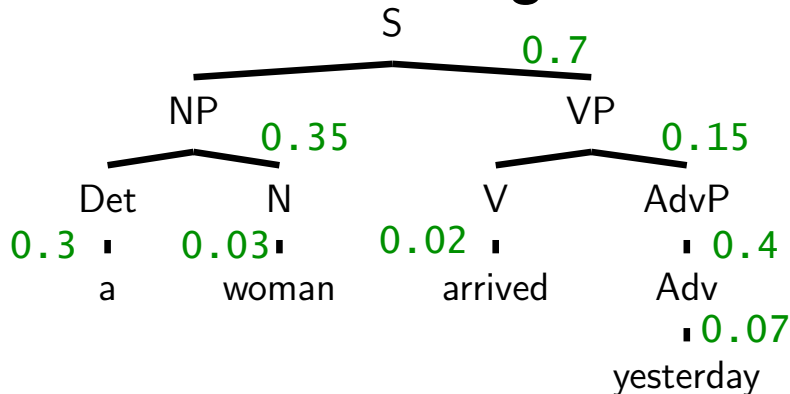
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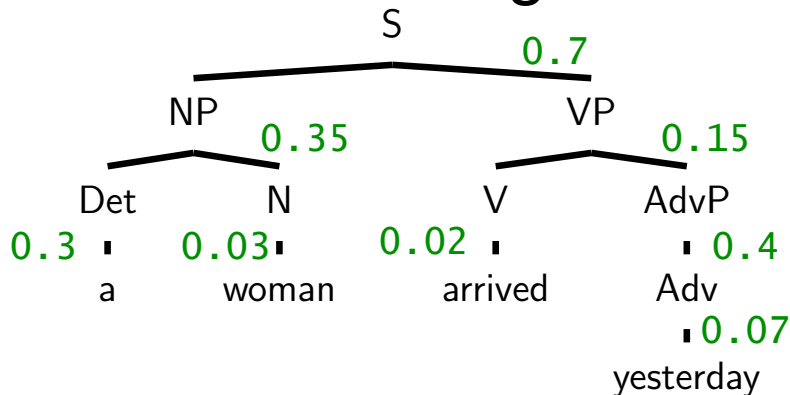
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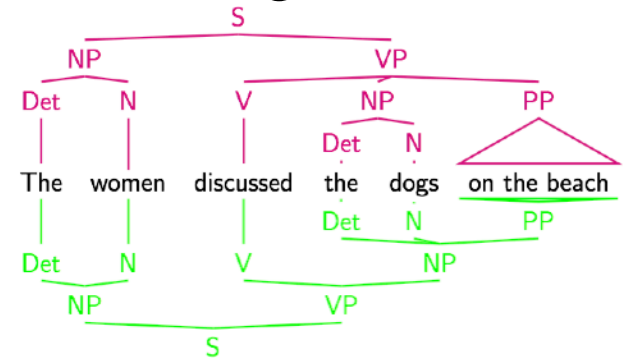


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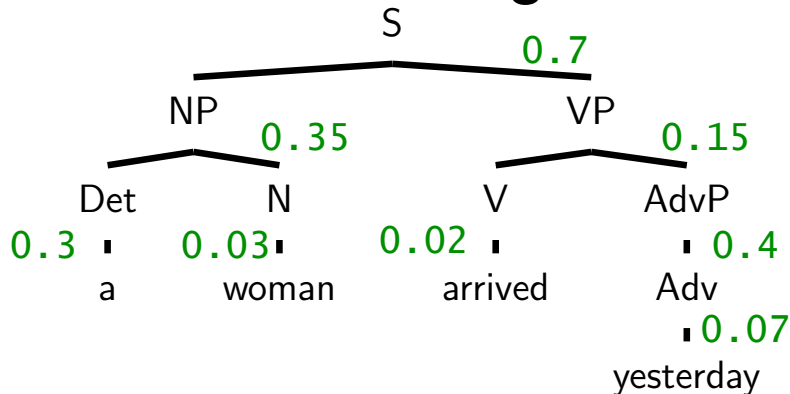
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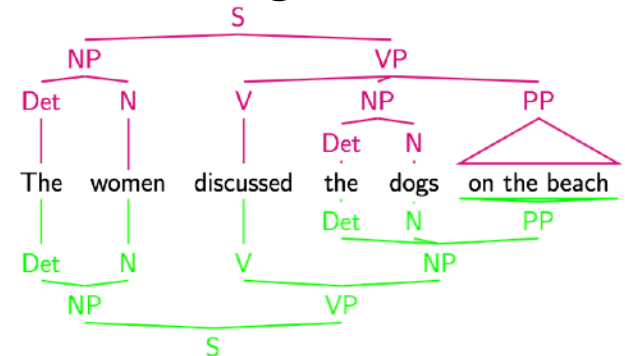


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- Garden-pathing

When the dog scratched the vet **removed** the muzzle.

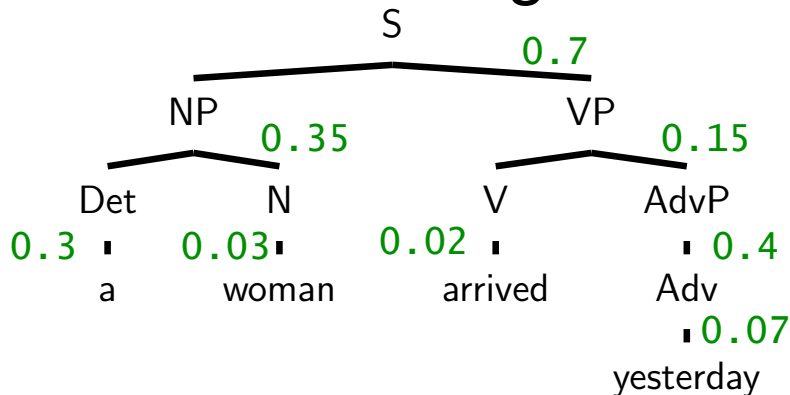
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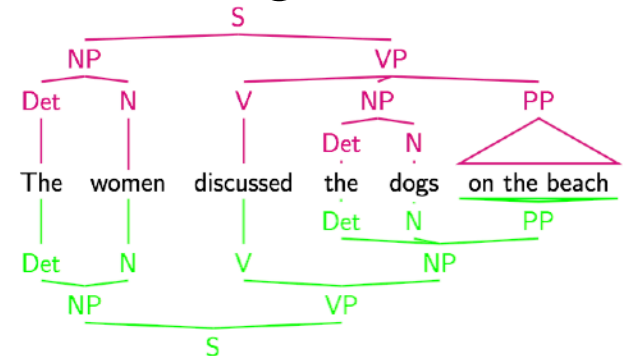
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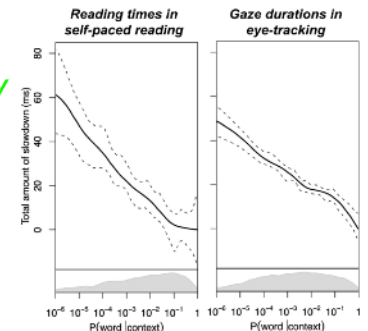


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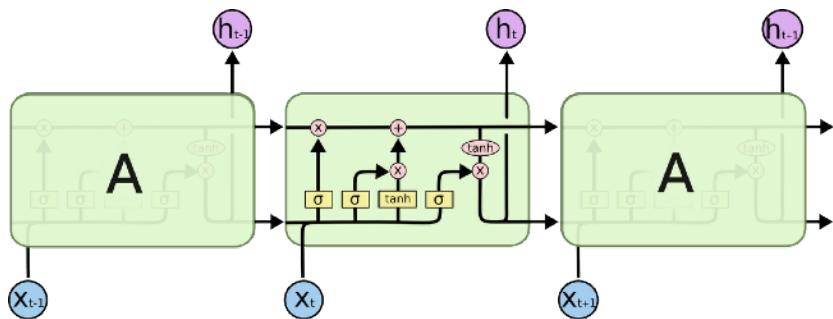
When the dog scratched the vet removed the muzzle.

- Prediction & reading times

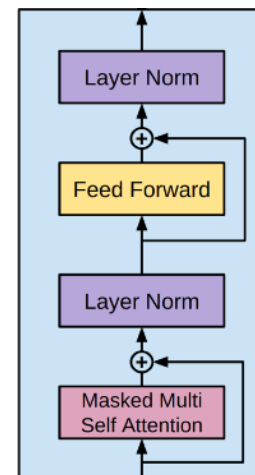
my brother came inside to... play
the children went outside to...



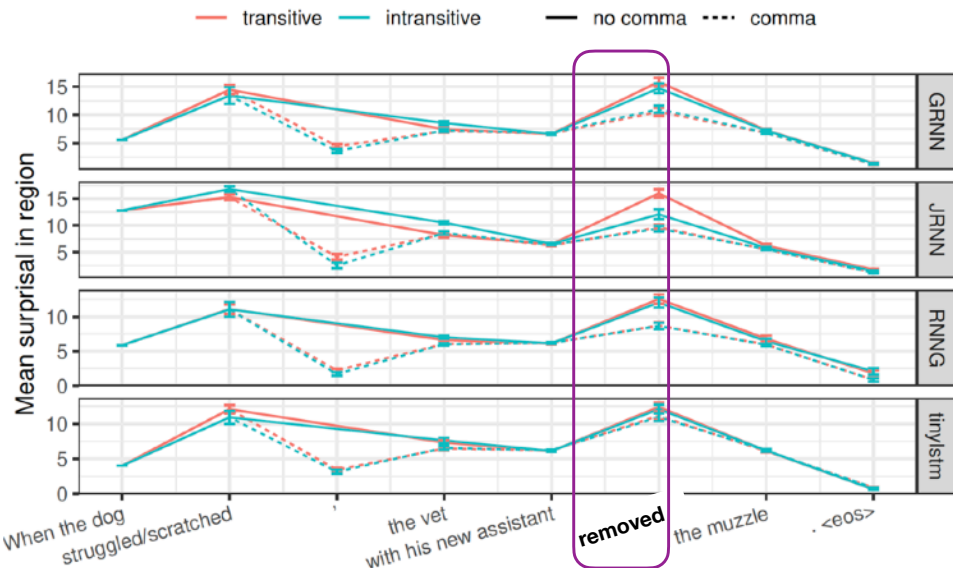
Syntax-like surprisal from deep-learning models



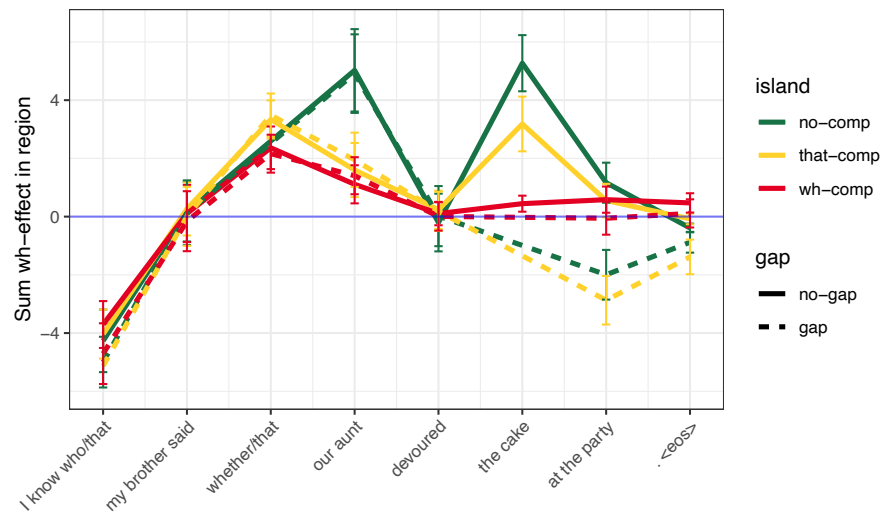
(Elman, 1990; Hochreiter & Schmidhuber, 1997)



(Vaswani et al., 2017; Radford et al., 2018, 2019)



(Futrell et al. 2019, NAACL)



(Wilcox et al., 2018, BlackBox NLP)

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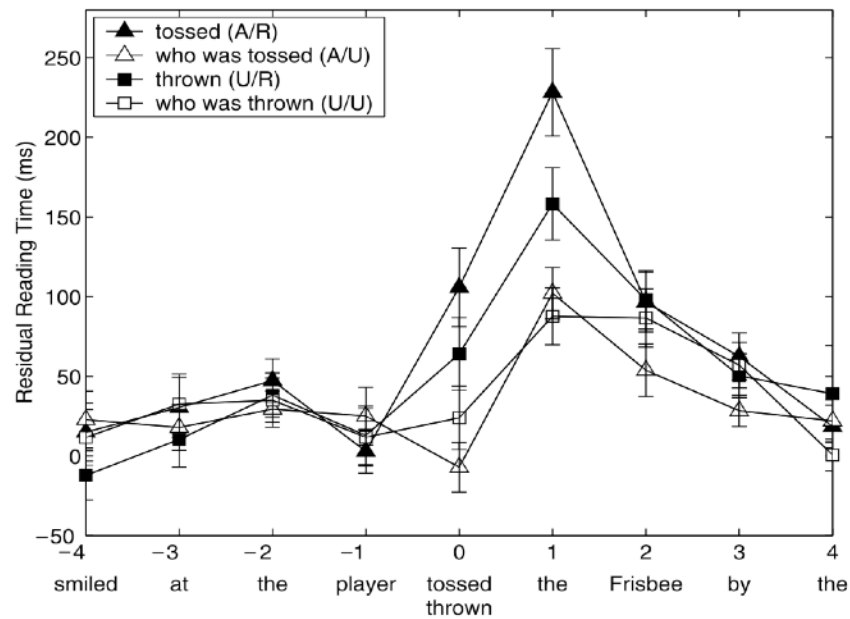
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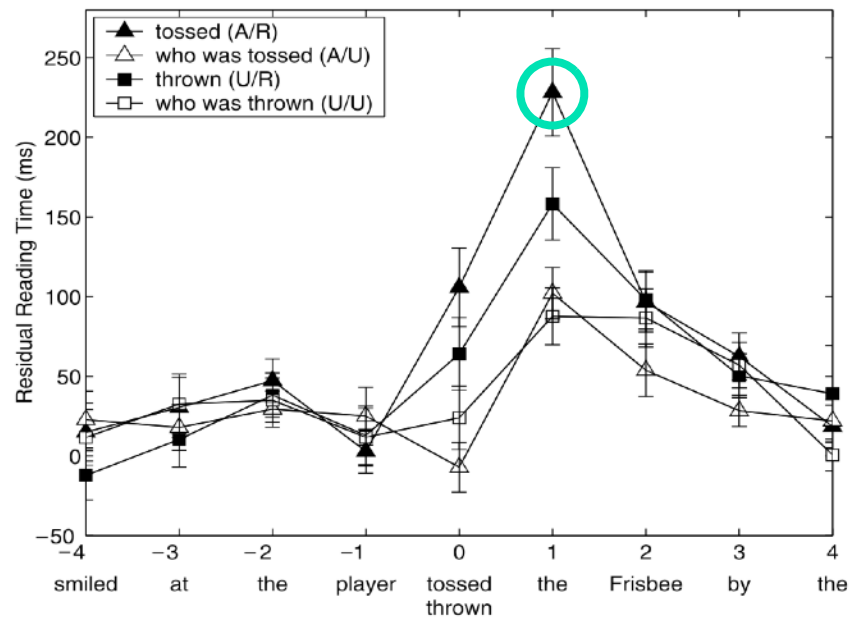
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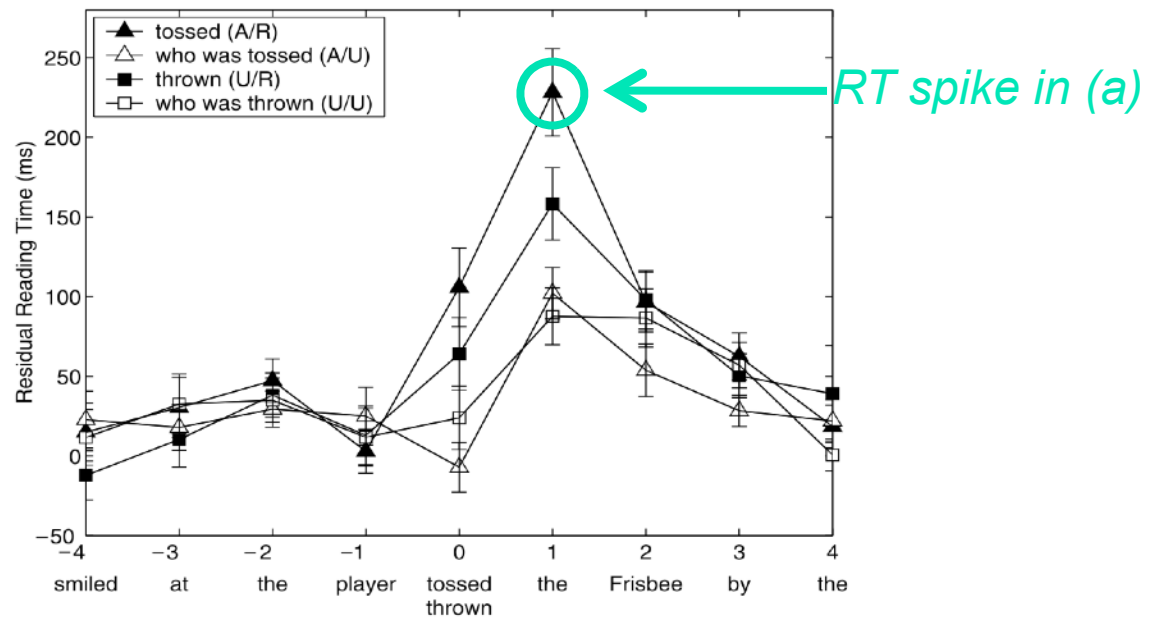
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 - *The woman brought the sandwich...tripped*

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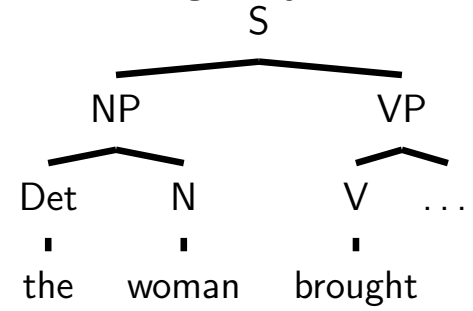
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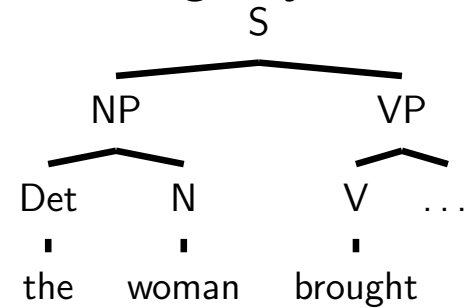


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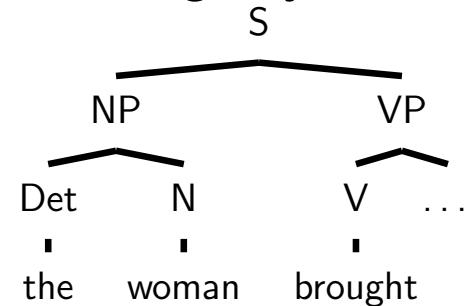
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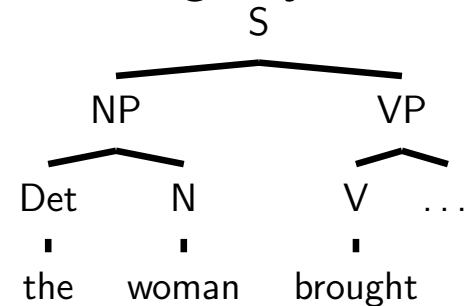
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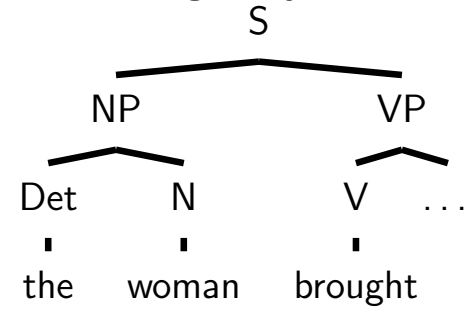
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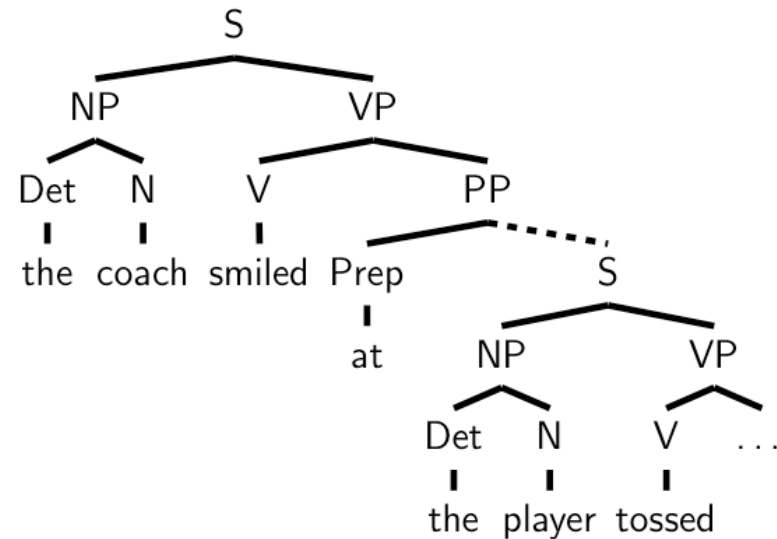
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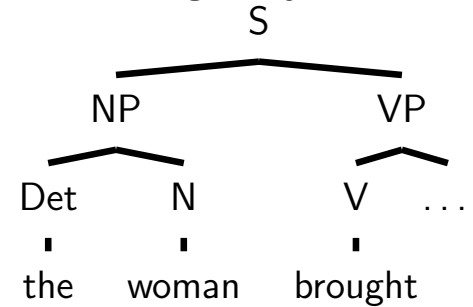


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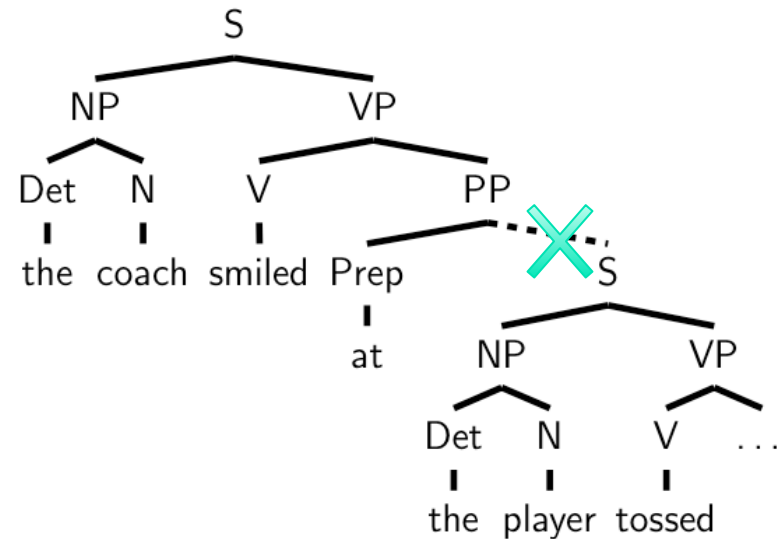
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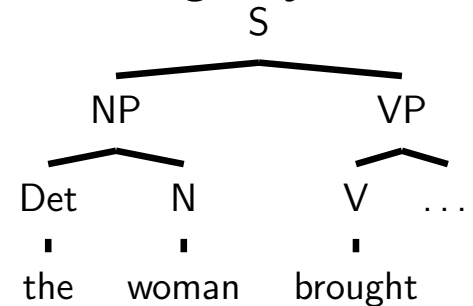


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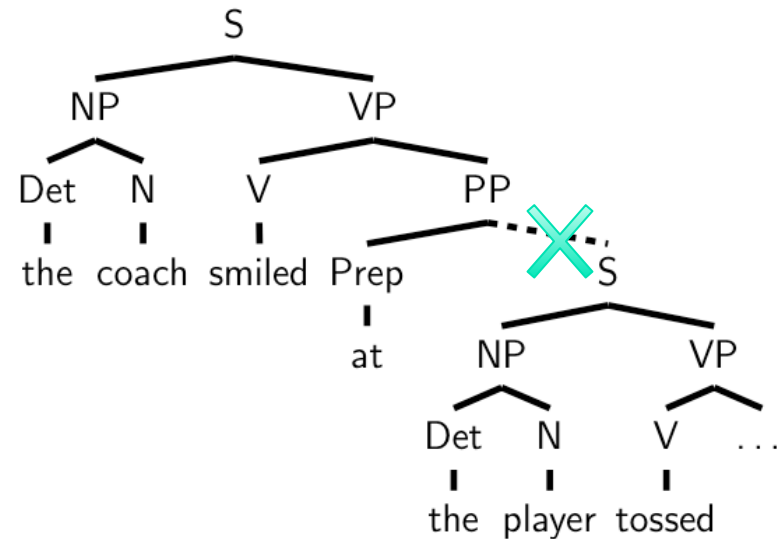
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- A challenge for rational models: **failure to condition on relevant context**

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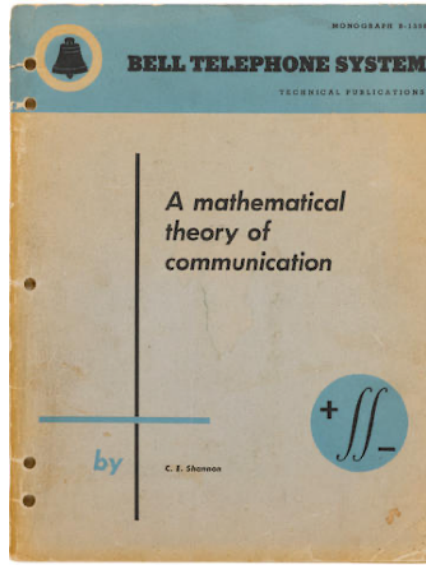
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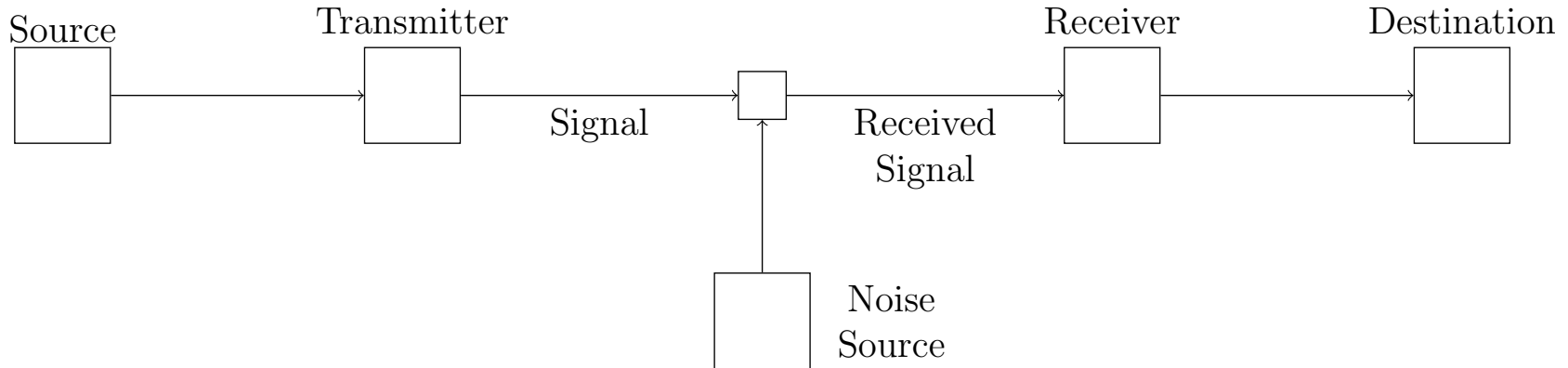
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- Leads to two questions:
 1. What might a model of sentence comprehension under uncertain input look like?
 2. What interesting consequences might such a model have?

Noisy-channel theory of language processing

(Shannon, 1948)

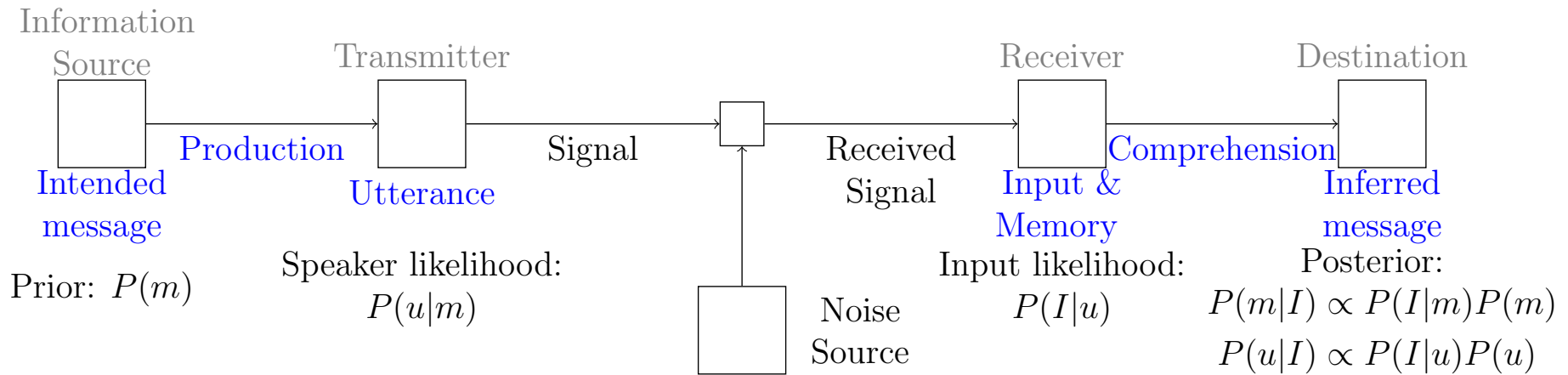
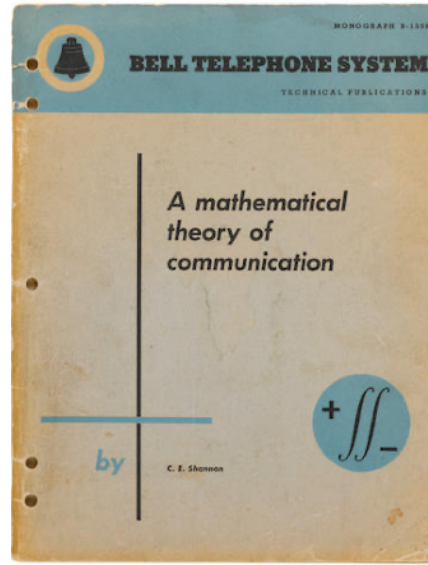


Information



Noisy-channel theory of language processing

(Shannon, 1948)



(Levy, 2008; Gibson et al., 2013)

Noisy-channel sentence processing

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- If we don't observe a sentence but only a noisy input I :

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- If we know true sentence \mathbf{w}^* but not input I :

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Noisy-channel sentence processing

- Standard probabilistic sentence processing:

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*comprehender's
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$$= P_C(\mathbf{w}) \int_I \frac{P_C(I|\mathbf{w})P_T(I|\mathbf{w}^*)}{P_C(I)} dI$$

$$\propto Q(\mathbf{w}, \mathbf{w}^*) \quad \text{Levy (2008, EMNLP)}$$

Representing noisy input

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- How can we represent the type of noisy input generated by a word sequence?

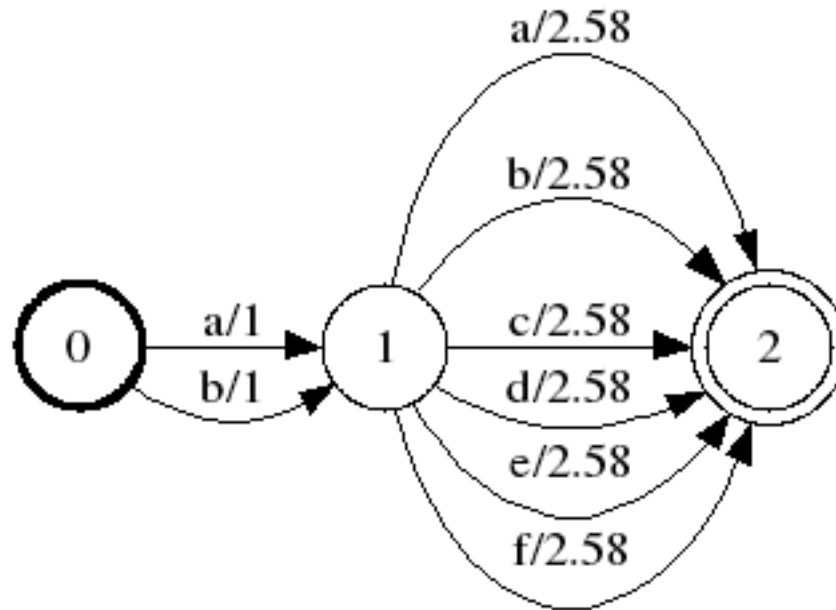
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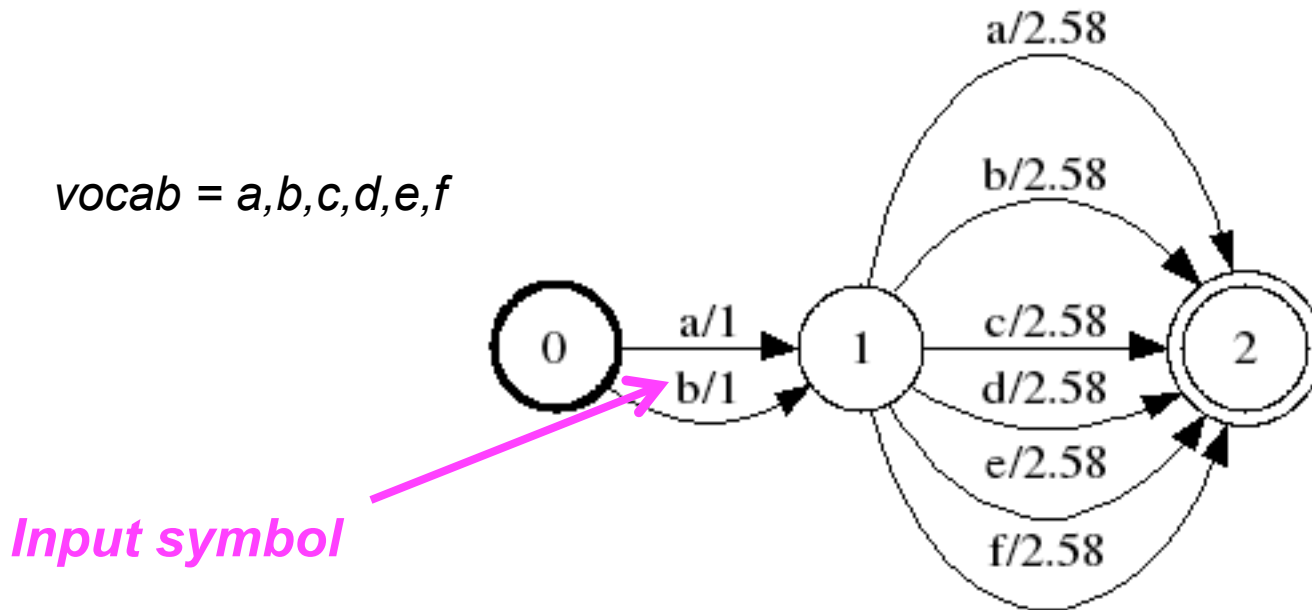
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vocab = a,b,c,d,e,f



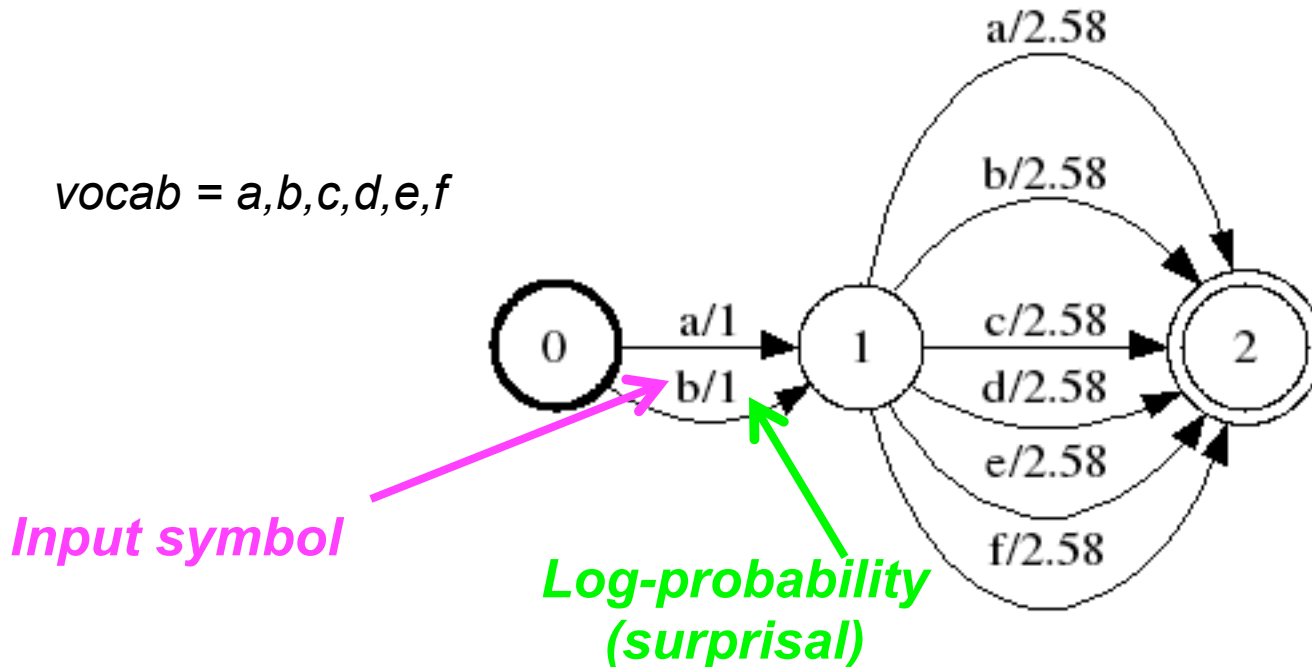
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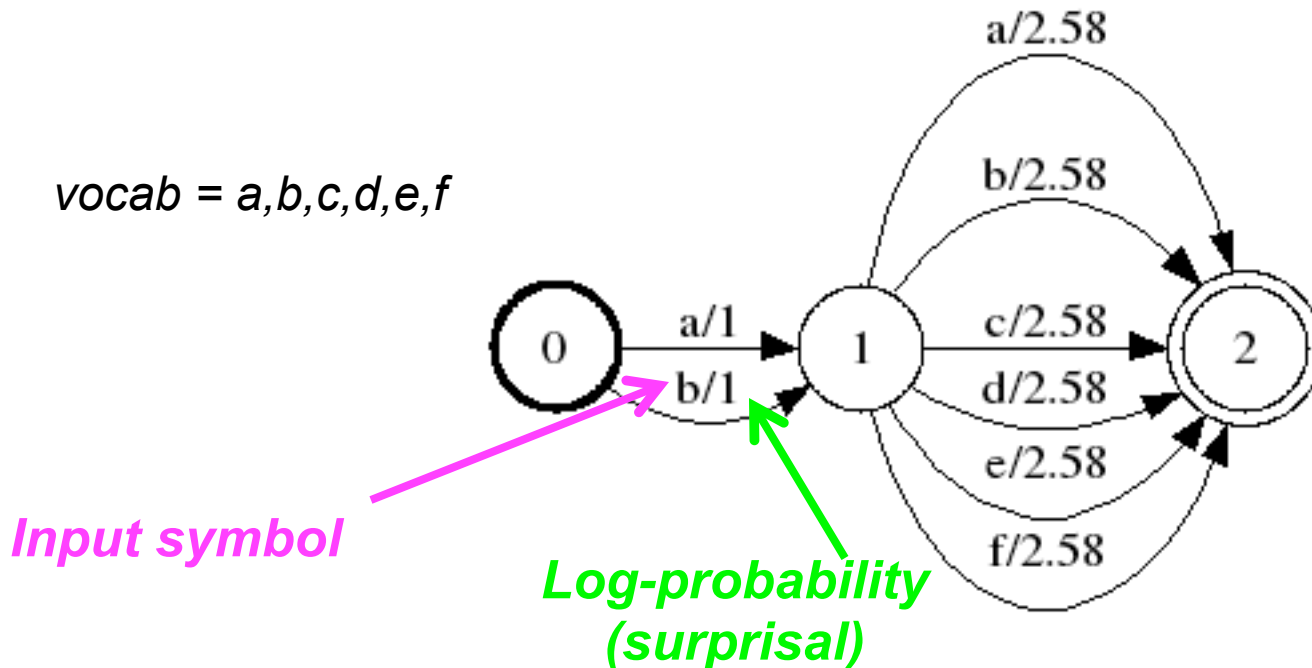
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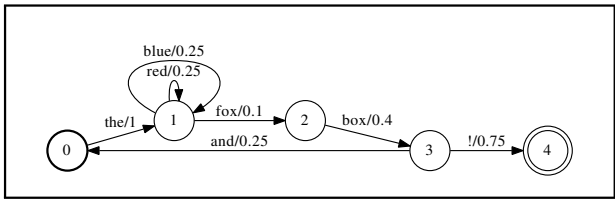
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- “Word 1 is a or b, and I have no info about Word 2”

Weighted finite-state automata



A WEIGHTED FINITE-STATE AUTOMATON (WFSA) consists of a tuple (Q, V, S, R) such that:

- ▶ Q is a finite set of STATES $q_0 q_1 \dots q_N$, with q_0 the designated START STATE;
- ▶ Σ is a finite set of terminal symbols;
- ▶ $F \subseteq Q$ is the set of FINAL STATES;
- ▶ Δ is a finite set of TRANSITIONS each of the form $q \xrightarrow{i} q'$, meaning that “if you are in state q and see symbol i you can consume it and move to state q' ”;
- ▶ λ is a function mapping transitions to real numbers (weights);
- ▶ ρ is a function mapping final states to real numbers (weights).

Weighted finite-state automata (2)

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 - ▶ ρ is a function mapping final states to real numbers (weights).
- ▶ $w_{1\dots N} \in \Sigma^N$ is ACCEPTED or RECOGNIZED by an automaton iff there is a PATH of transitions $\xrightarrow{1\dots N}$ to a final state $q^* \in F$ such that

$$q_0 \xrightarrow[1]{w_1} \xrightarrow[2]{w_2} \dots \xrightarrow[N-1]{w_{N-1}} \xrightarrow[N]{w_N} q^*$$

- ▶ The WEIGHT of such a path $\xrightarrow{1\dots N}$ is the product of the weights of each of the transitions, together with the weight of the final state:

$$P(q_0 \xrightarrow[1]{w_1} \xrightarrow[2]{w_2} \dots \xrightarrow[N-1]{w_{N-1}} \xrightarrow[N]{w_N} q^*) = \rho(q^*) \prod_{i=1}^N \lambda(\xrightarrow{i}) \quad (1)$$

Probabilistic Linguistic Knowledge

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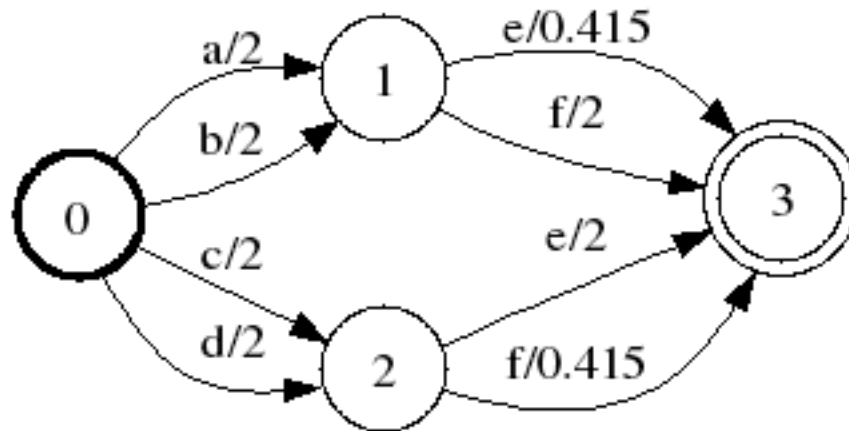
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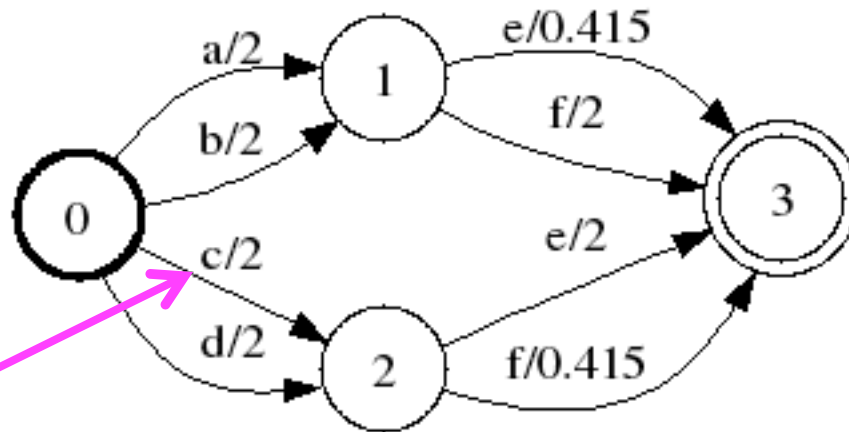
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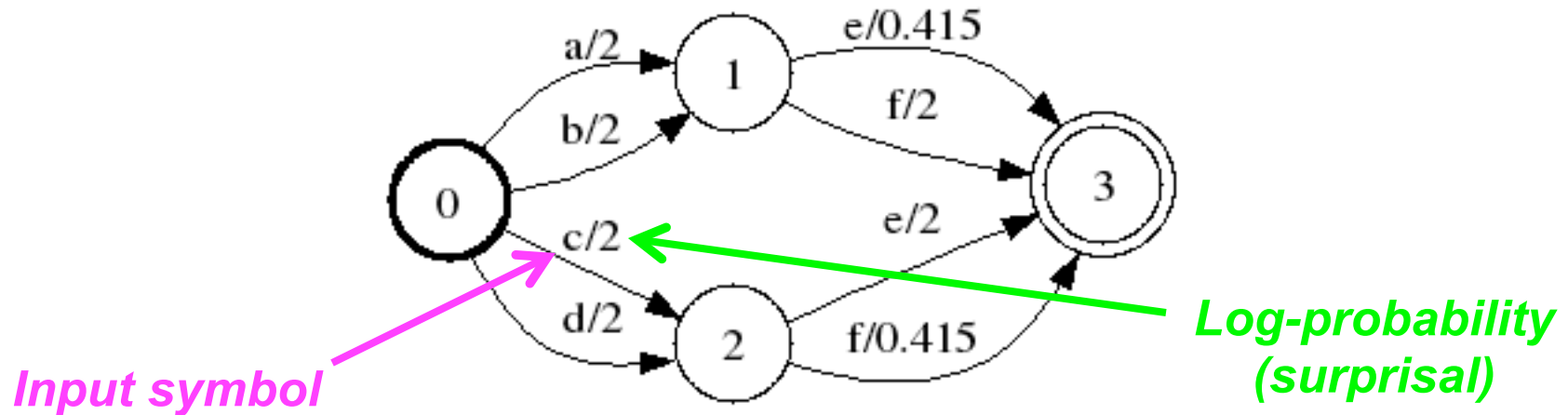
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Input symbol

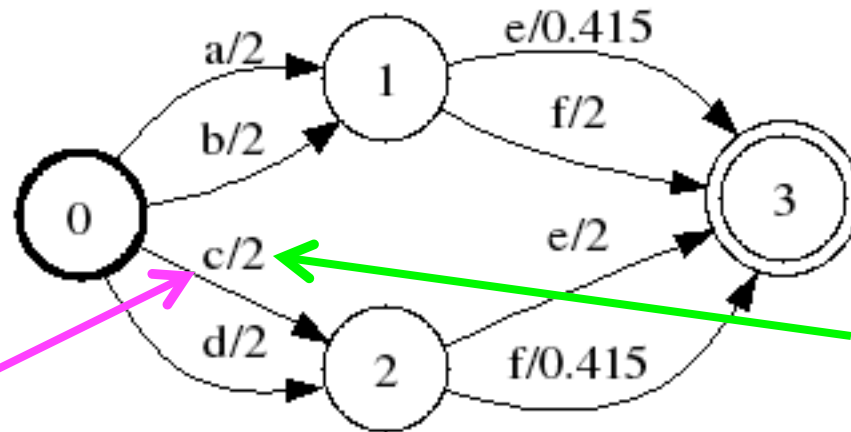
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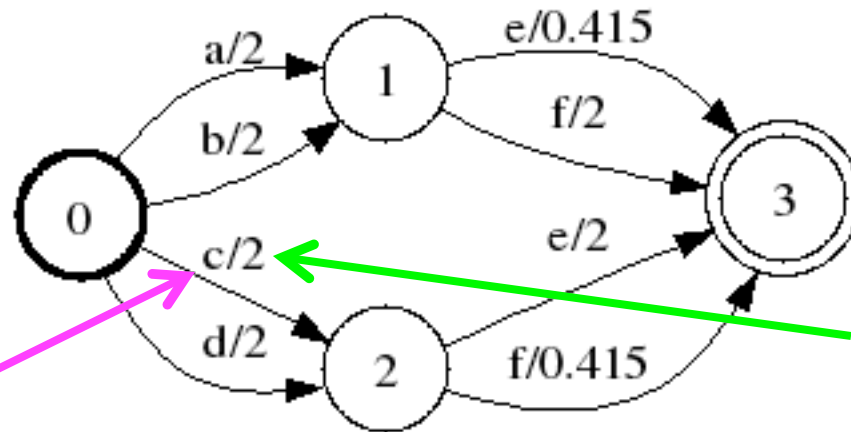
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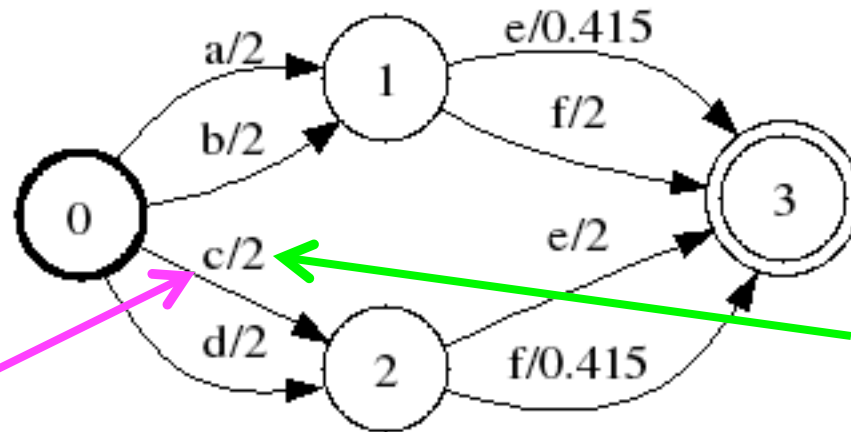
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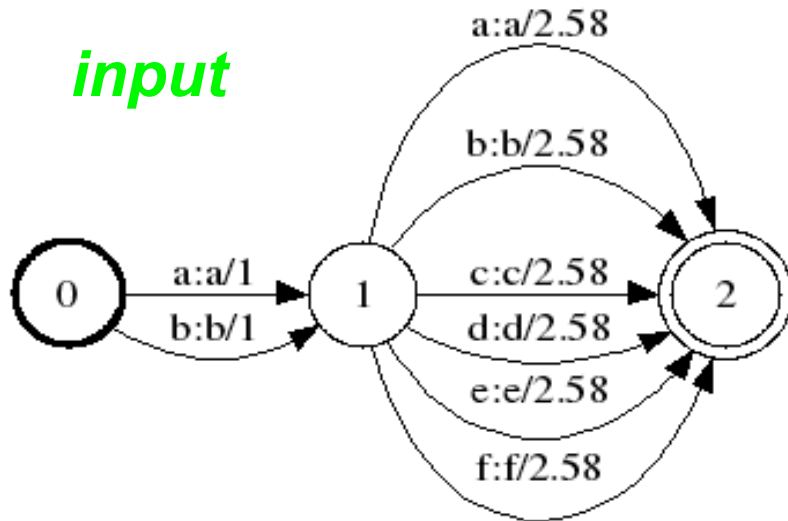
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Combining grammar & uncertain input

- Bayes' Rule says that the *evidence* and the *prior* should be combined (multiplied)
- For probabilistic grammars, this combination is the formal operation of *weighted intersection*

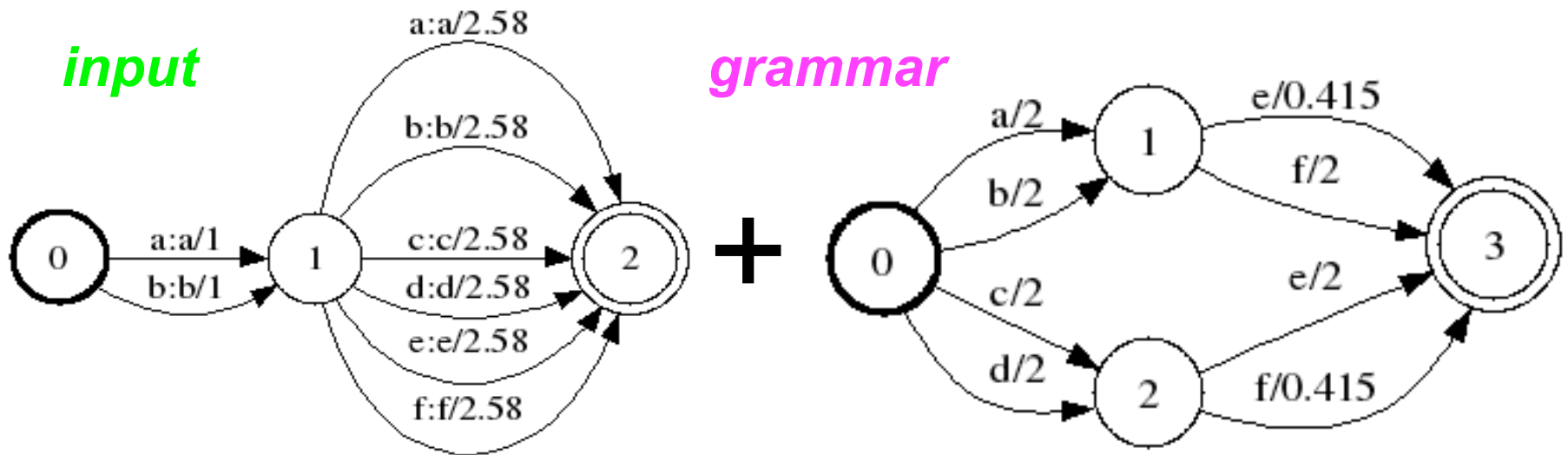
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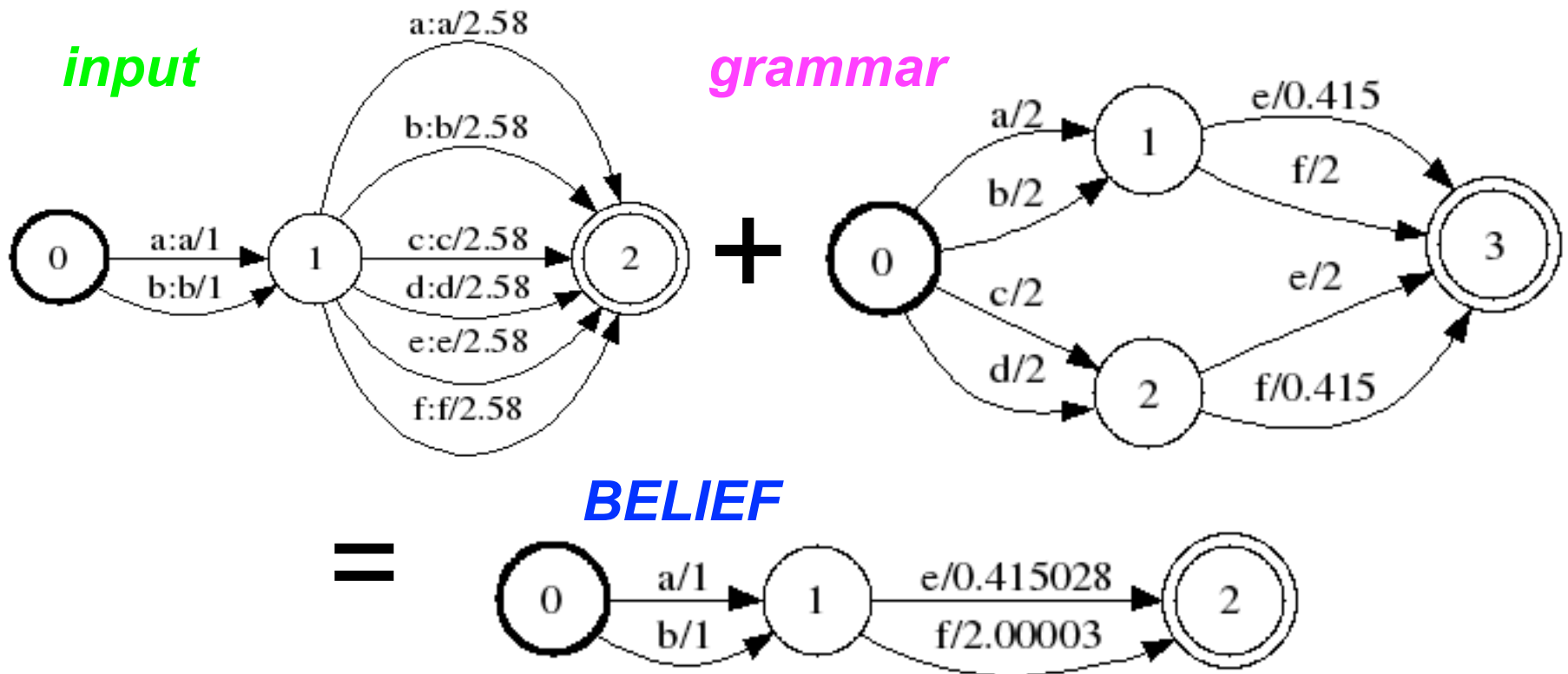
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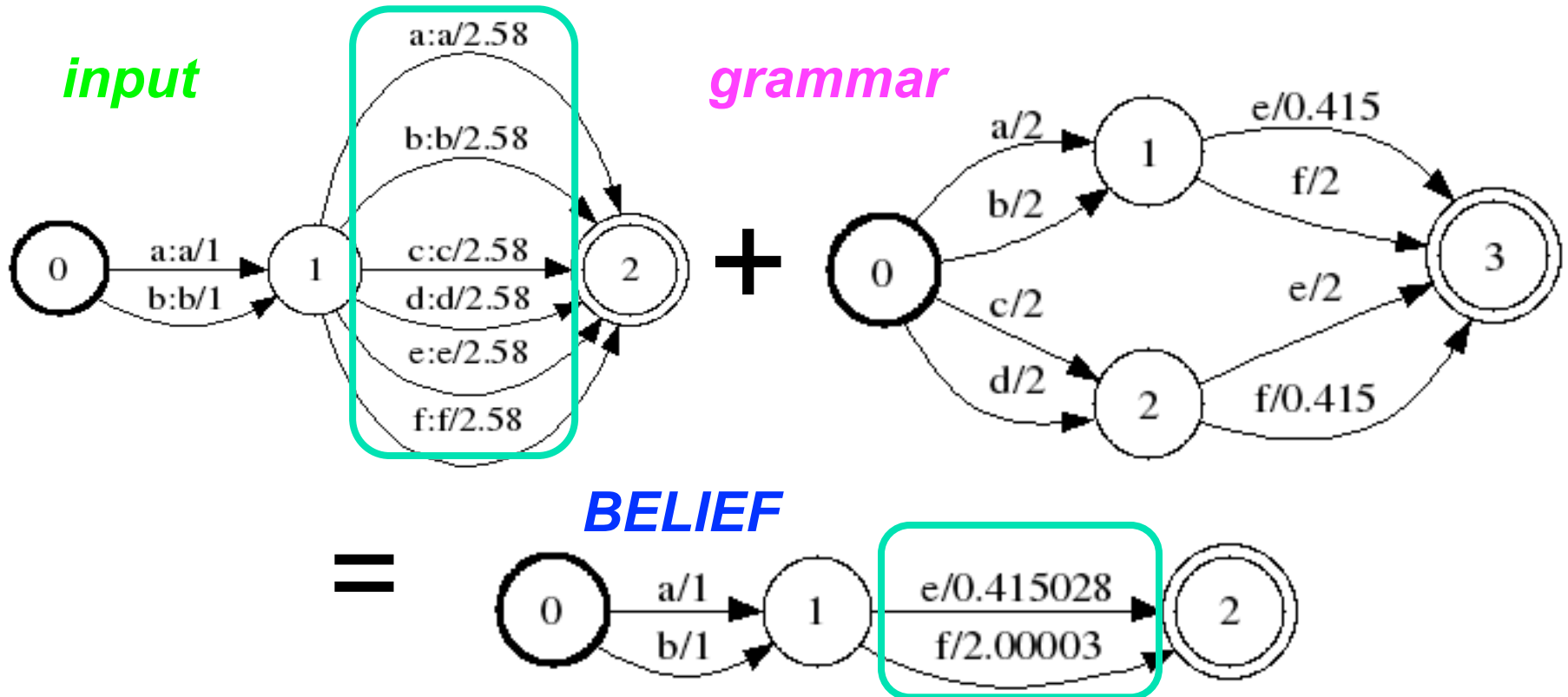
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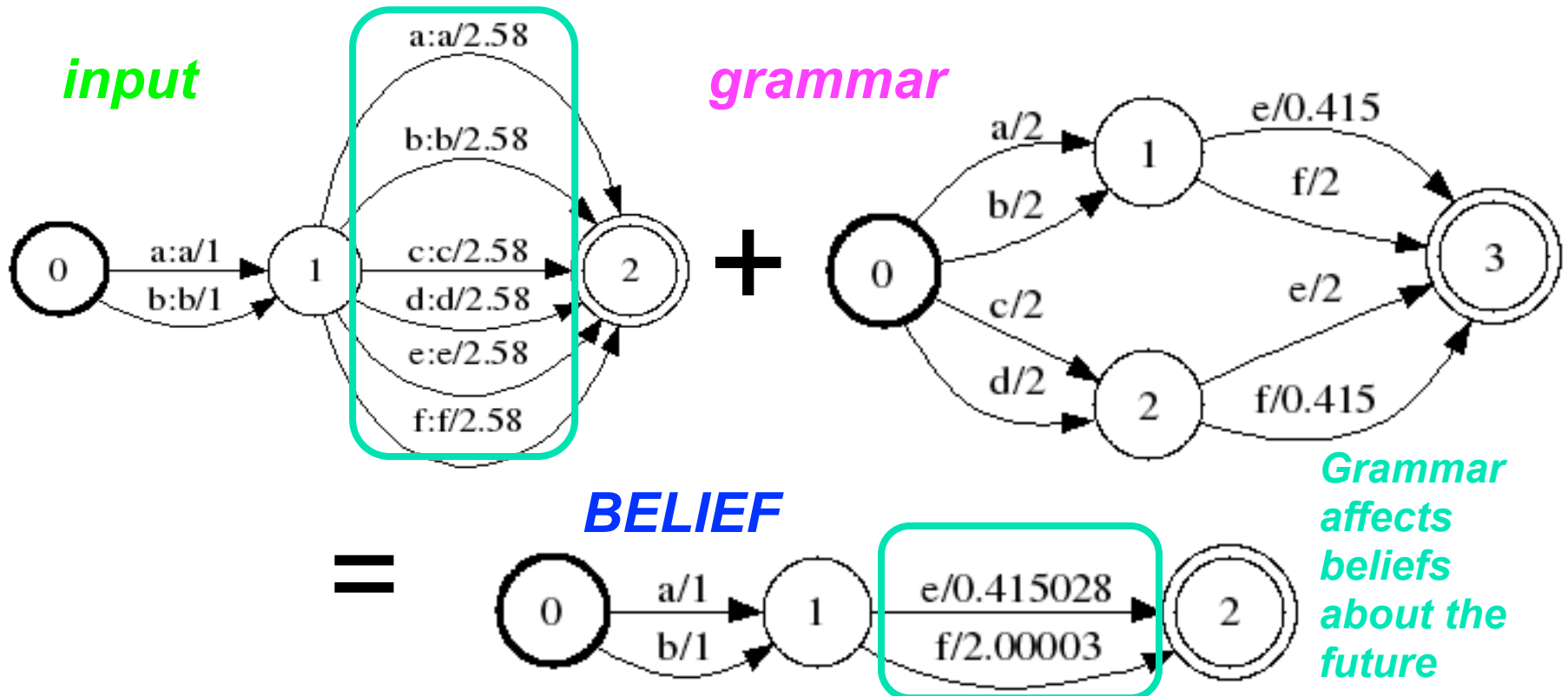
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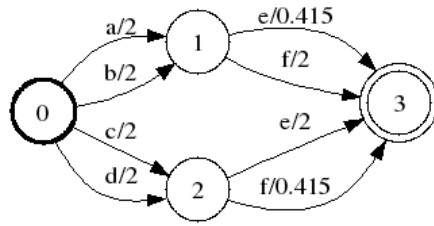
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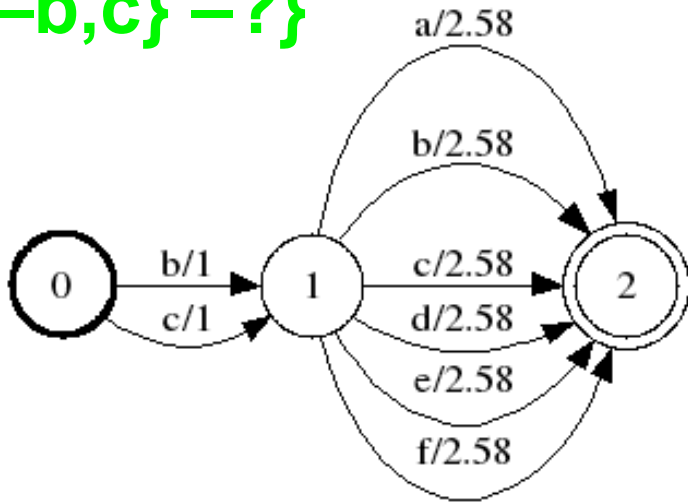
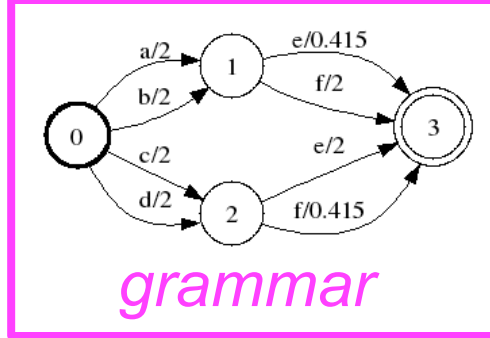
Revising beliefs about the past

- When we're uncertain about the future, grammar + partial input can affect beliefs about what will happen
- With uncertainty of the past, grammar + future input can affect beliefs about *what has already happened*

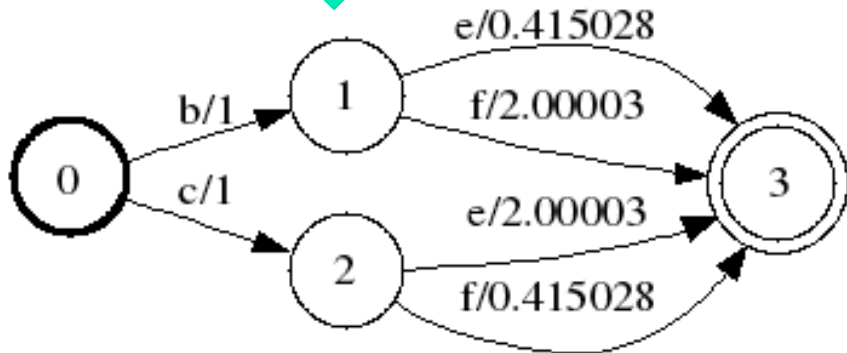
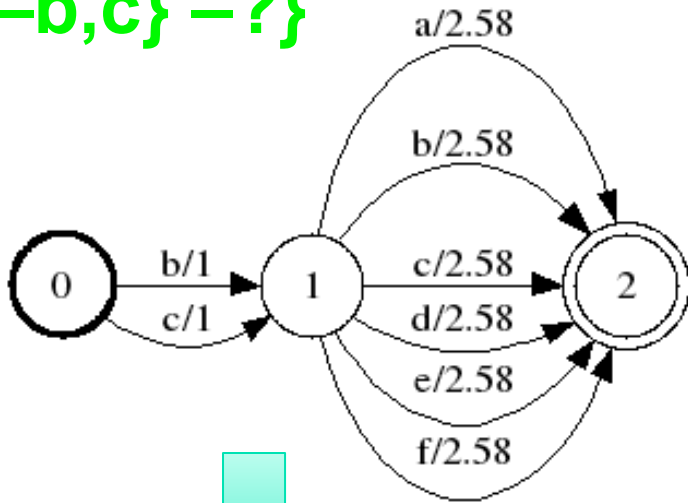
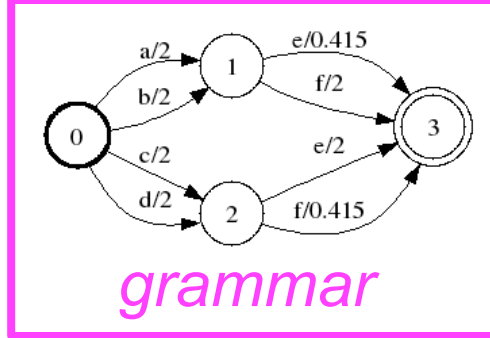


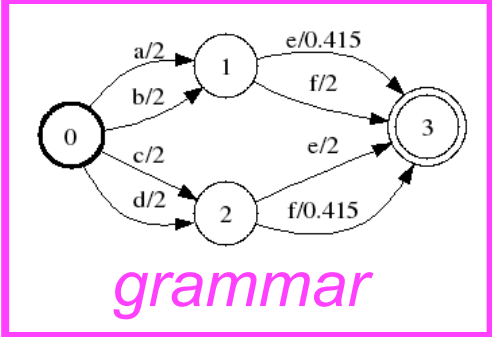
grammar

word 1
-b,c} -?}

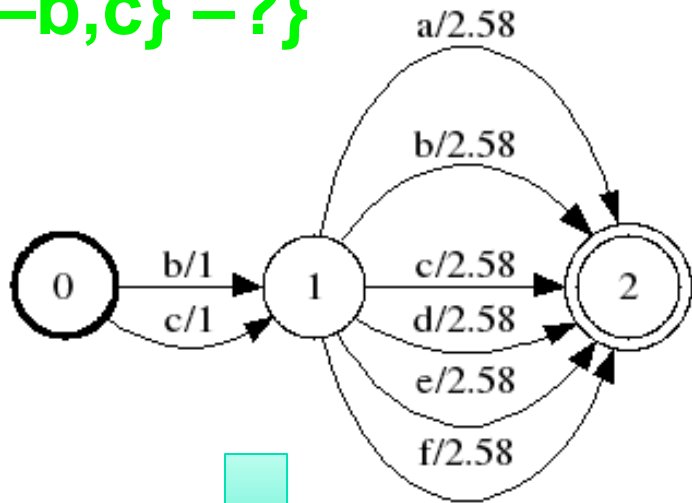


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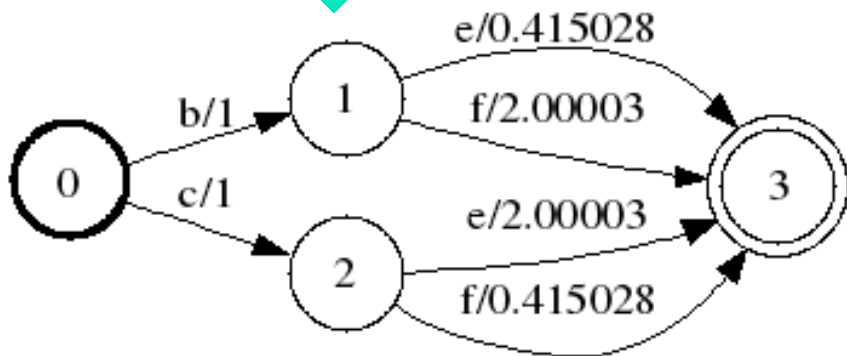
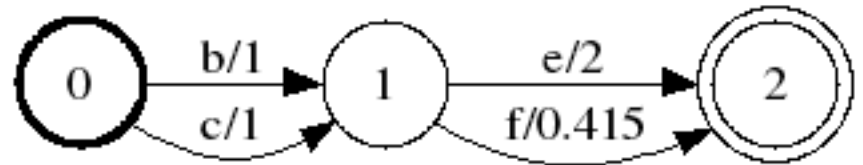


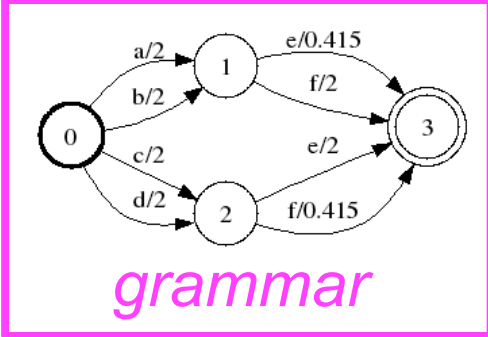


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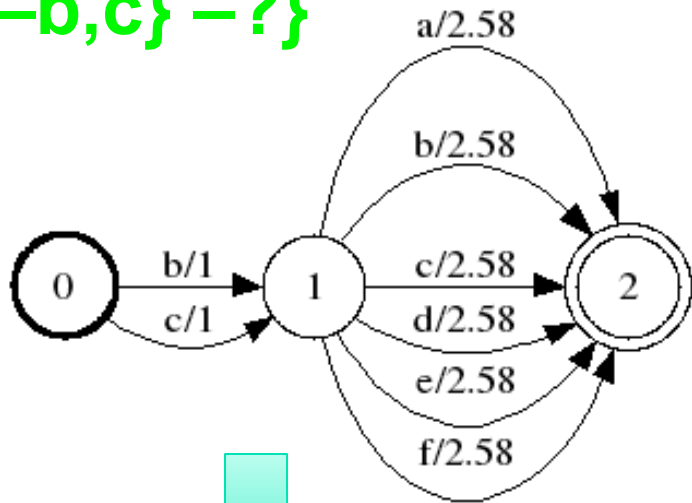


words 1 + 2
-b,c} -f,e}

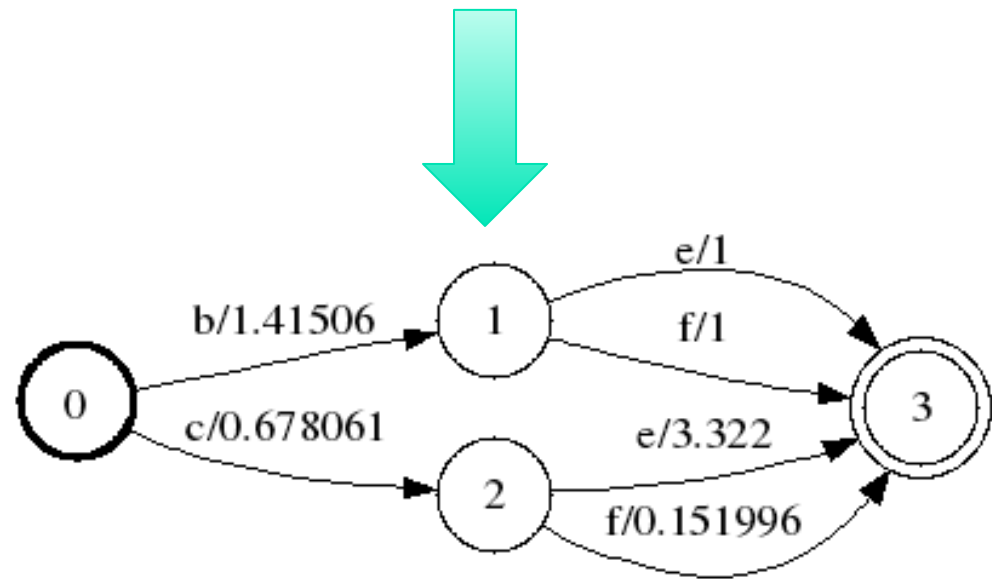
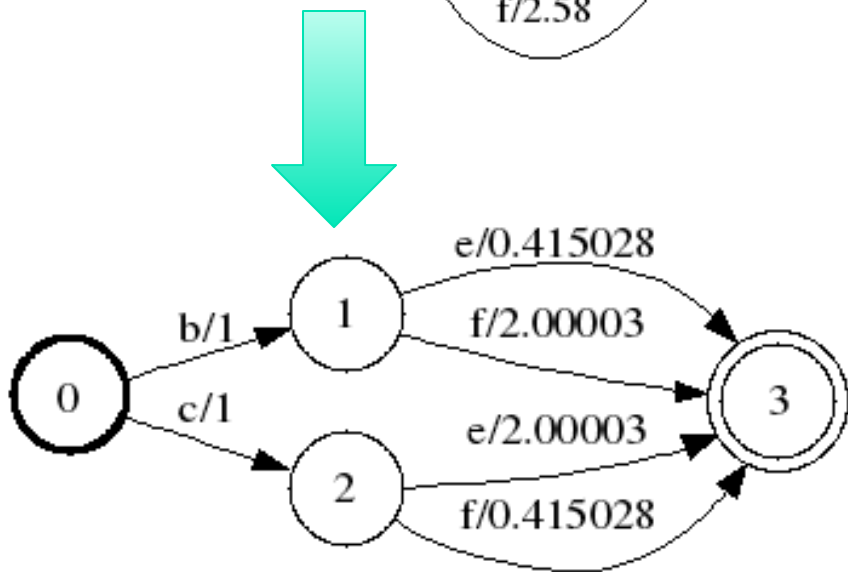
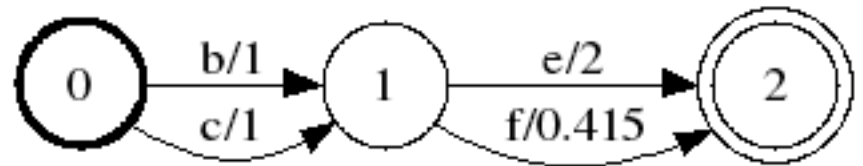


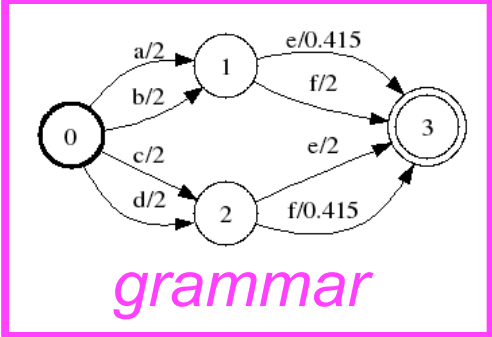


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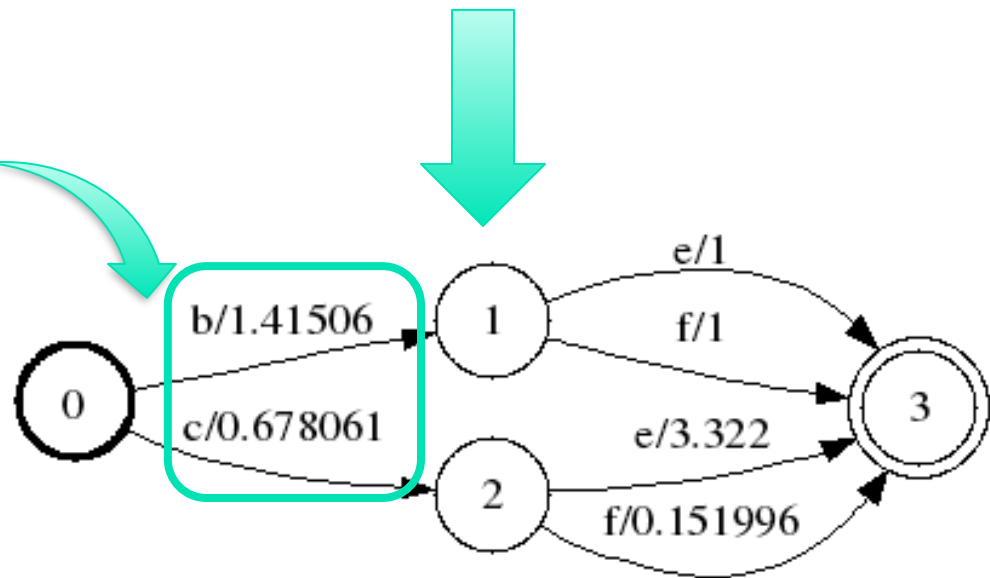
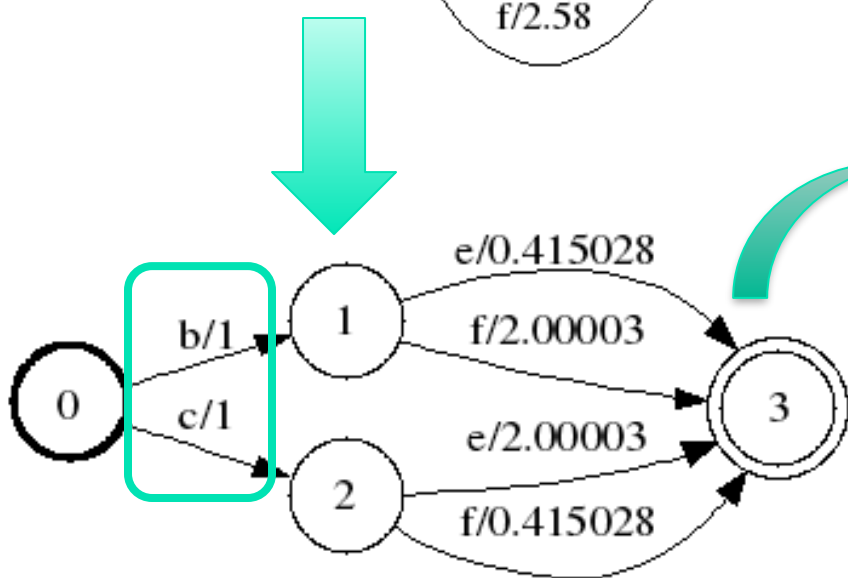
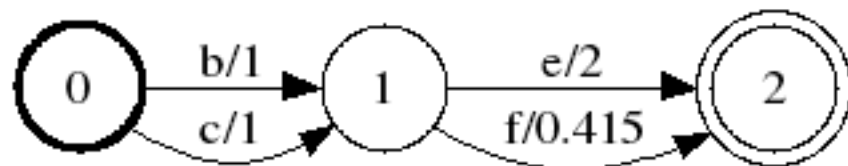
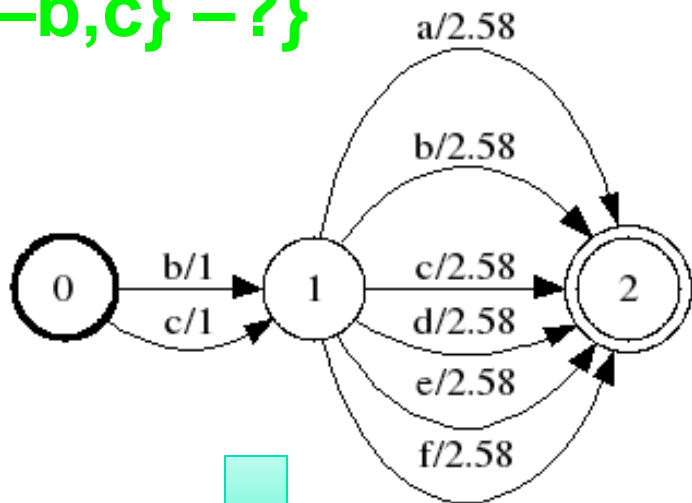
words 1 + 2
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word 1
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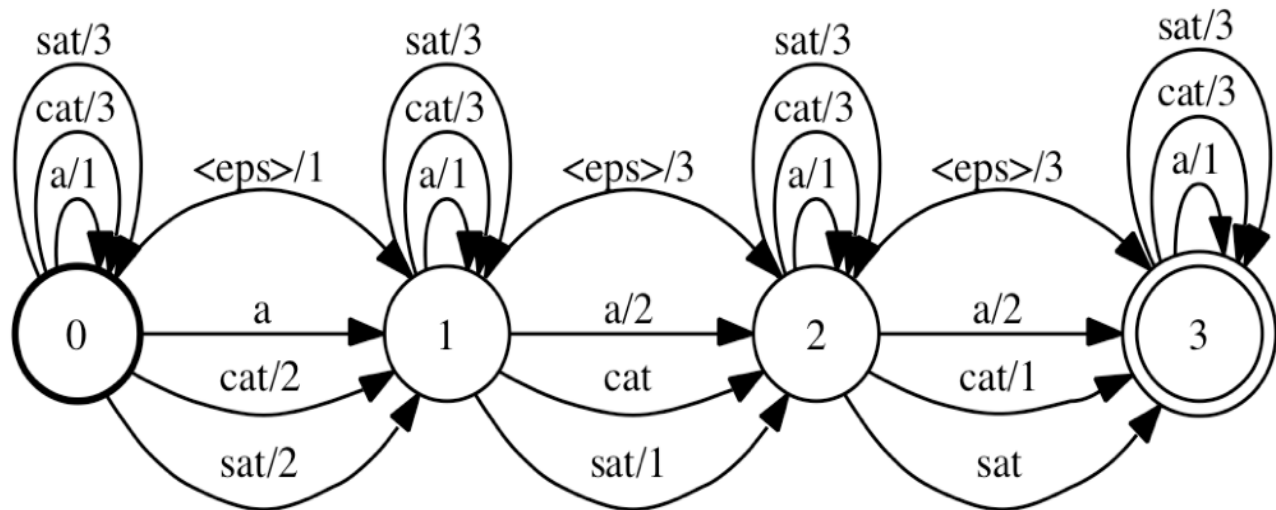
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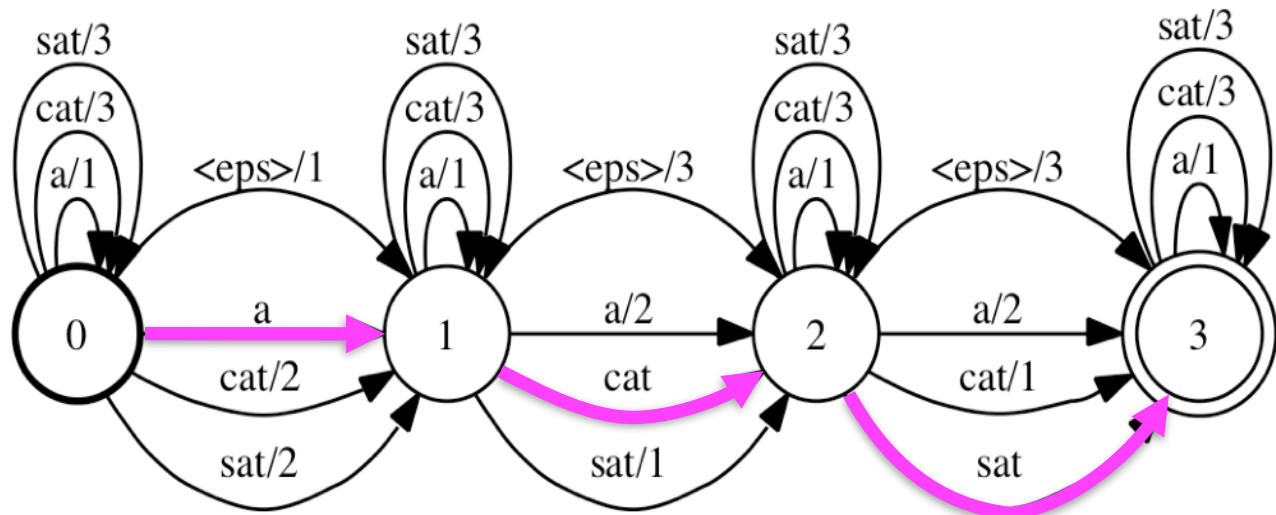


Result of K_{LD} applied to $\mathbf{w}^* = \mathbf{a\ cat\ sat}$

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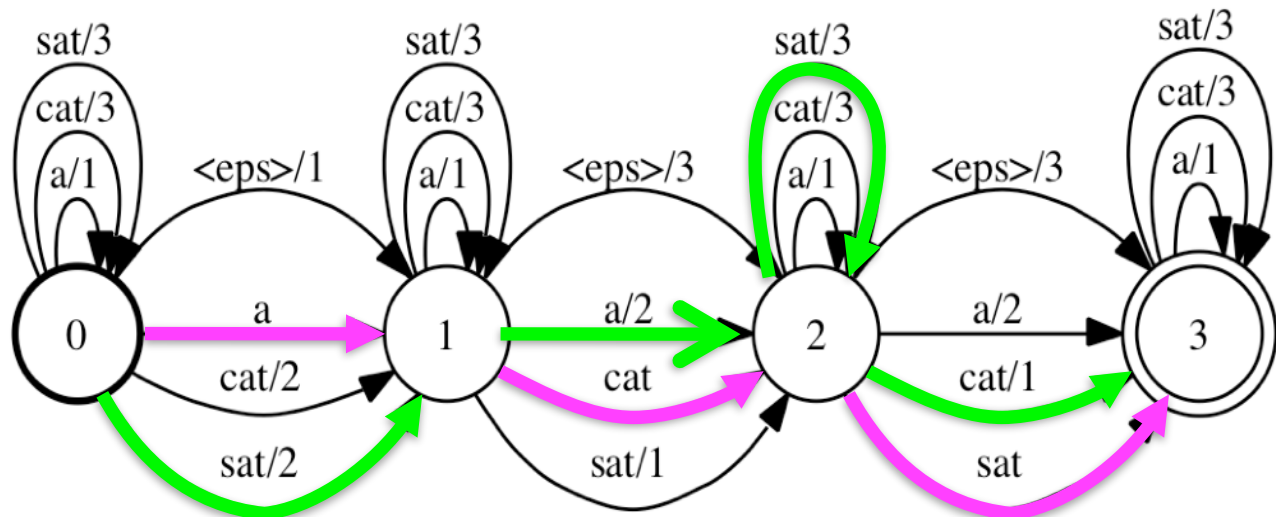
Cost(*a cat sat*)=0

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Cost(*a cat sat*)=0

Cost(*sat a sat cat*)=8

Result of K_{LD} applied to $\mathbf{w}^* = \mathbf{a\ cat\ sat}$

Rational analysis

- Background assumption: cognitive agent is optimized via evolution and learning to solve everyday tasks effectively
 1. Specify precisely the goals of the cognitive system
 2. Formalize model of the environment adapted to
 3. Make minimal assumptions re: computational limitations
 4. Derive predicted optimal behavior given 1—3
 5. Compare predictions with empirical data
 6. If necessary, iterate 1—5

Incremental inference under uncertain input

*The coach smiled at the player **tossed** the frisbee*

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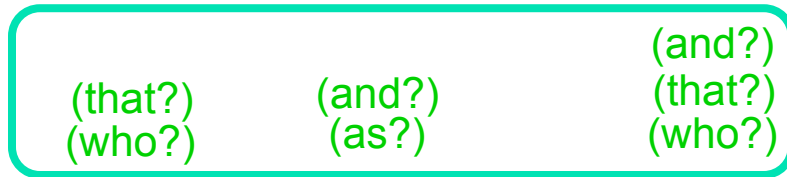
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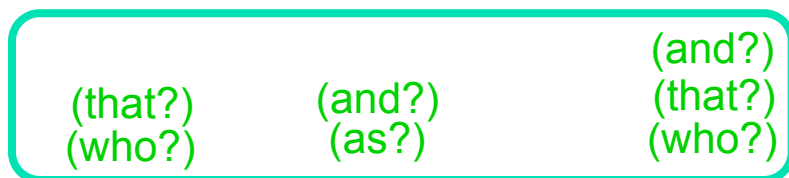


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- Hypothesis: the boggle at “tossed” involves *what the comprehender wonders whether she might have seen*

Rational analysis

- Background assumption: cognitive agent is optimized via evolution and learning to solve everyday tasks effectively
 1. Specify precisely the goals of the cognitive system
 2. Formalize model of the environment adapted to
 3. Make minimal assumptions re: computational limitations
 4. Derive predicted optimal behavior given 1—3
 5. Compare predictions with empirical data
 6. If necessary, iterate 1—5

The core of the intuition

the coach smiled...

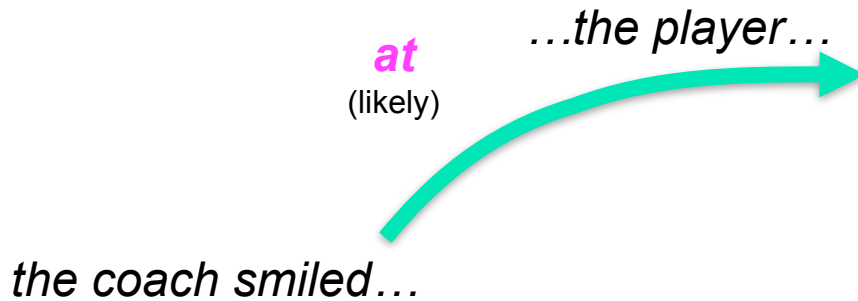
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- Grammar & input come together to determine two possible “paths” through the partial sentence:

the coach smiled...

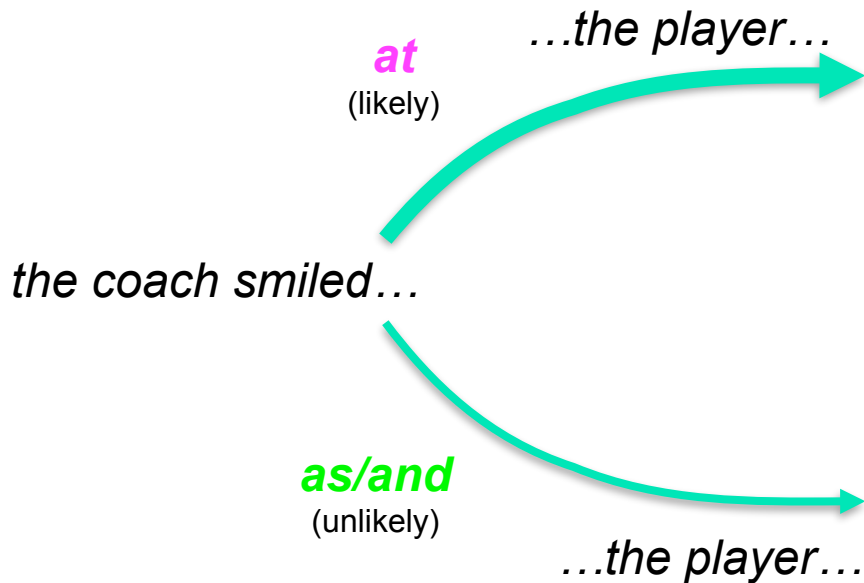
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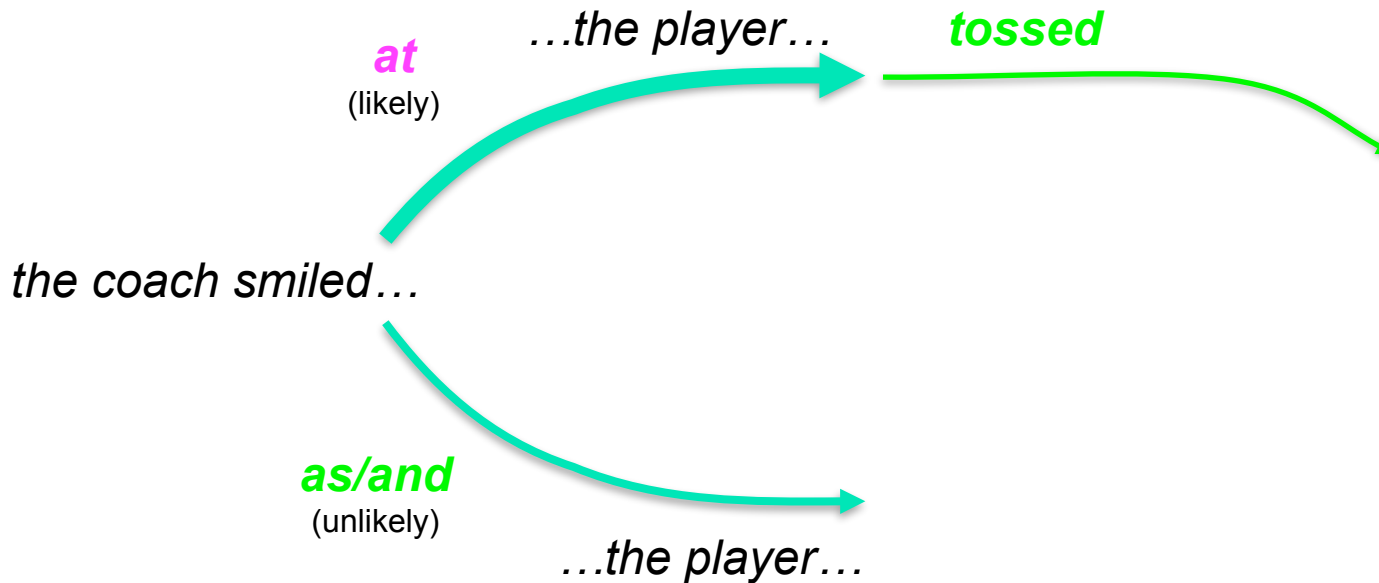
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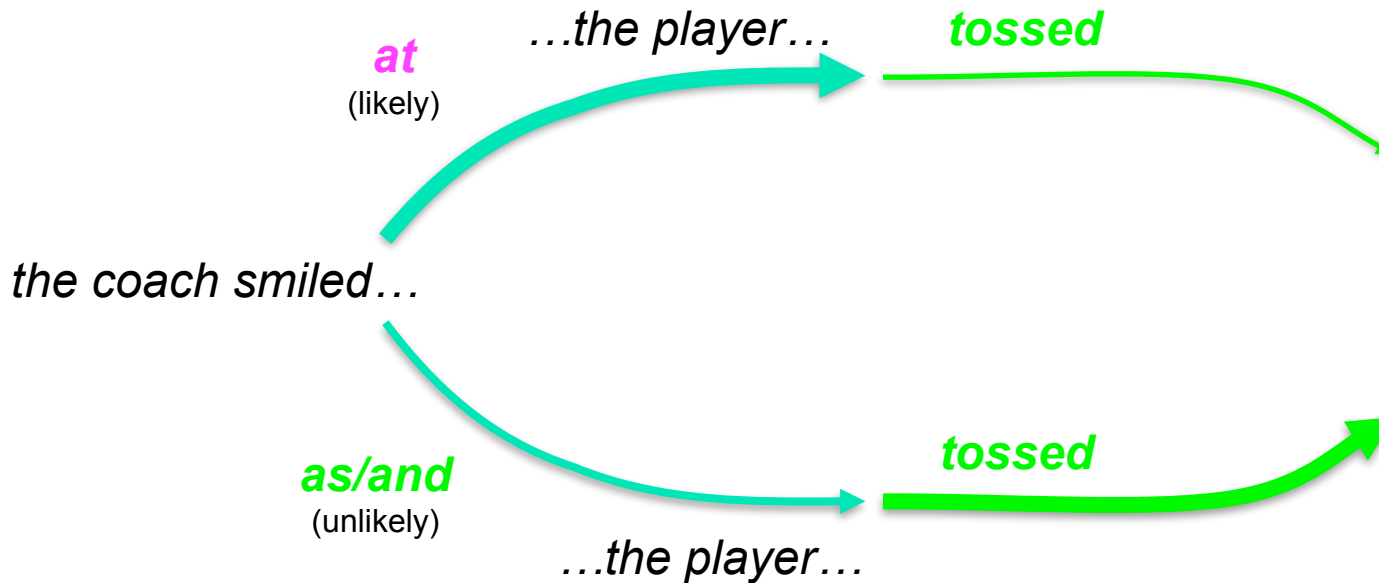
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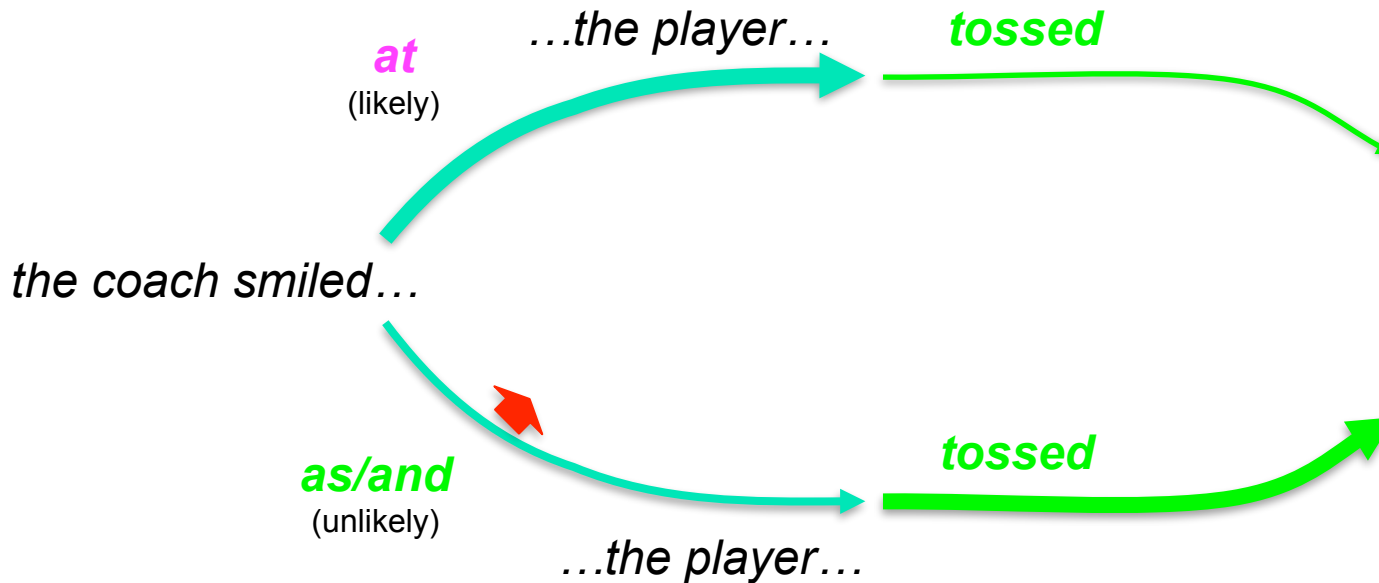
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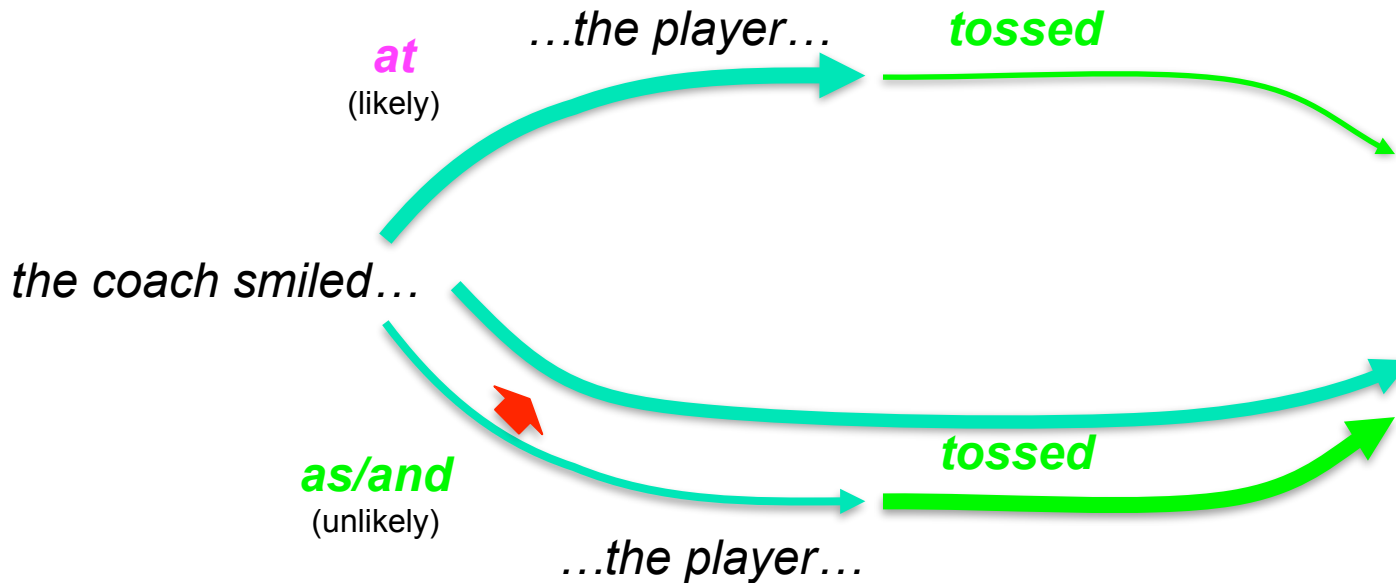
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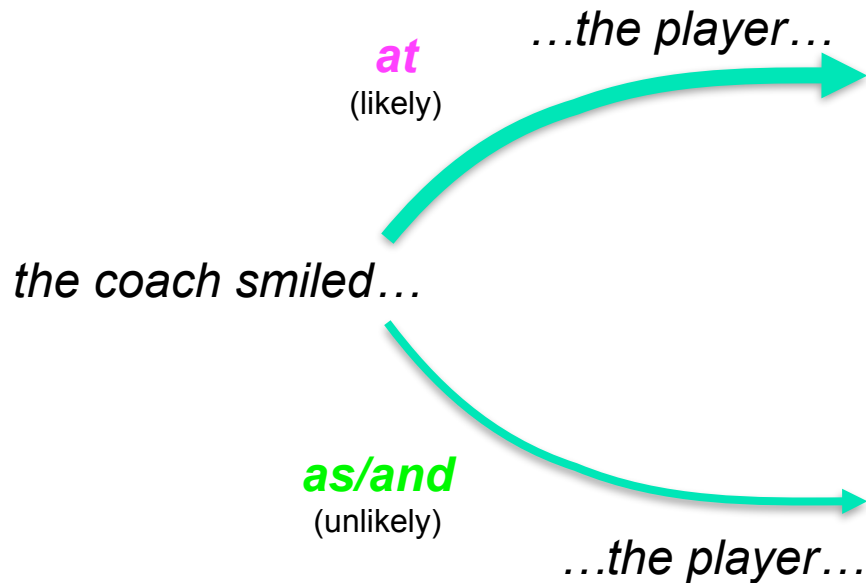
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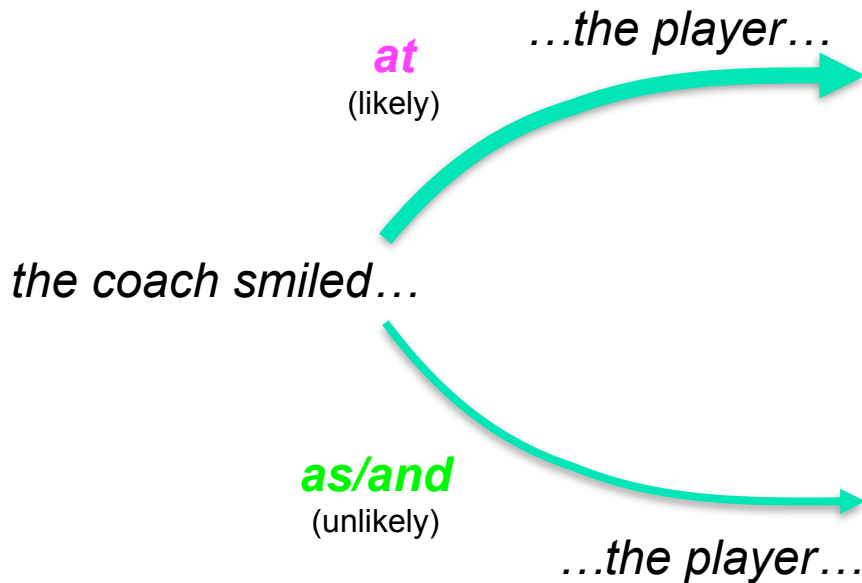
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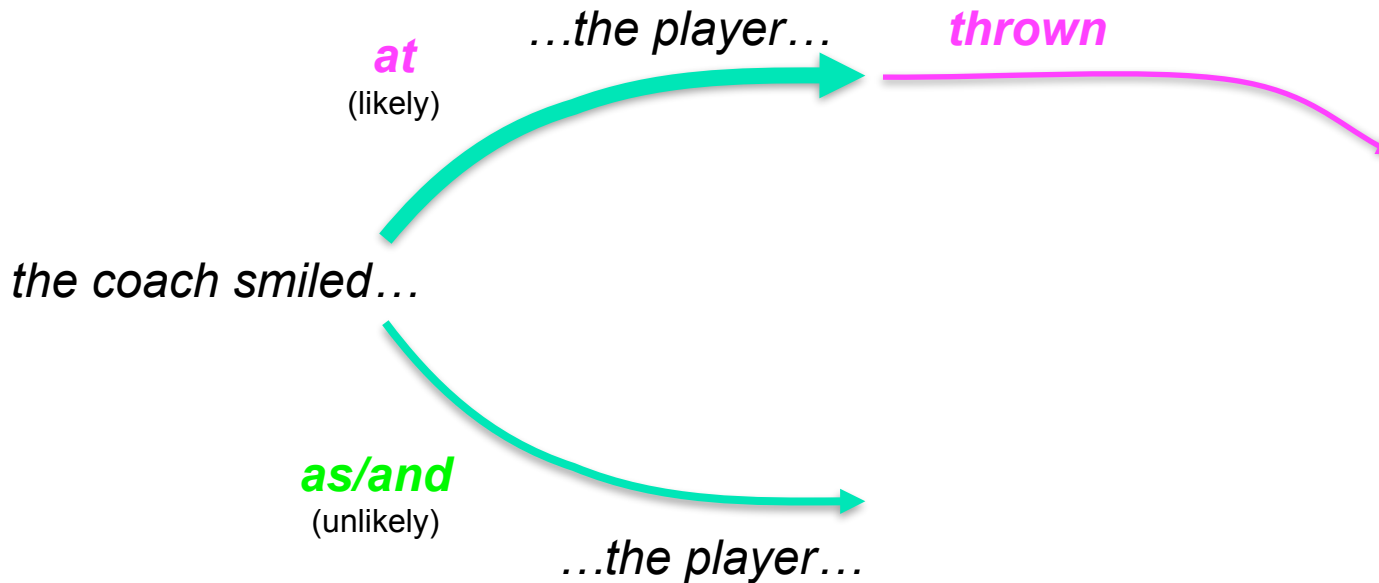
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- tossed** is more likely to happen along the bottom path
 - This creates a large shift in belief in the **tossed** condition

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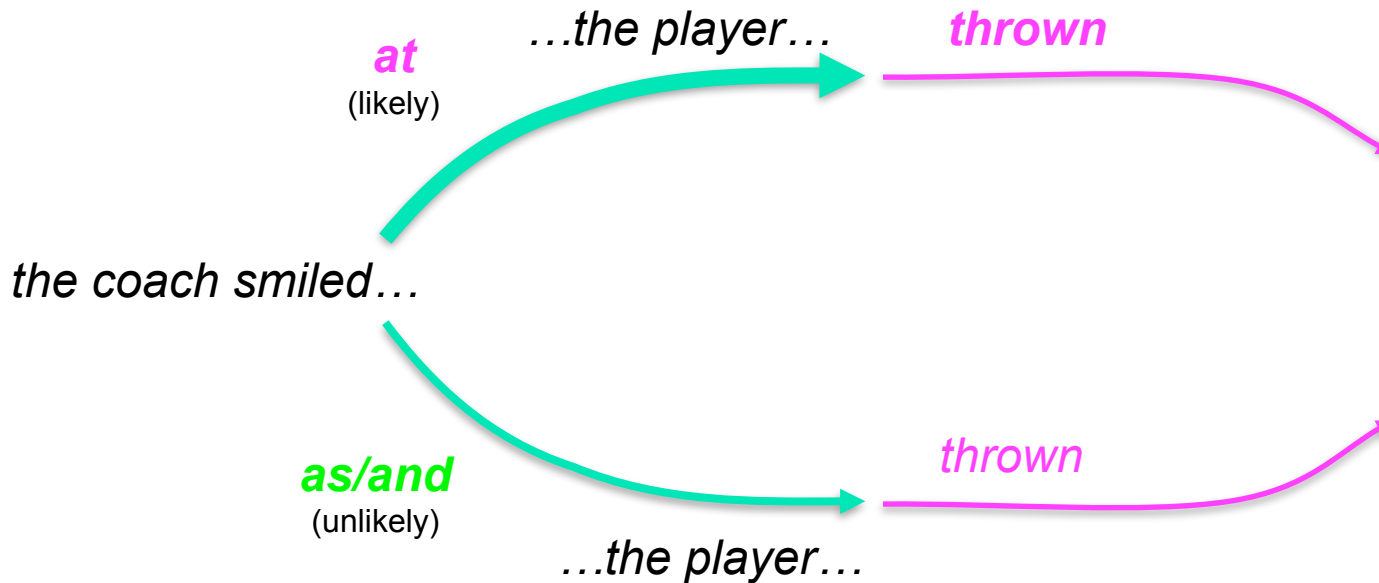
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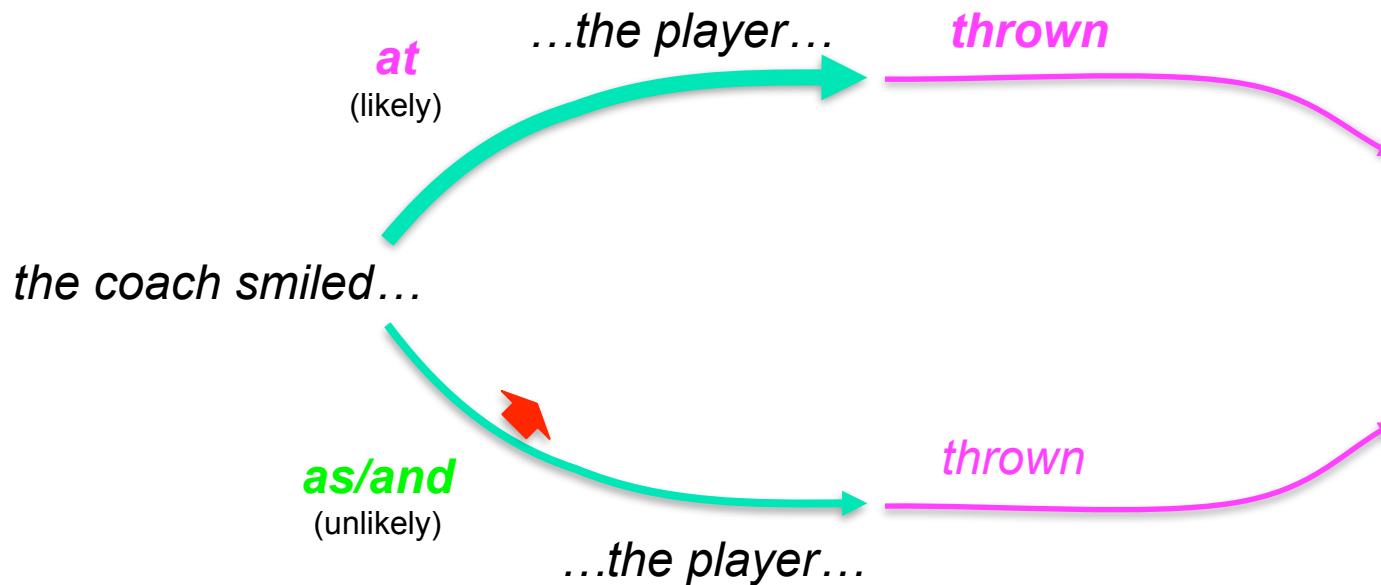
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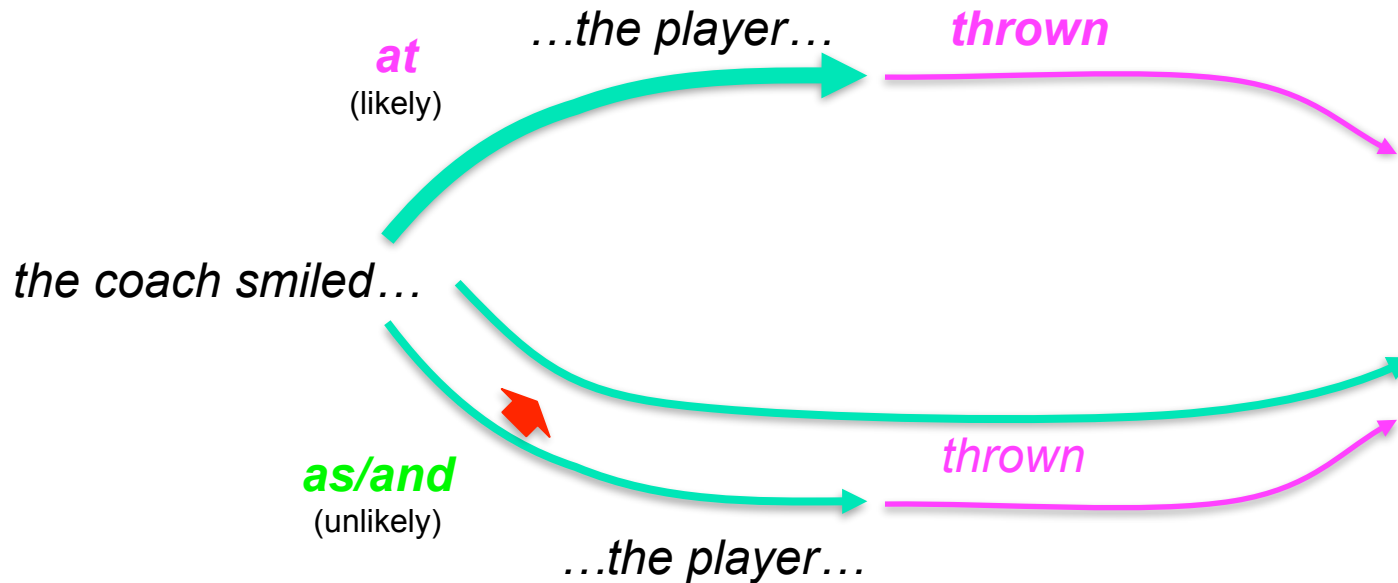
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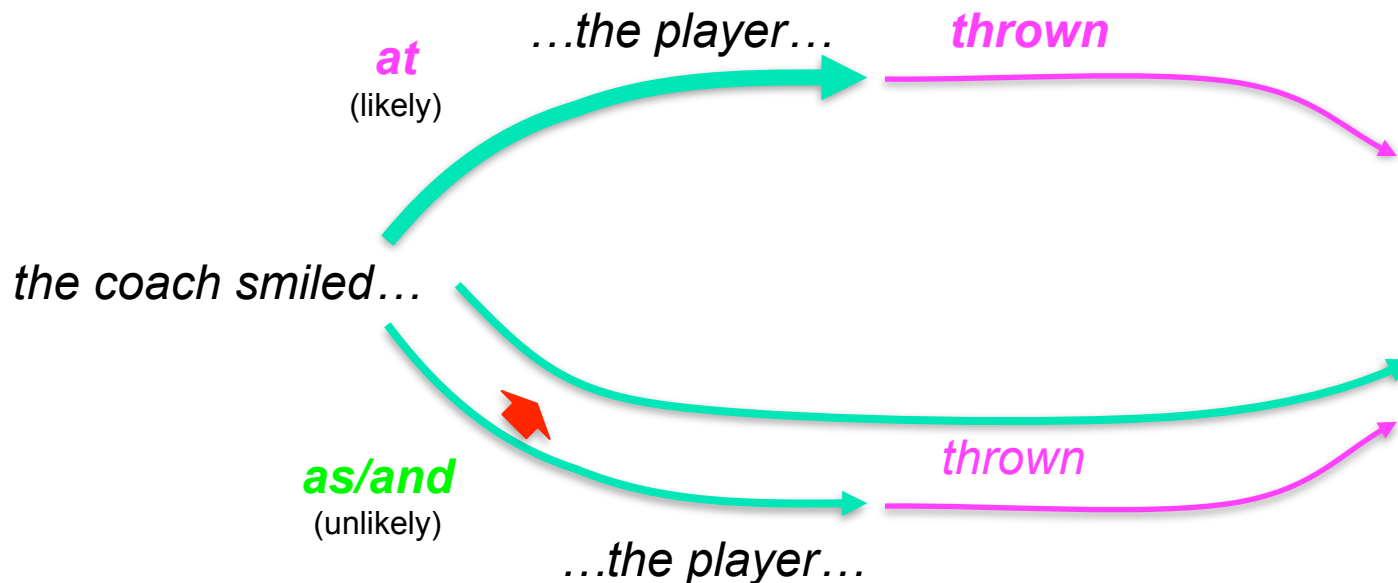
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- tossed** is more likely to happen along the bottom path
 - This creates a large shift in belief in the **tossed** condition
- thrown** is very unlikely to happen along the bottom path
 - As a result, there is no corresponding shift in belief

Ingredients for the model

$$P(\mathbf{w}|\mathbf{w}^*) \propto \underbrace{P_C(\mathbf{w})}_{\text{Prior}} \underbrace{Q(\mathbf{w}, \mathbf{w}^*)}_{\text{Expected evidence}}$$

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- We need one more ingredient:
 - a **quantified signal** of the alarm induced by word w_i about changes in beliefs about the past

Quantifying alarm about the past

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- *Relative Entropy* (KL-divergence) is a natural metric of change in a probability distrib. (Levy, 2008; Itti & Baldi, 2005)

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- The change induced by w_i is the **error identification signal** EIS_i , defined as

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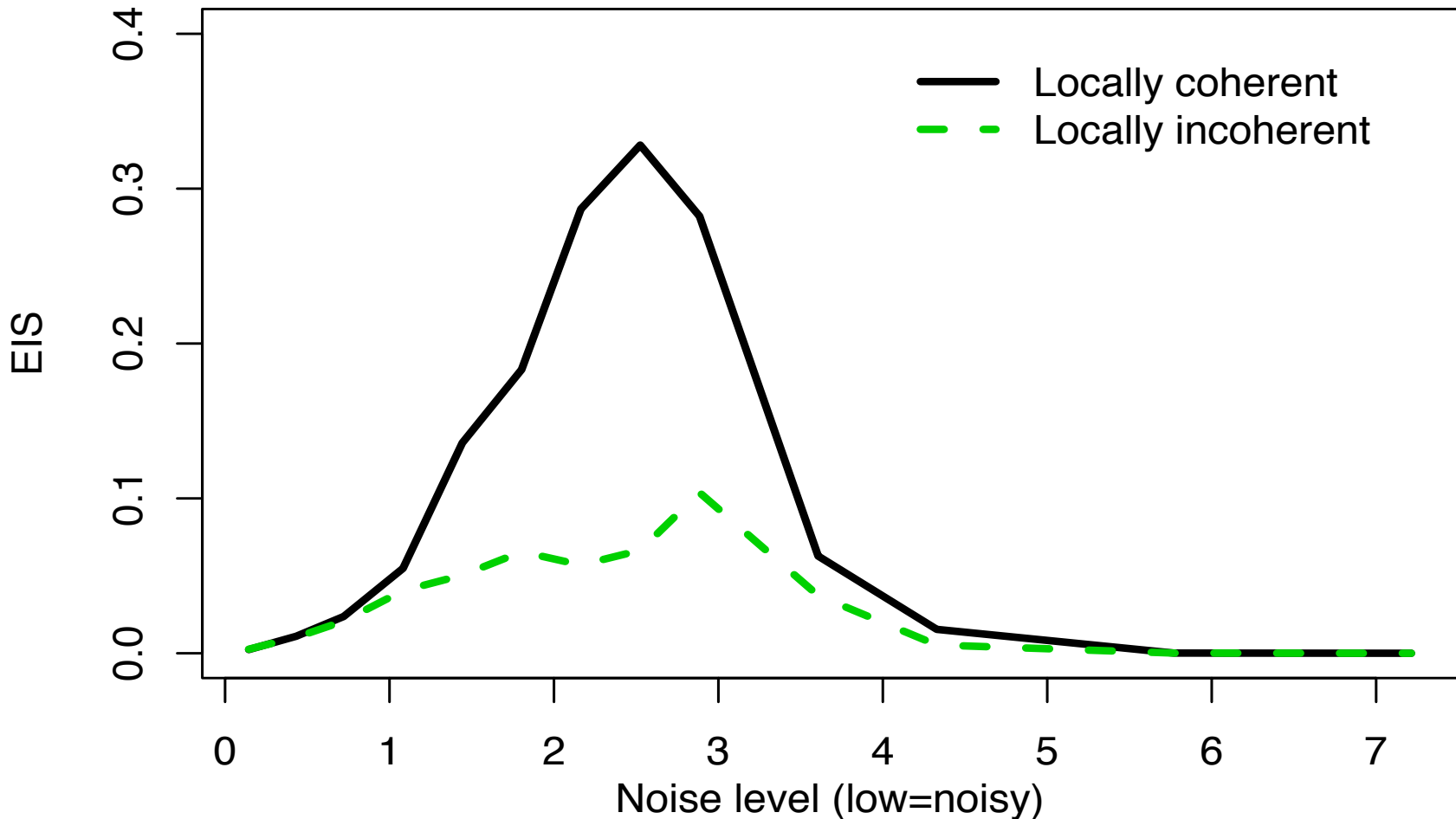
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 - conditions on words 0 through i* (arrow pointing to P_i)
 - strings up to but excluding word j* (arrow pointing to $w_{[0,j]}$)
- The change induced by w_i is the **error identification signal EIS_i** , defined as

$$D \left(\underbrace{P_i \left(w_{[0,i]} \right)}_{\text{new distribution}} \parallel \underbrace{P_{i-1} \left(w_{[0,i]} \right)}_{\text{old distribution}} \right)$$

Results on local-coherence sentences

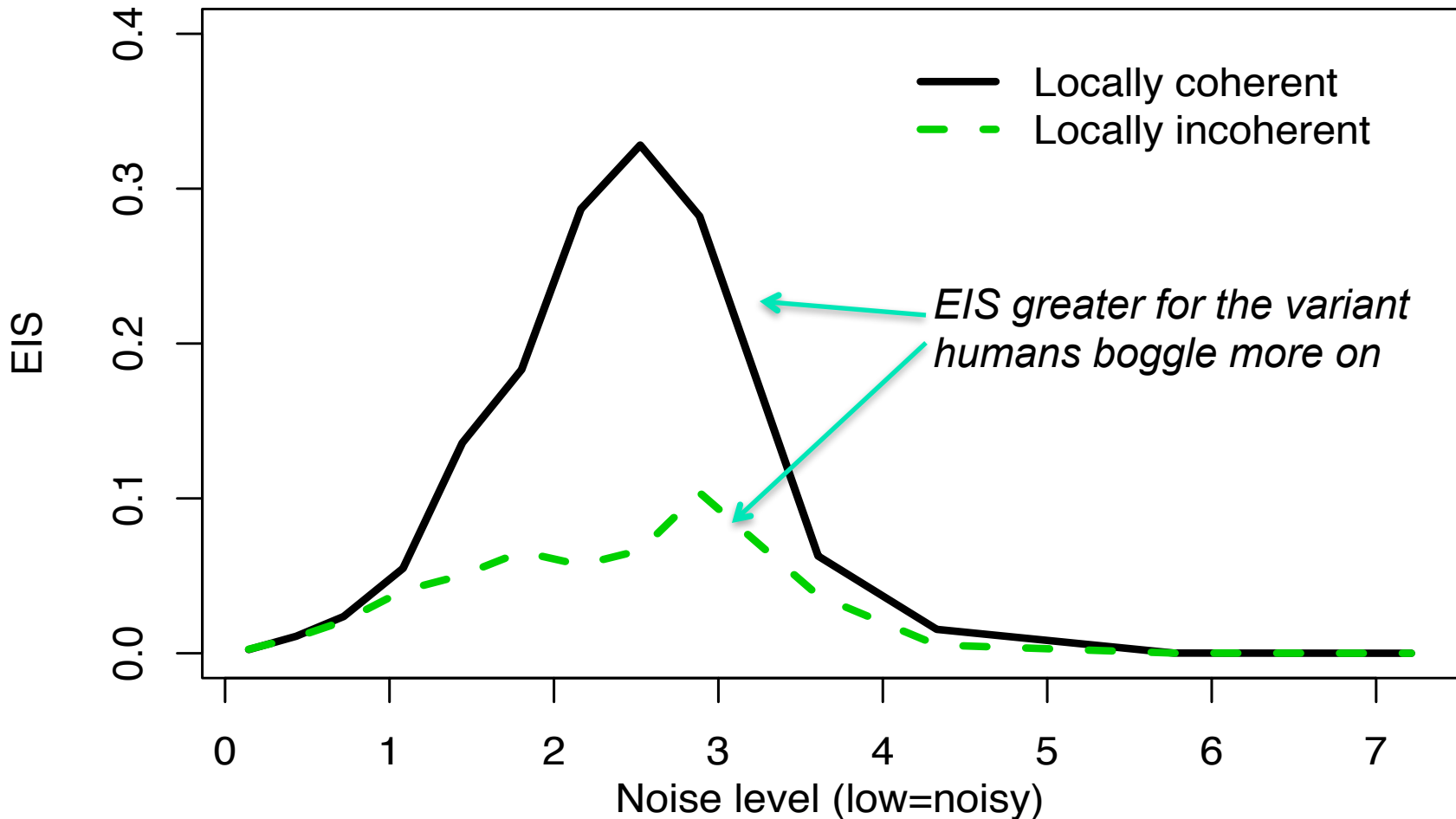
- Locally coherent: *The coach smiled at the player **tossed** the frisbee*
- Locally incoherent: *The coach smiled at the player **thrown** the frisbee*



(All sentences of Tabor et al. 2004 with lexical coverage in model)

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Today's summary

- Reviewed principles of rational analysis and its application to theory of language comprehension
- Examined a phenomenon challenging for surprisal theory
- Proposed a noisy-channel processing theory, using information theory and probabilistic grammars
- Developed a hypothesis within the theory for the challenging phenomenon
-

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Prediction 2: hallucinated garden paths

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While the clouds crackled, above the glider soared a magnificent eagle.

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- Readers are ordinarily very good at using commas to guide syntactic analysis:

While the man hunted, the deer ran into the woods

While Mary was mending the sock fell off her lap

- “With a comma after *mending* there would be no syntactic garden path left to be studied.” (Fodor, 2002)

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- We'll see that the story is slightly more complicated.

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Prediction 2: hallucinated garden paths

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A diagram illustrating a garden path sentence. The sentence is "While the clouds crackled, above the glider soared a magnificent eagle." The words "While the clouds crackled," are underlined in red. The words "above the glider" are underlined in blue. A pink arrow points from the end of the blue underline back to the start of the blue underline, indicating a shift in the reader's expectation.

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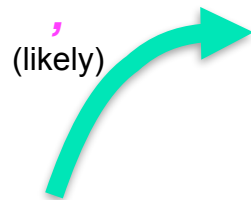
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- Inferences through *...glider* should thus involve a tradeoff between perceptual input and prior expectations

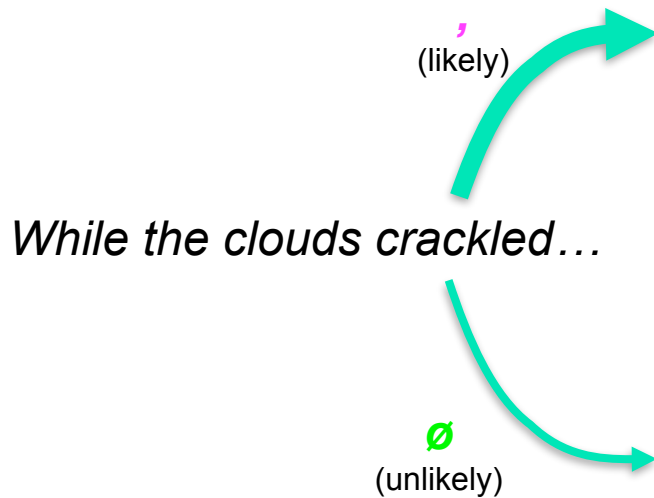
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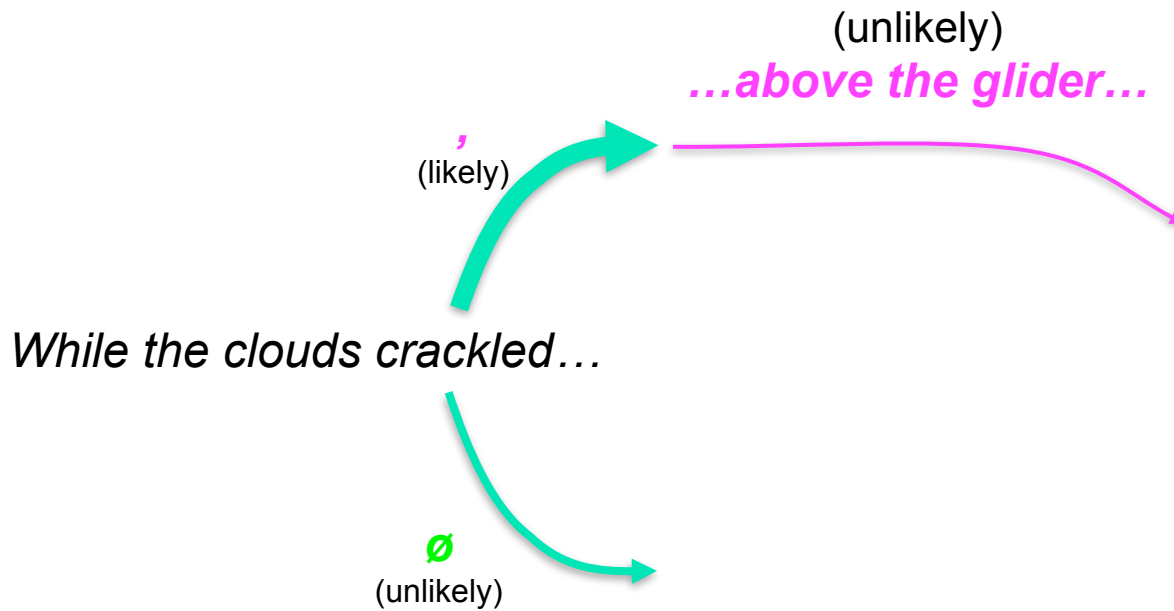


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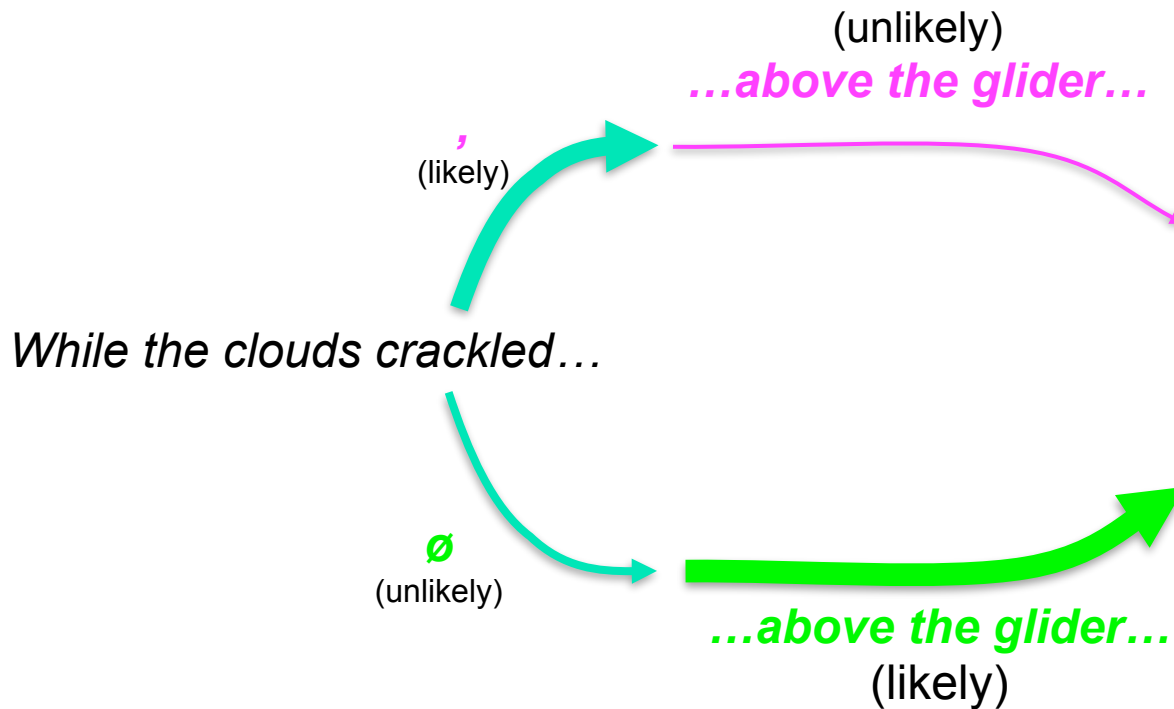
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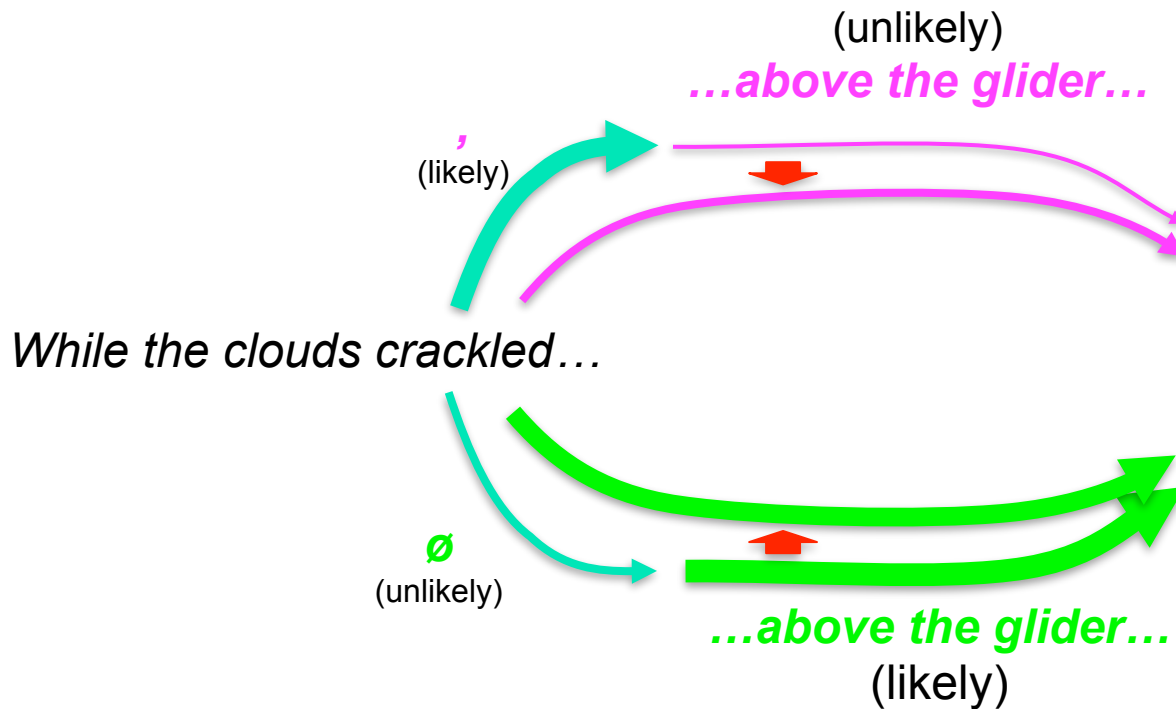
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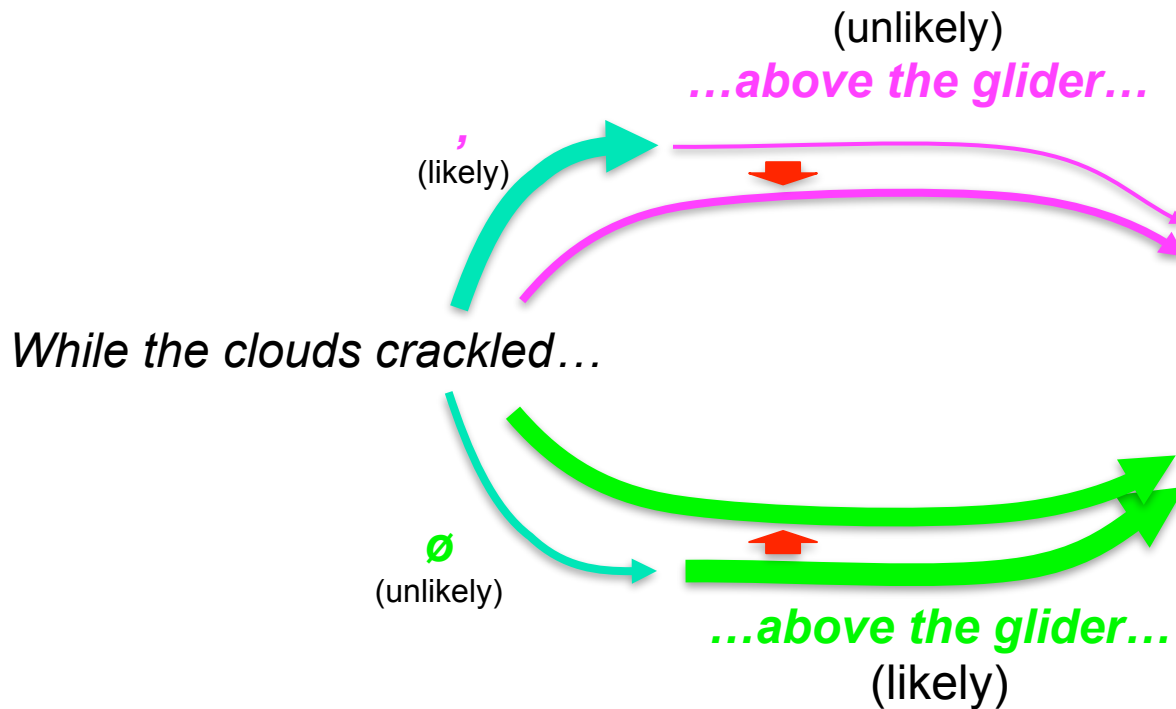
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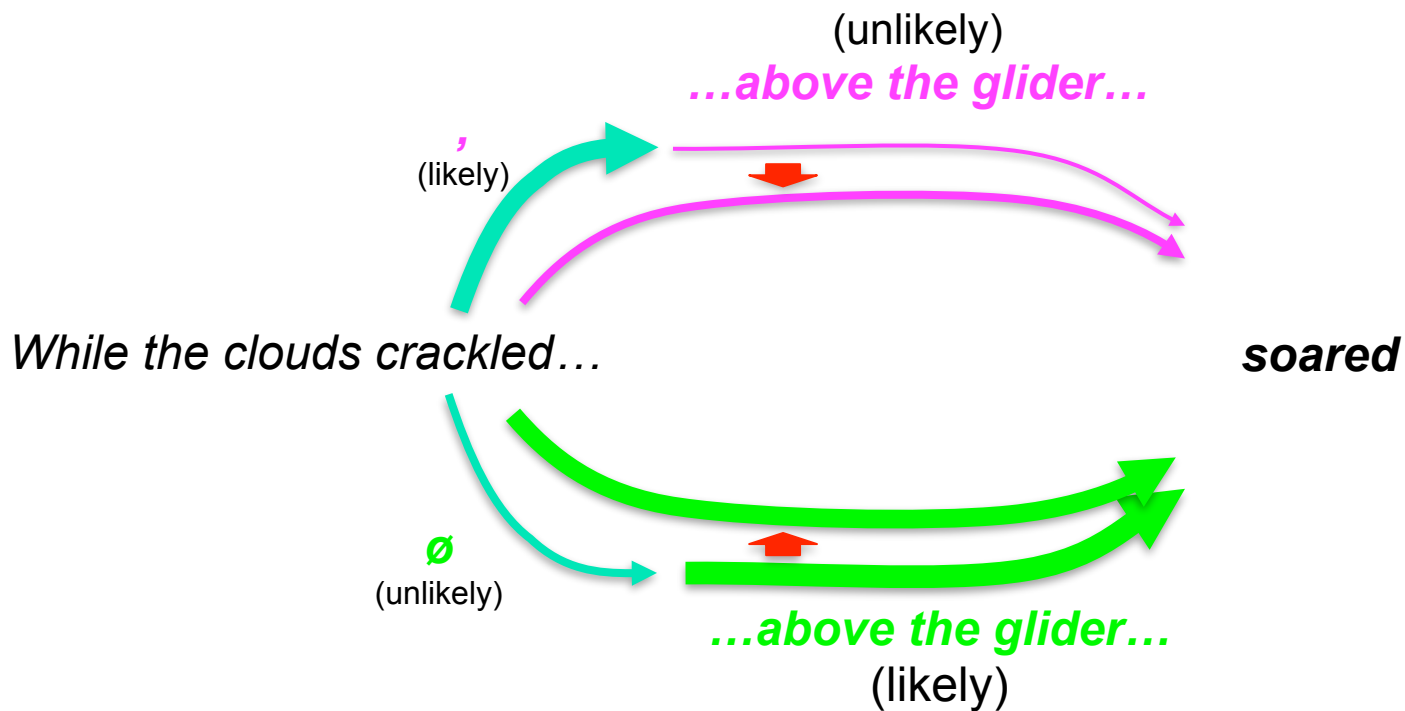
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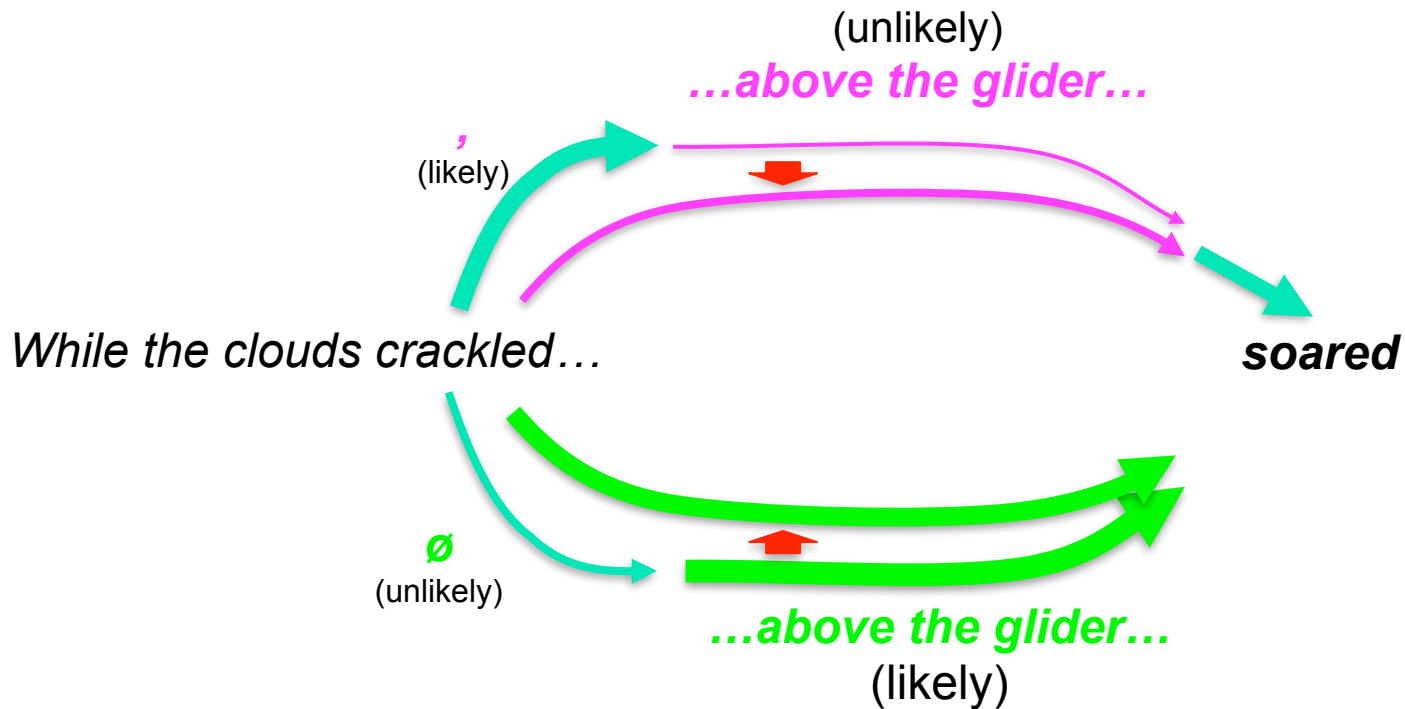
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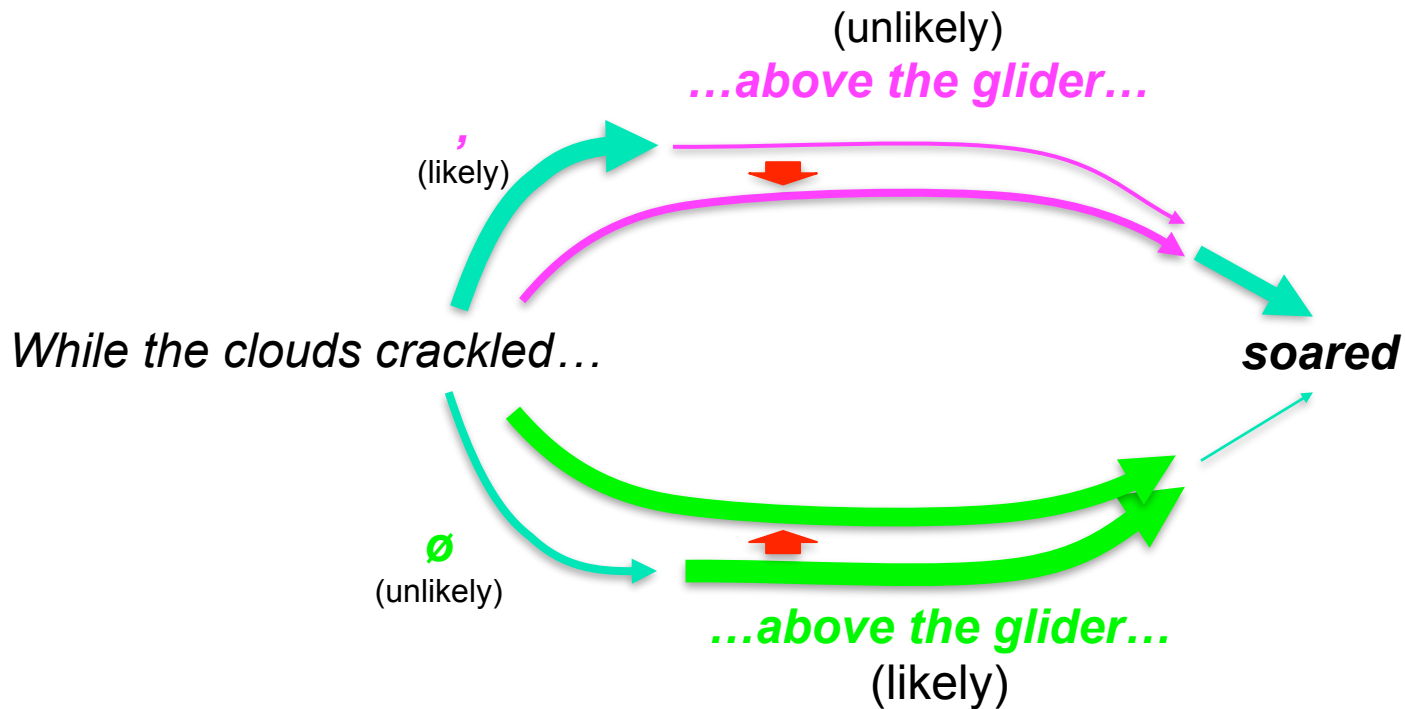
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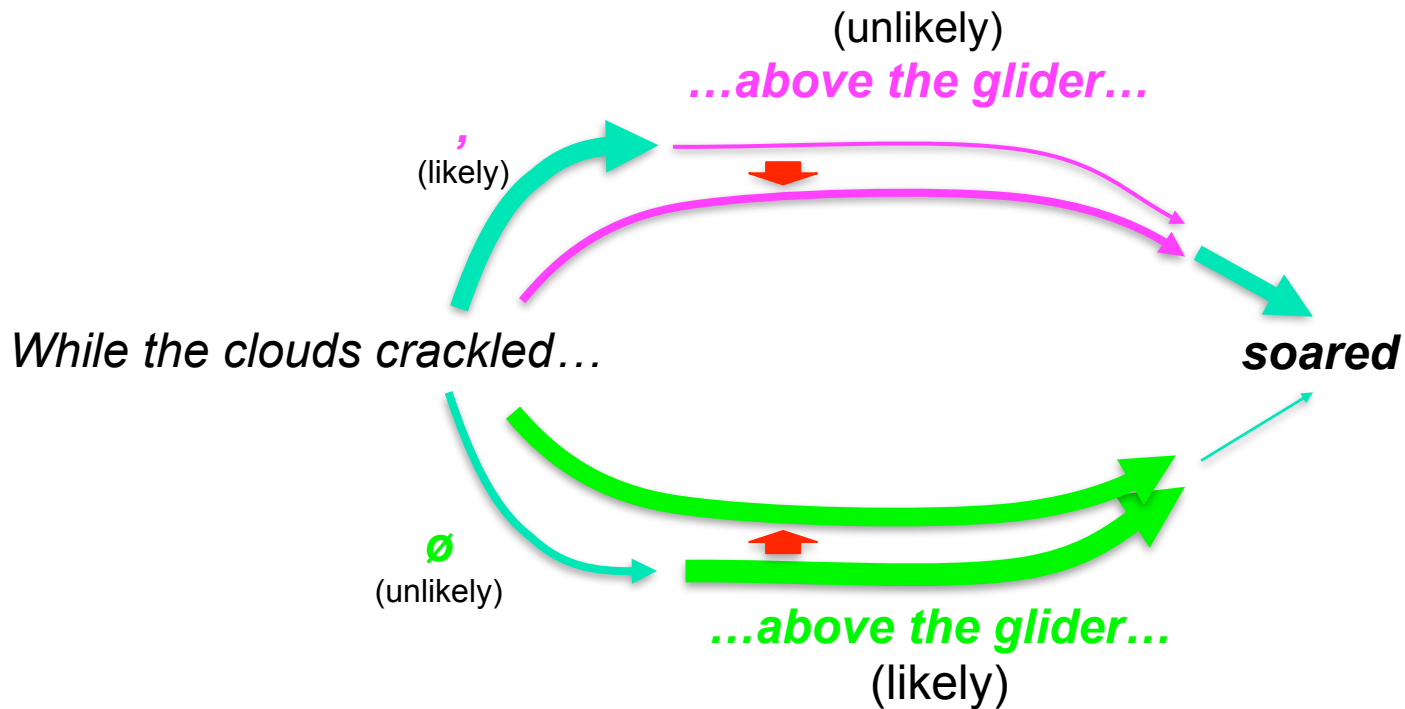
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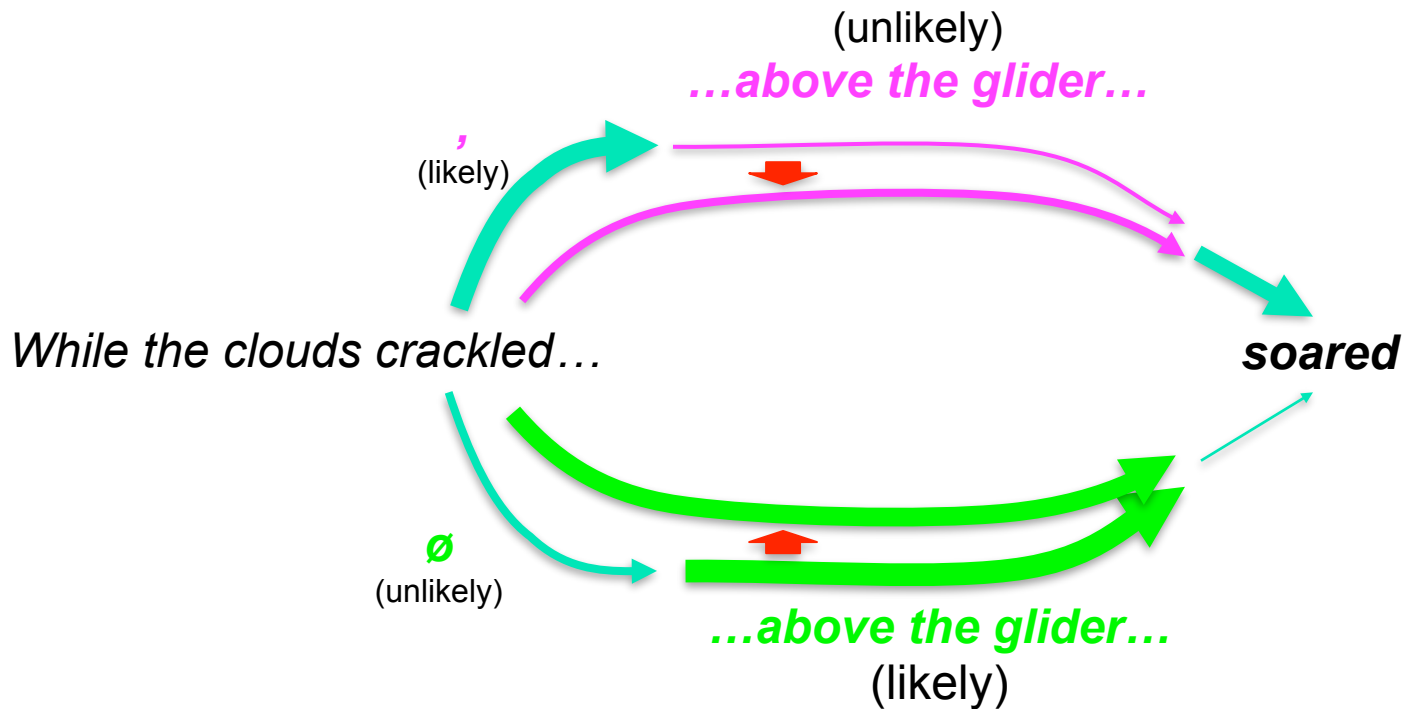


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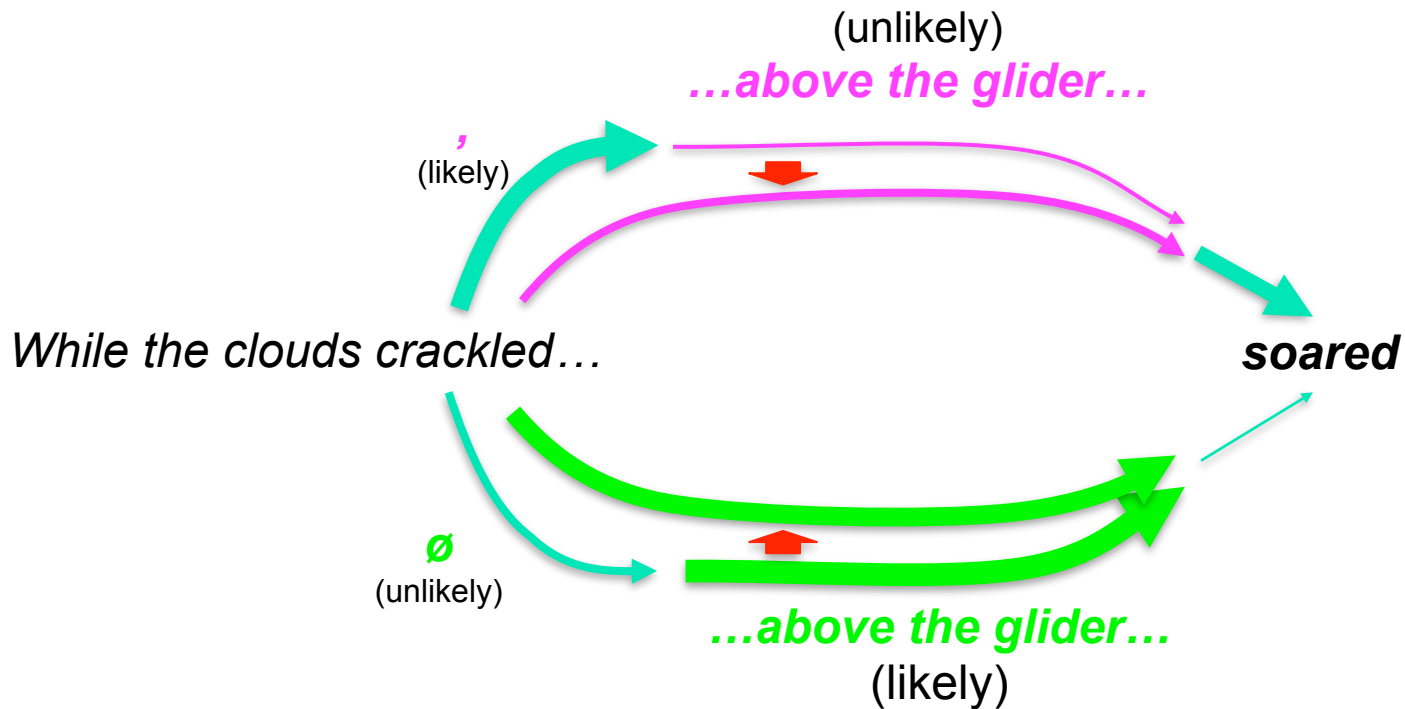
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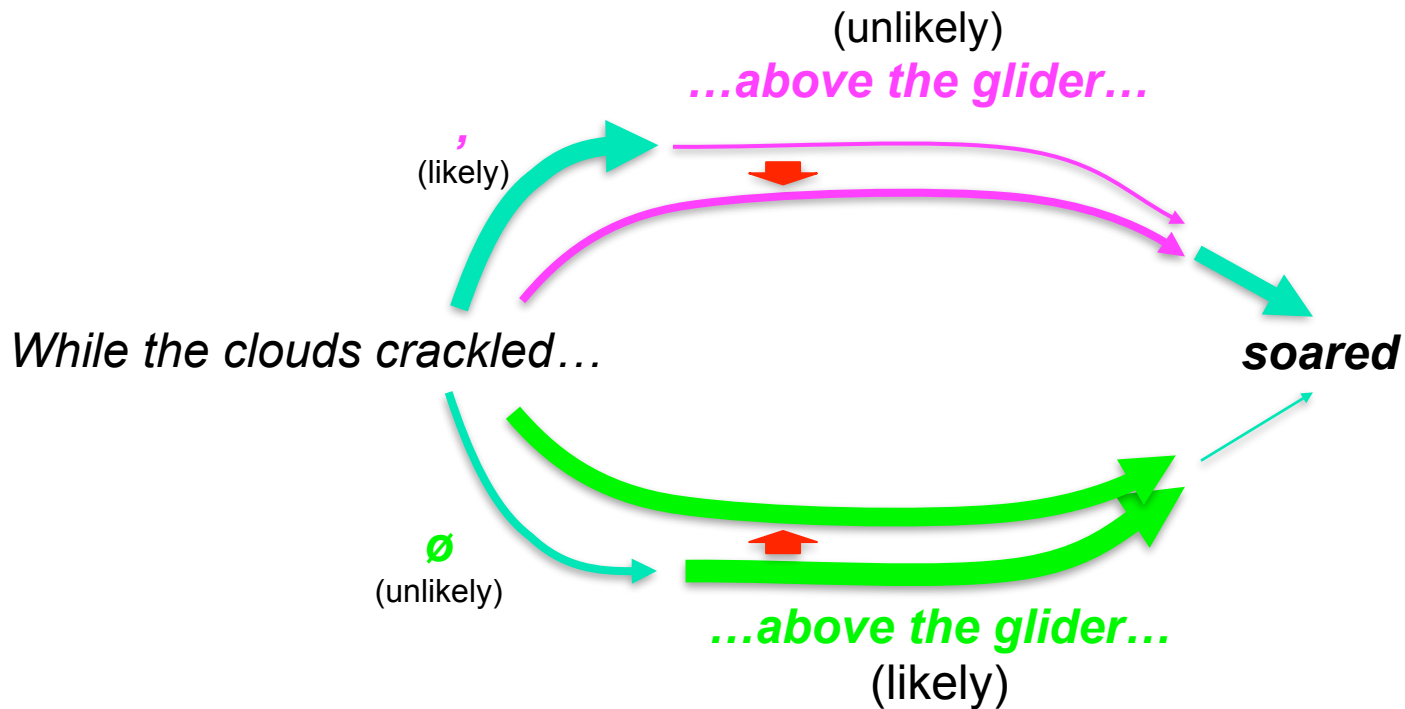
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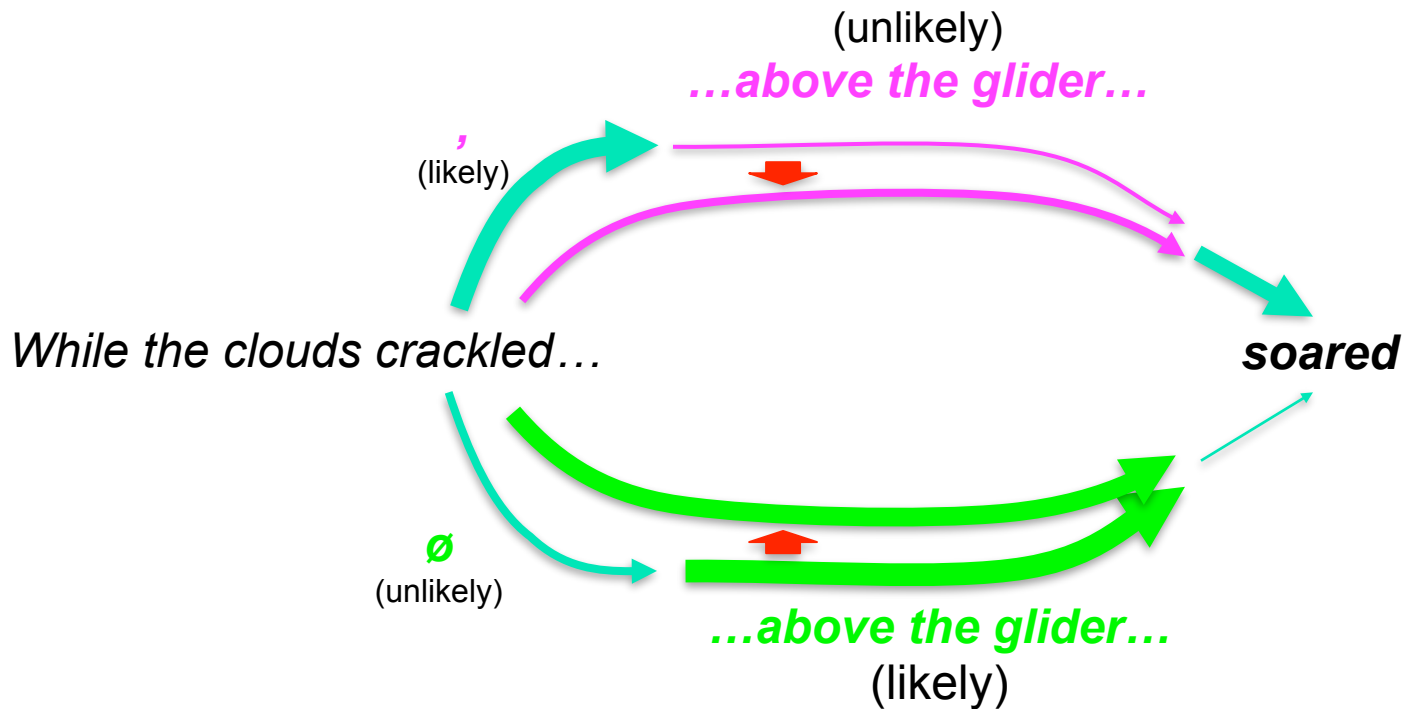
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- Inferences as probabilistic paths through the sentence:
 - Perceptual cost of ignoring the comma
 - Unlikeliness of main-clause continuation after comma
 - Likelihood of postverbal continuation without comma
- These inferences together make *soared* very surprising!

$$P(w_i | \text{Context}) = \sum_{\text{Path}} \underbrace{P(w_i | \text{Path}, \text{Context})}_{\text{green bar}} P(\text{Path} | \text{Context})$$

Prediction 2: hallucinated garden paths

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- Two properties come together to create “hallucinated garden path”
 1. Subordinate clause into which the main-clause inverted phrase would fit well
 2. Main clause with locative inversion

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- Experimental design: cross (1) and (2)

While the clouds crackled, above the glider soared a magnificent eagle.

While the clouds crackled, the glider soared above a magnificent eagle.

While the clouds crackled in the distance, above the glider soared a magnificent eagle.

While the clouds crackled in the distance, the glider soared above a magnificent eagle.

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- The phrase *in the distance* fulfills a similar thematic role as above the glider for crackled

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Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading
- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading
-

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds~~-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds-cracked,~~-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds-cracked,~~ -above-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds-cracked,~~ -above-the-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds-cracked,-above-the-glider-----~~

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~white-the-clouds-cracked,~~ ~~above-the-glider-soared~~-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~while the clouds cracked,~~ ~~above the glider soared~~-----

- Readers aren't allowed to backtrack
- So the comma is visually *gone* by the time the inverted main clause appears

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

~~while the clouds cracked,~~ ~~above the glider~~ soared-----

- Readers aren't allowed to backtrack
- So the comma is visually *gone* by the time the inverted main clause appears
- Simple test of whether beliefs about previous input can be revised

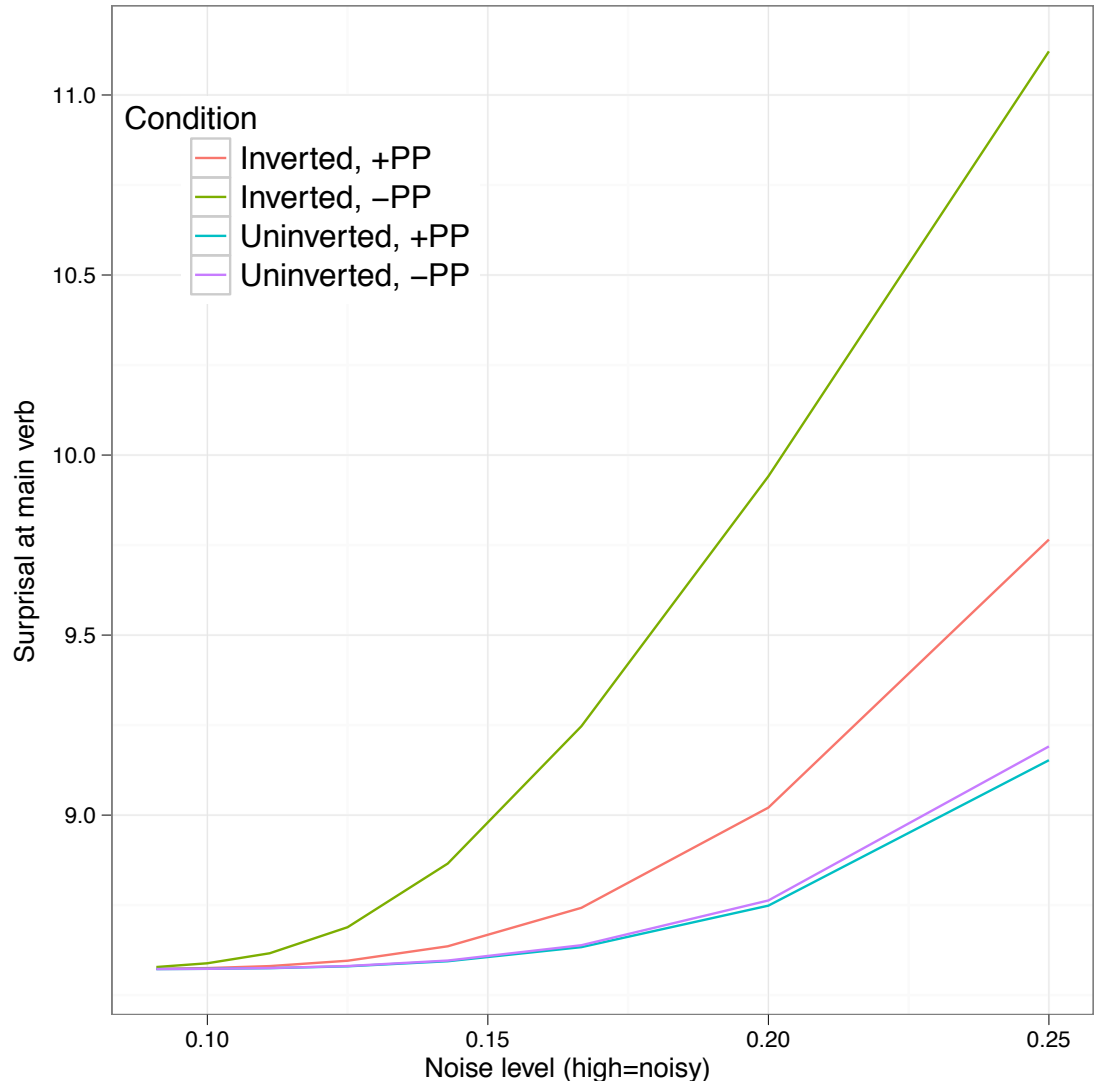
Model predictions

While the clouds
crackled, above the
glider soared a
magnificent eagle.

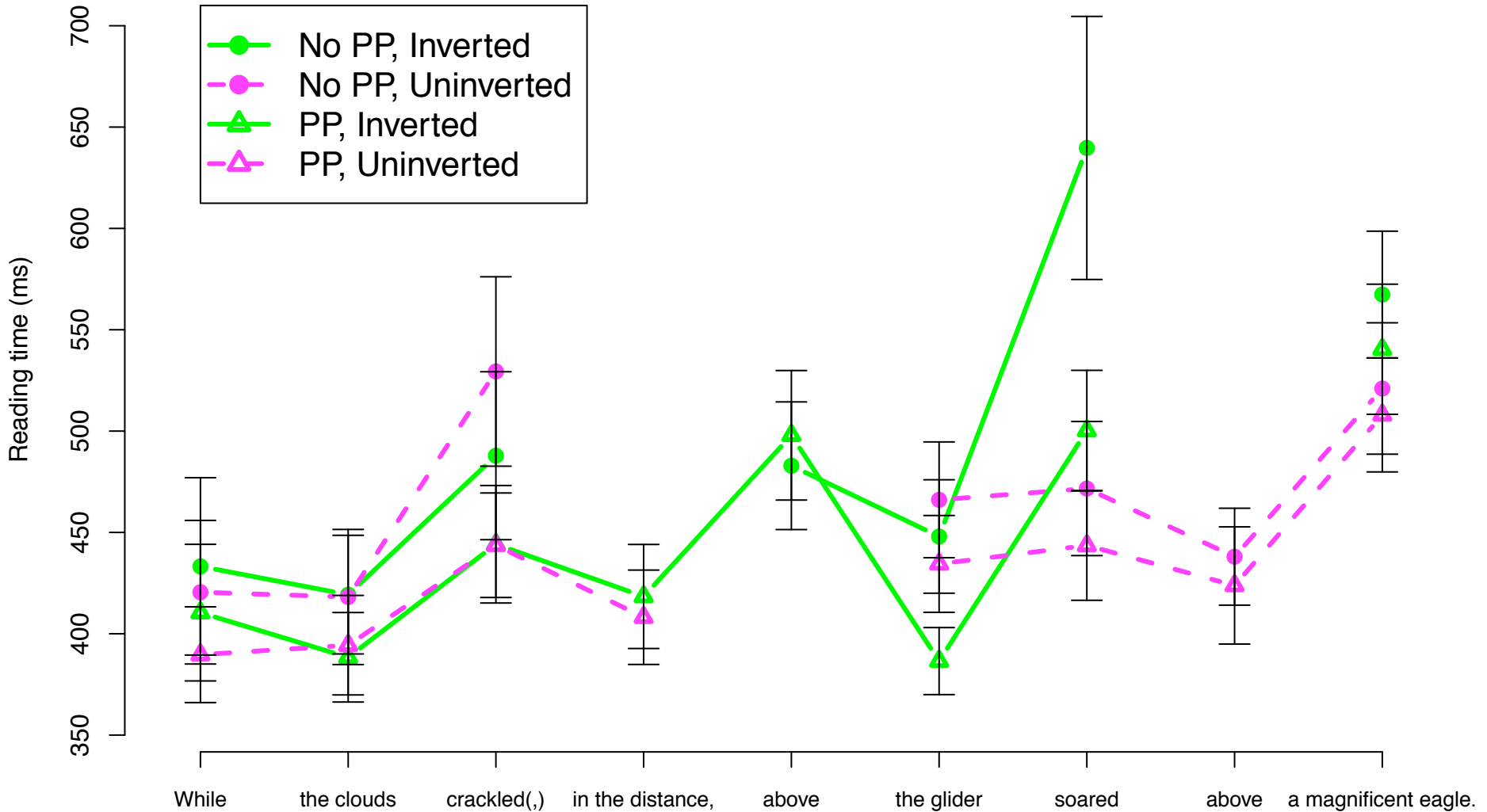
While the clouds crackled
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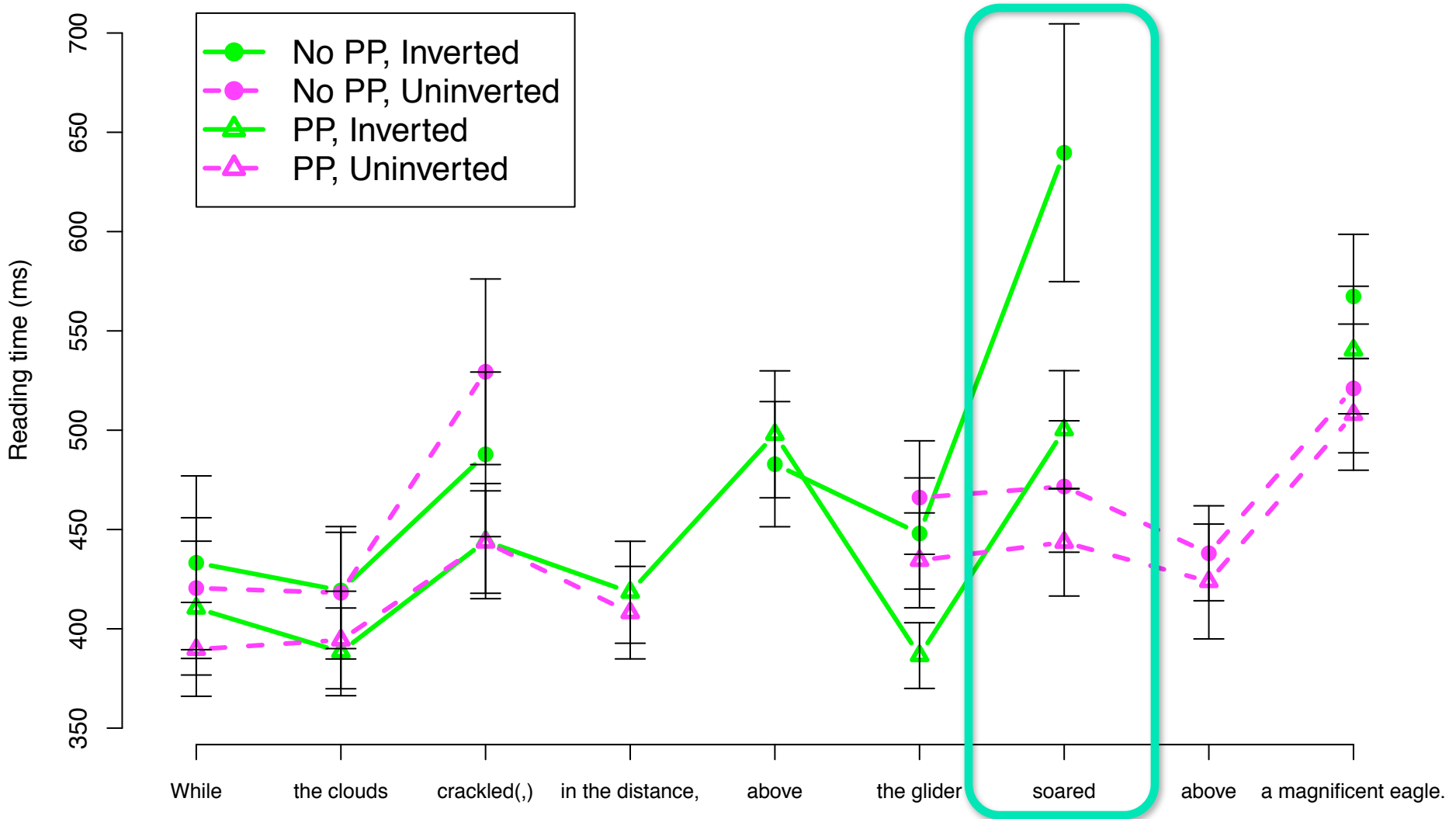
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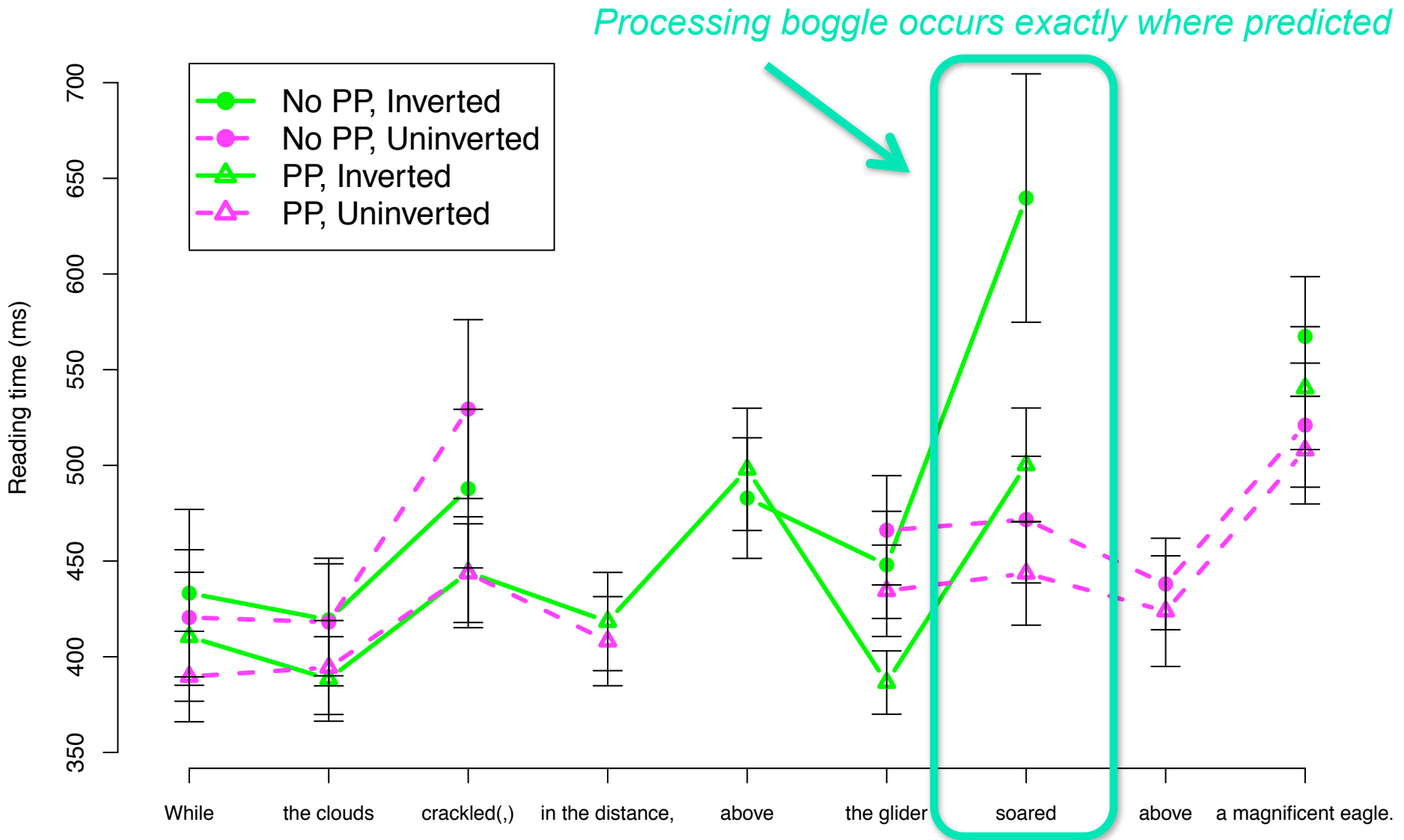
Results: whole sentence reading times



Results: whole sentence reading times



Results: whole sentence reading times



Hallucinated garden-path summary

- The *at/toward* study showed that comprehenders *note the possibility of* alternative strings and *act on it*
- This study showed that comprehenders can actually *devote resources to* grammatical analyses inconsistent with the surface string

Hallucinated garden paths cont'd

- Sure, but punctuation's weird stuff
- What about *real words*?

I know that the desert trains could resupply the camp.

- At least sometimes, bias *against* N N interpretation

Hallucinated garden paths cont'd

- Sure, but punctuation's weird stuff
- What about *real words*?

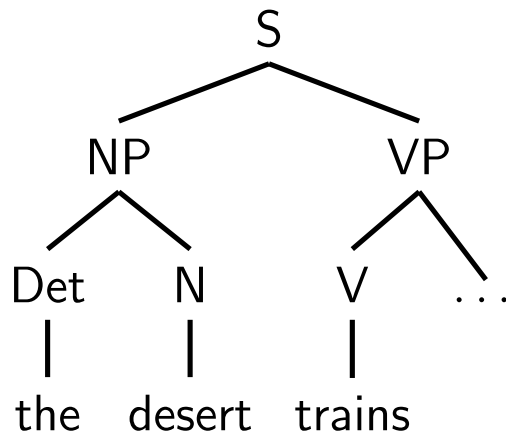
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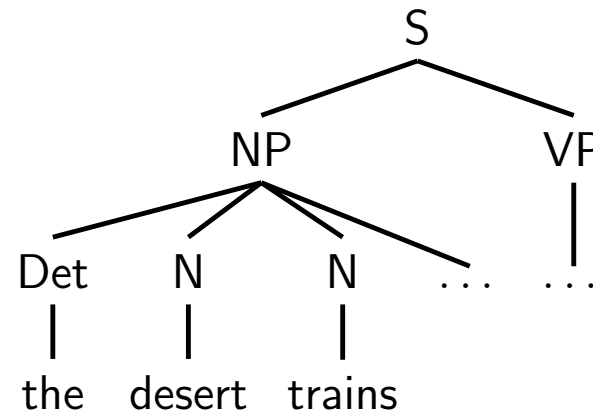
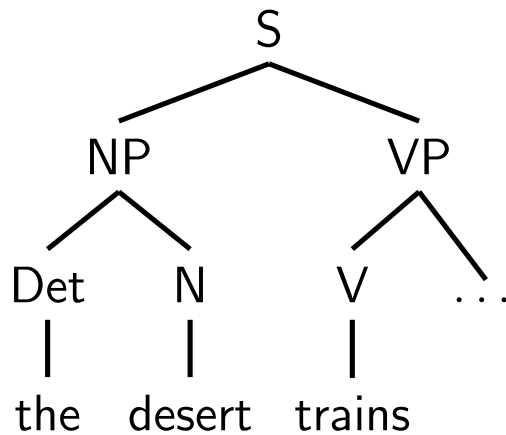


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Hallucinated garden paths cont'd

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- At least sometimes, bias *against* N N interpretation

Hallucinated GPs with words

Could be “intern chauffeured”

Could NOT be “inexperienced chauffeured”

Hallucinated GPs with words

- We use a contextual bias against NN and toward NV to test for GP hallucinations involving wordform change

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[NN, “dense” neighborhood]

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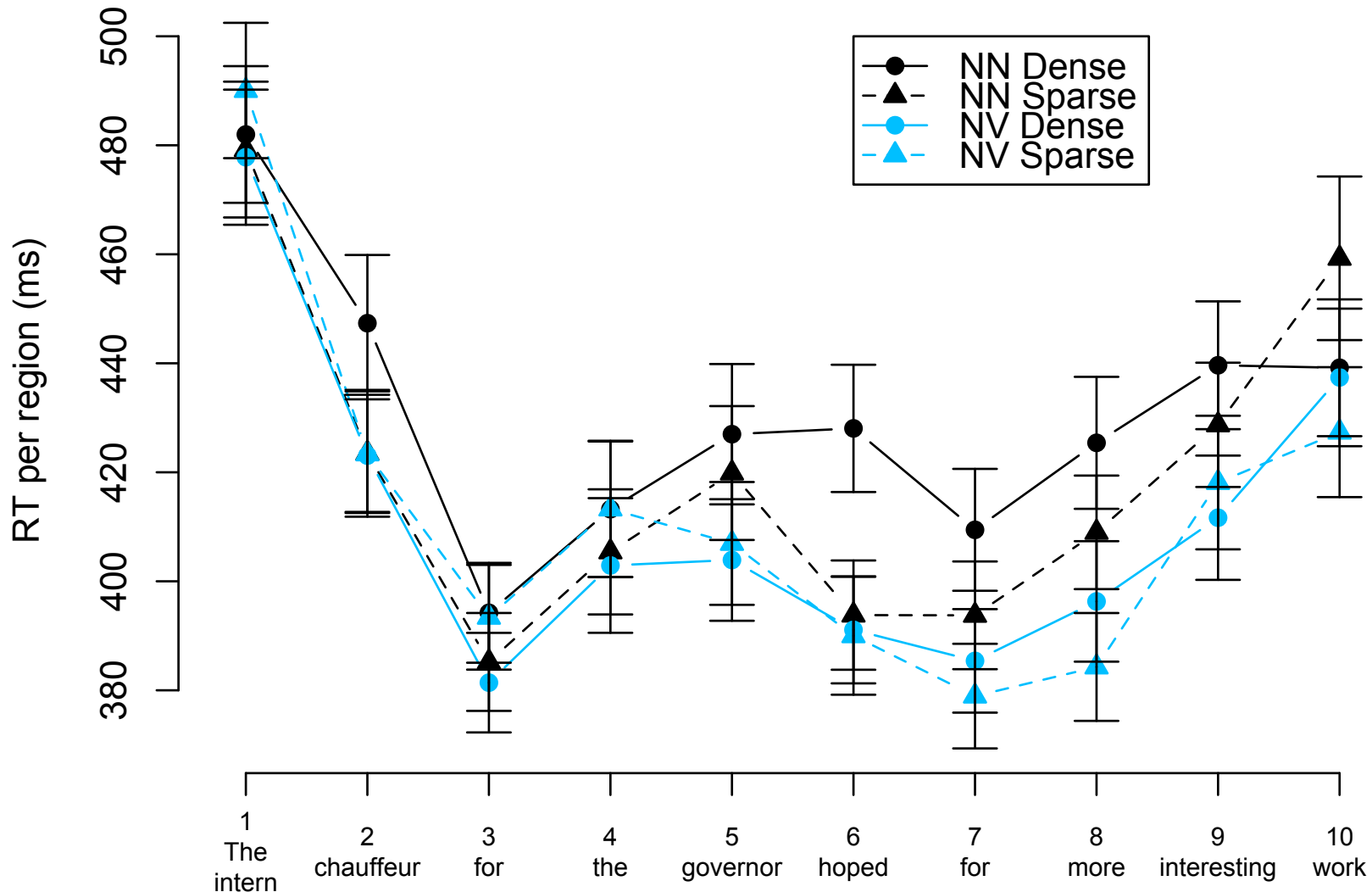
Could NOT be “inexperienced chauffeured”

The inexperienced chauffeur for the governor hoped for more interesting work.
[NN, “sparse” neighborhood]

Some interns chauffeured for the governor but hoped for more interesting work.
[NV, “sparse” neighborhood]

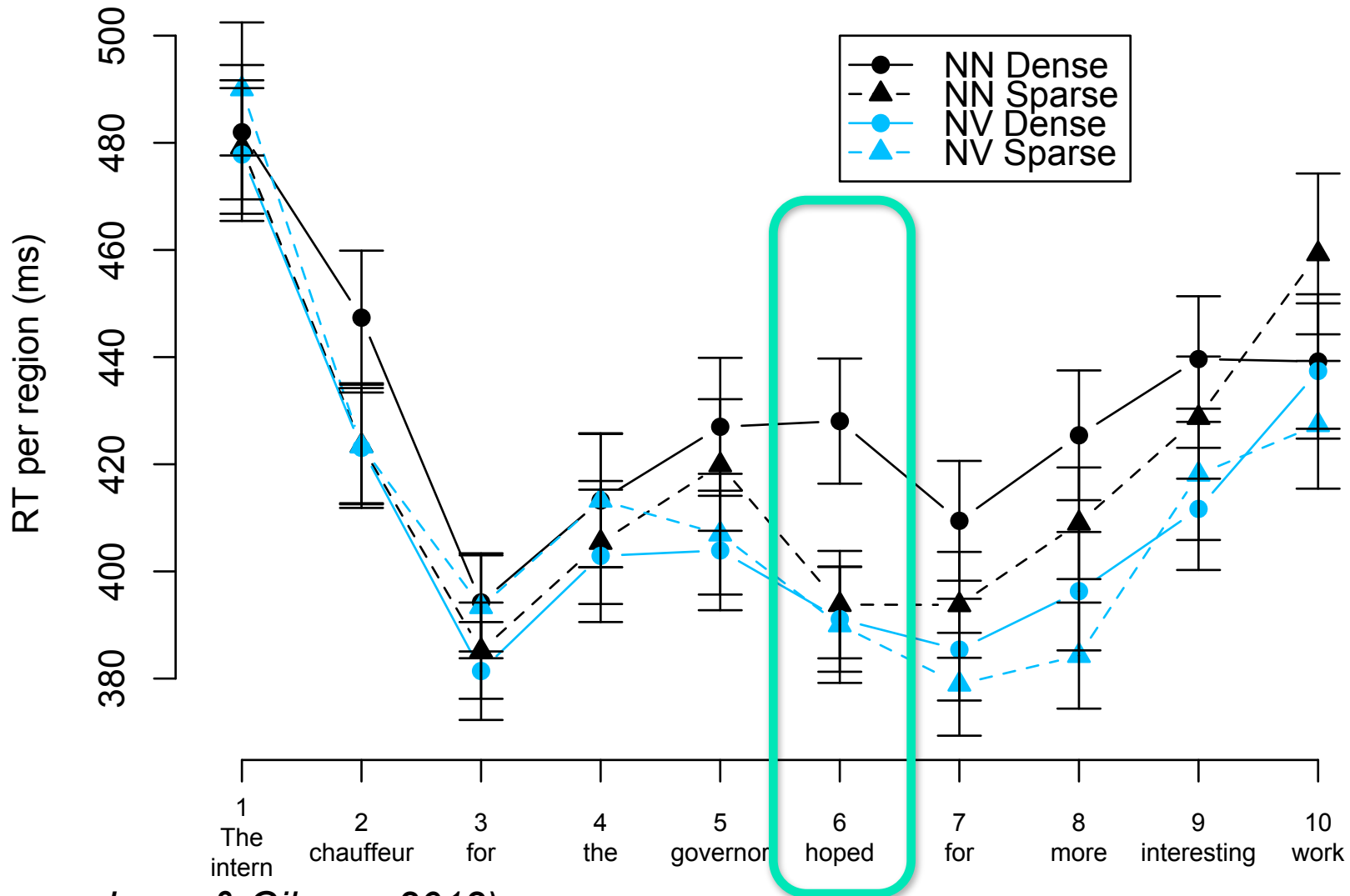
Results

- RT spike at disambiguating region for NN Dense

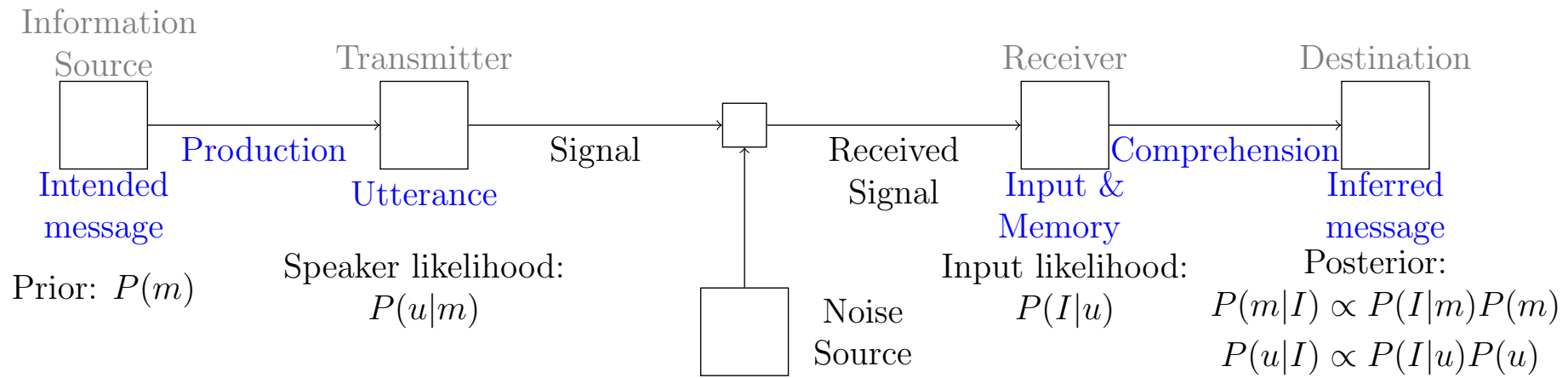


Results

- RT spike at disambiguating region for NN Dense



Noisy-channel theory of language processing



Simple question-answering

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

The ball kicked the girl.

Did the girl kick something?

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

The ball kicked the girl.

Did the girl kick something?

No

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No

The businessman benefited from the tax law.

Did the tax law benefit from anything?

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The cook baked a cake Lucy.

Was something baked for Lucy?

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Was something baked for Lucy?

No (Yes?)

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The woman lost the diamond.

Did the woman lose something?

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Did the girl kick something?

No

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No

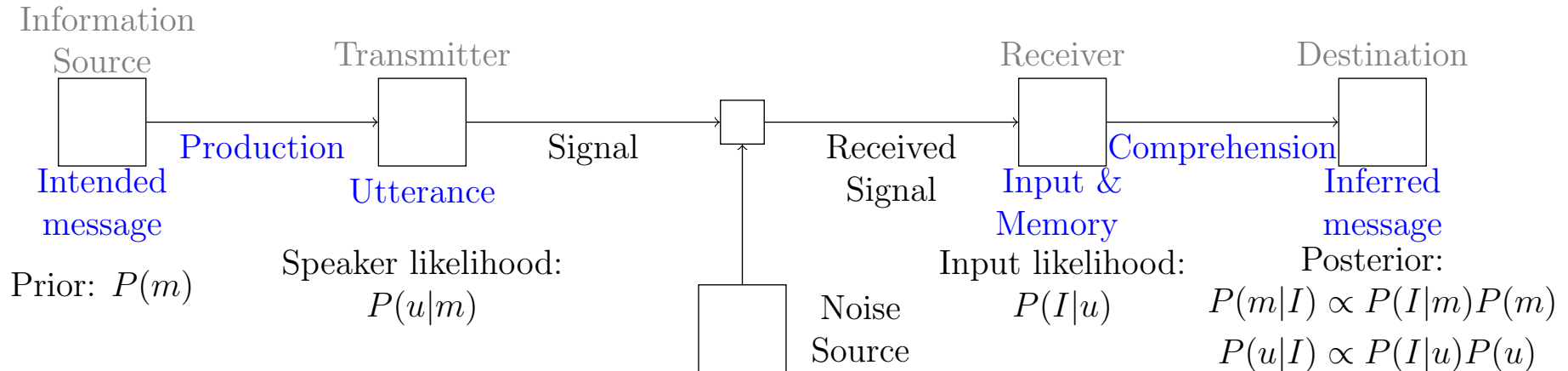
(Yes?)

Over 2/3 of answers!

Noisy-channel semantic interpretation?

The cook baked a cake Lucy.

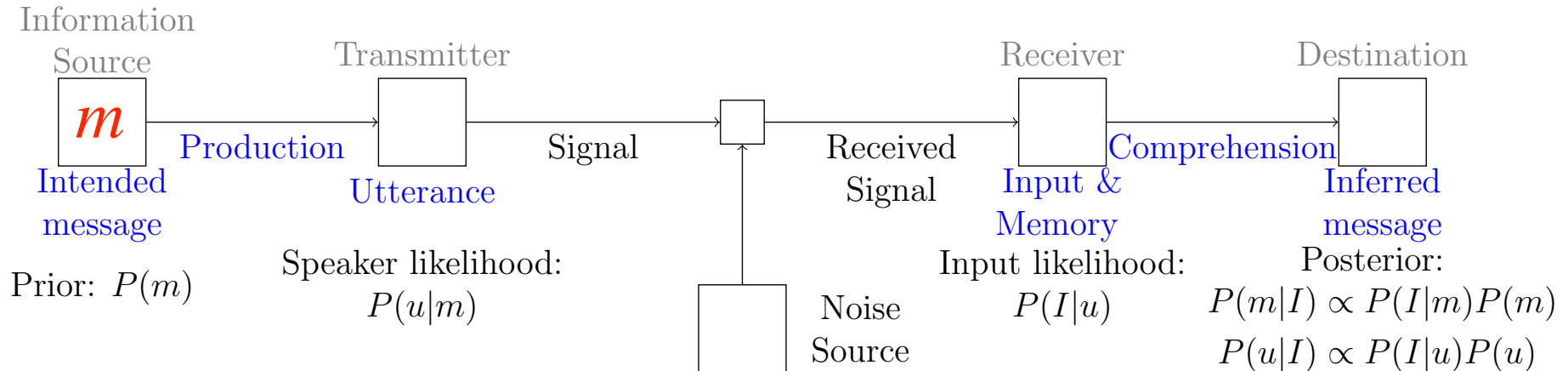
Was something baked for Lucy?



Noisy-channel semantic interpretation?

The cook baked a cake Lucy.

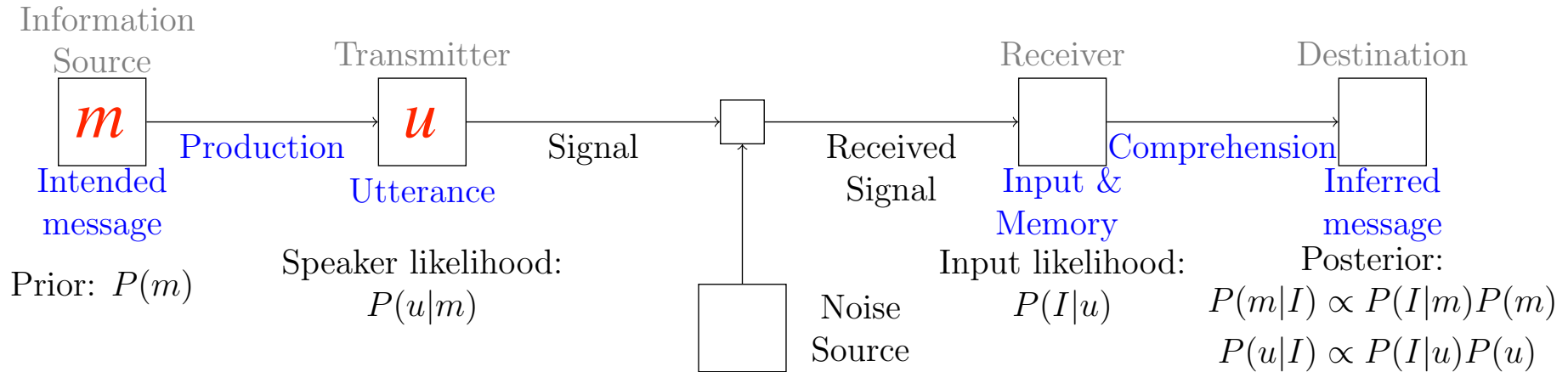
Was something baked for Lucy?



Noisy-channel semantic interpretation?

The cook baked a cake Lucy.

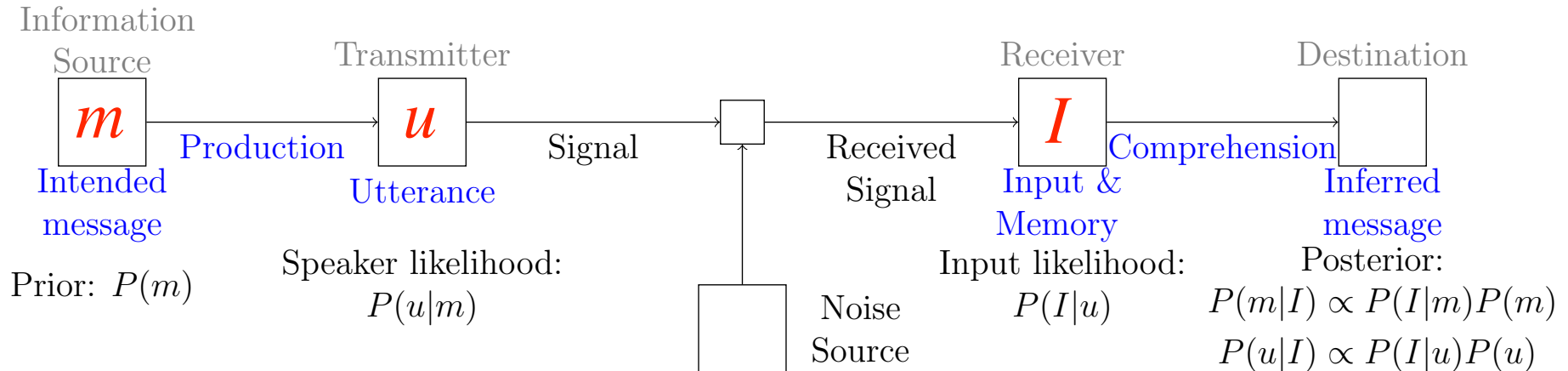
Was something baked for Lucy?



Noisy-channel semantic interpretation?

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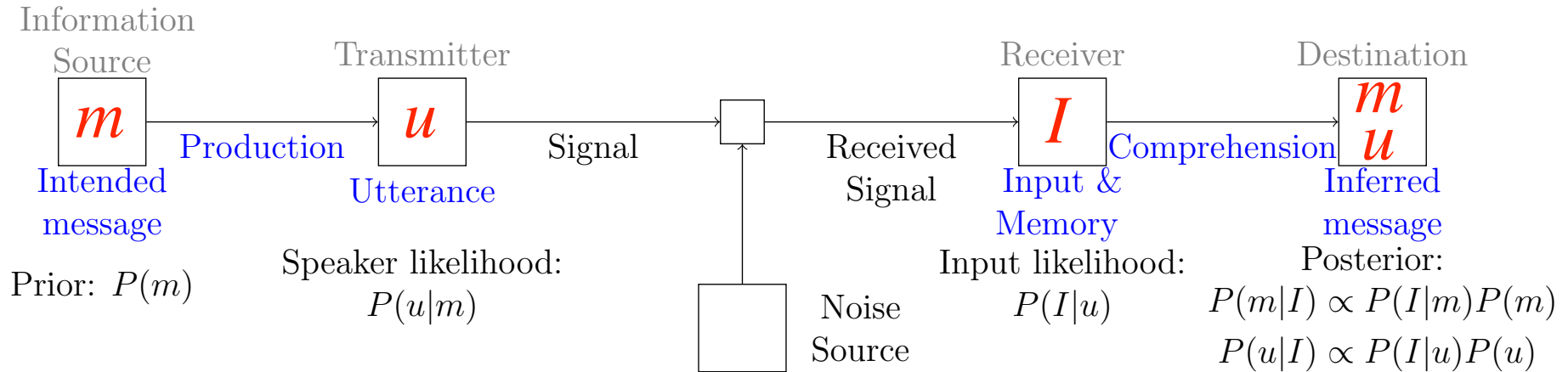
Was something baked for Lucy?



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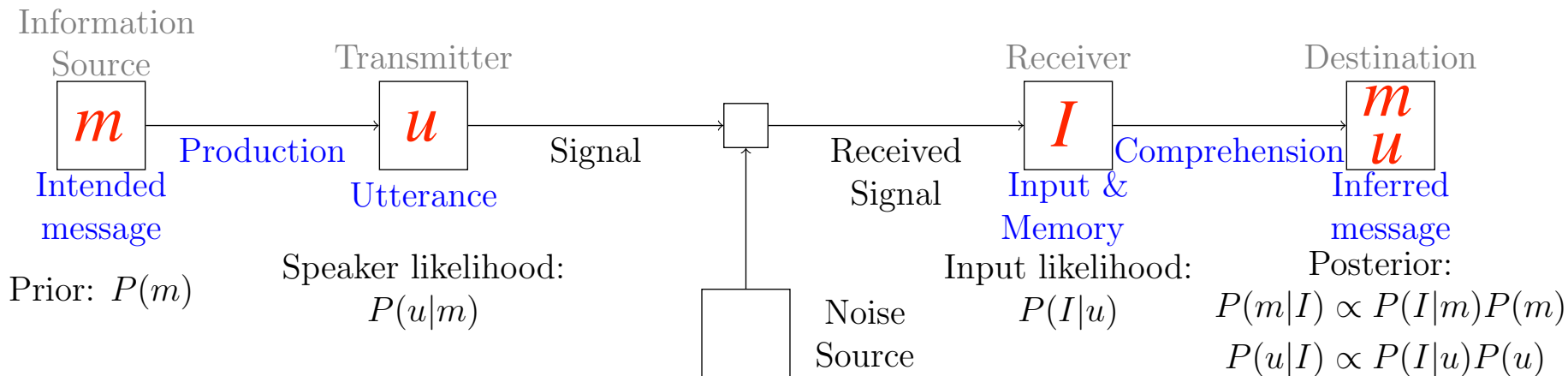
Was something baked for Lucy?



Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

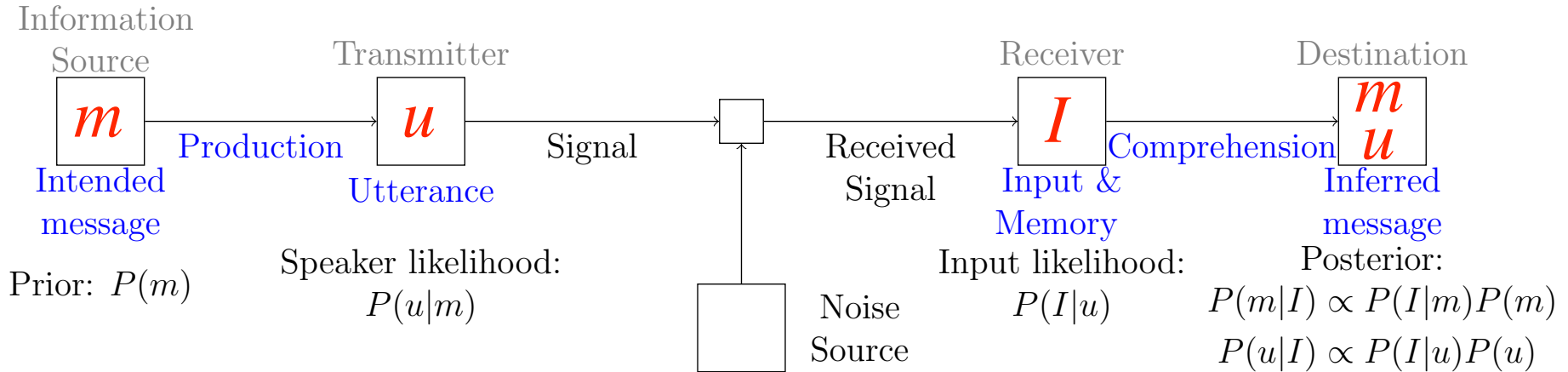
Was something baked for Lucy?



Noisy-channel semantic interpretation?

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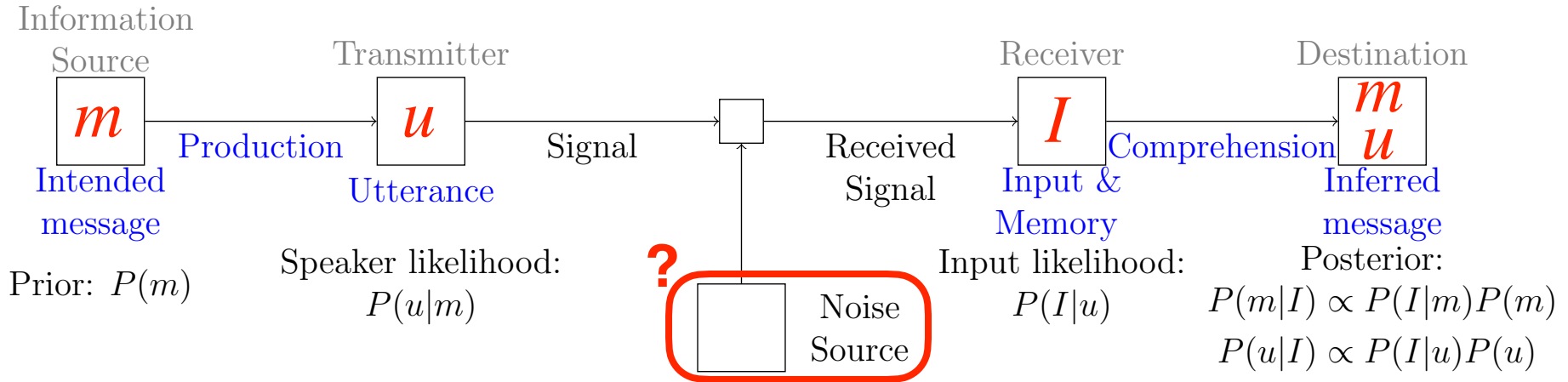
m? Was something baked for Lucy?



Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

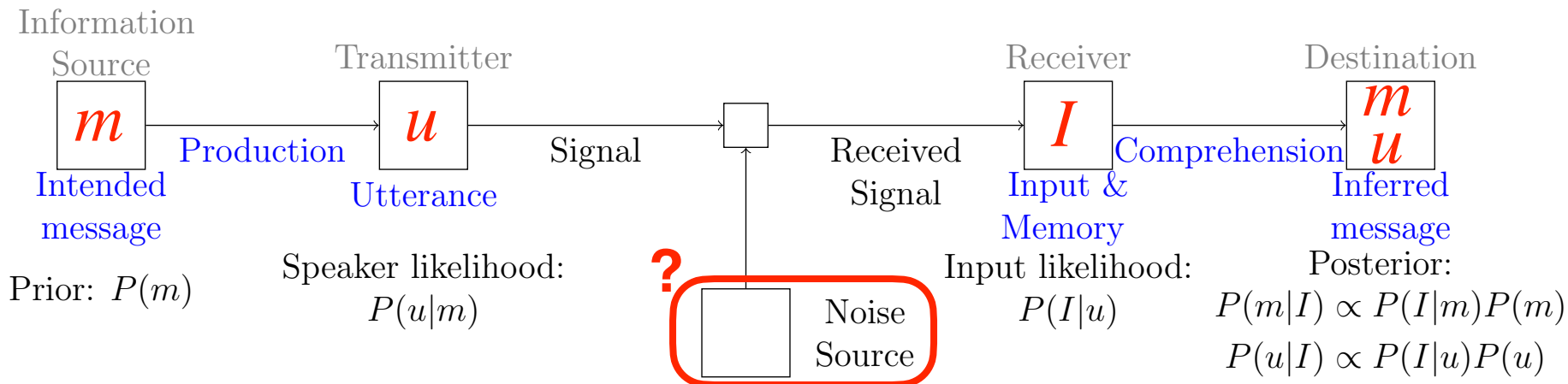
m? Was something baked for Lucy?



Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

m? Was something baked for Lucy?

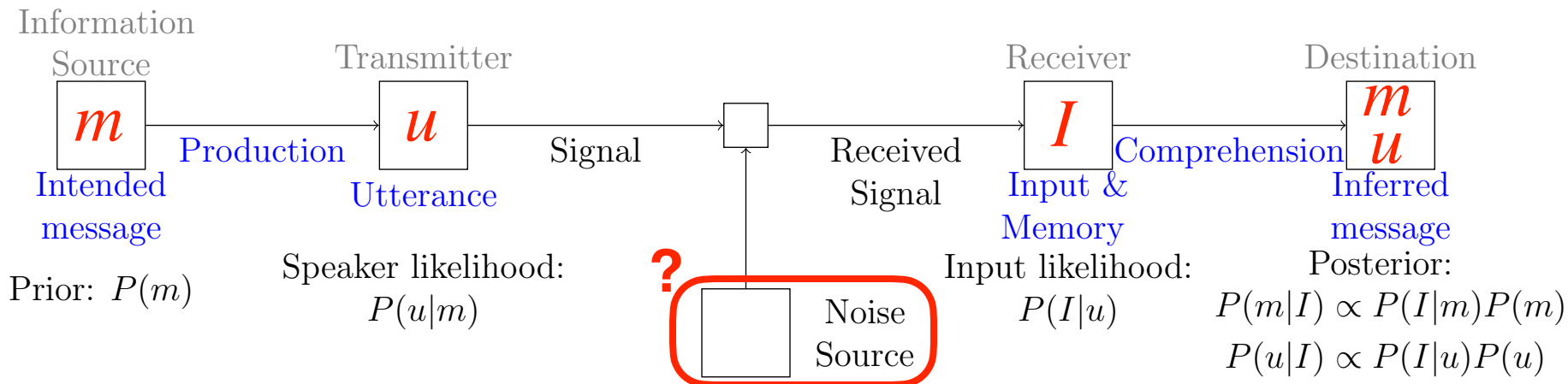


In two semantically plausible "neighbor" sentences, the answer is "yes":

Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

m? Was something baked for Lucy?



In two semantically plausible "neighbor" sentences, the answer is "yes":

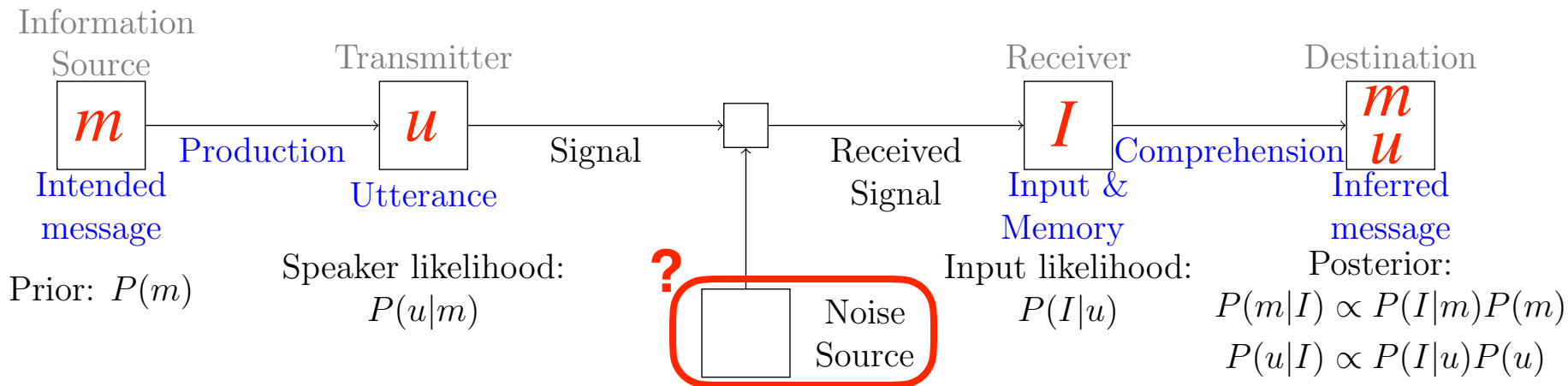
The cook baked a cake Lucy.

for

Noisy-channel semantic interpretation?

***I* ← The cook baked a cake Lucy.**

m? Was something baked for Lucy?



In two semantically plausible "neighbor" sentences, the answer is "yes":

The cook baked a cake Lucy.

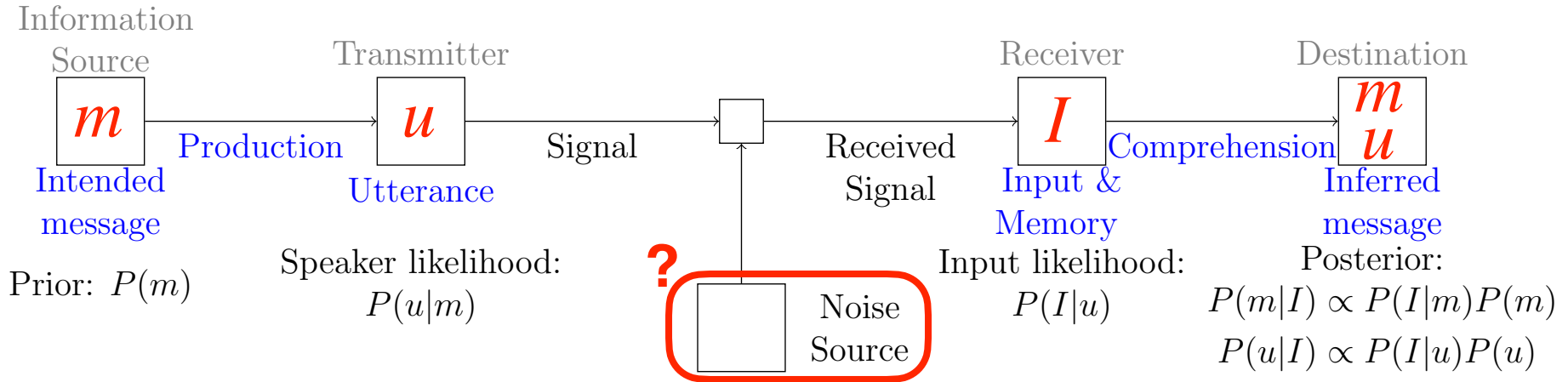
Hypothesized noise operation: **deletion**

for

Noisy-channel semantic interpretation?

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for

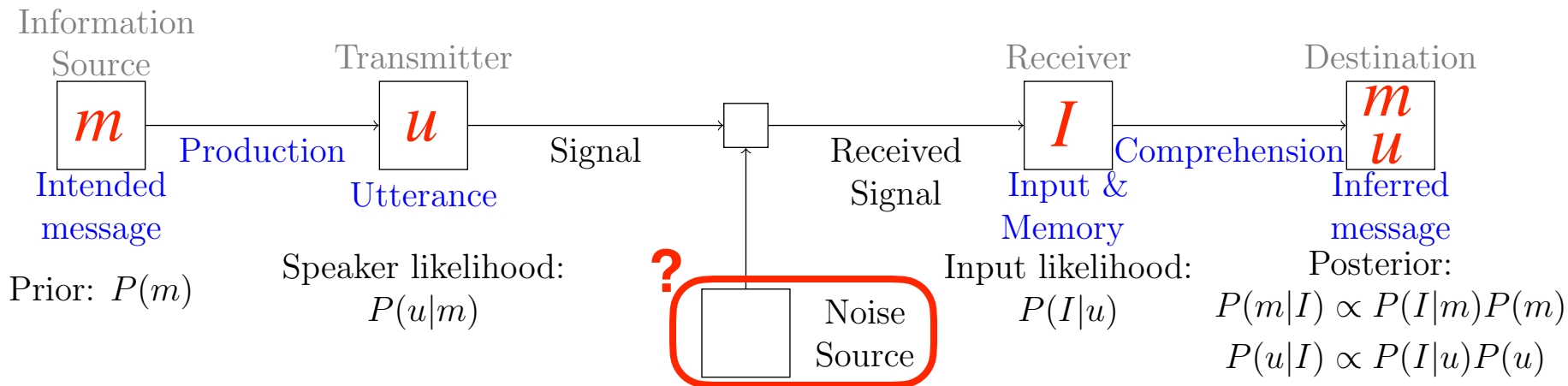
The cook baked a cake Lucy.

Lucy a cake

Noisy-channel semantic interpretation?

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m? Was something baked for Lucy?



In two semantically plausible "neighbor" sentences, the answer is "yes":

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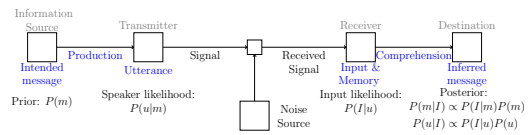
Hypothesized noise operation: **deletion**

for

The cook baked a cake Lucy.

Hypothesized noise operation: **exchange** *Lucy a cake*

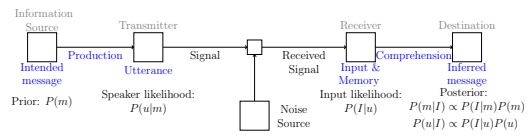
Predictions for implausible sentences



$$P(m | I) \propto \underbrace{P(I | m)}_{\text{Plausibility}} \underbrace{P(m)}_{\text{Noise operation}}$$

Noise operation Plausibility

Predictions for implausible sentences



$$P(m | I) \propto \underline{P(I | m)} \underline{P(m)}$$

Noise operation Plausibility

Non-literal interpretation?

Double Object/Benefactive-*for* alternation

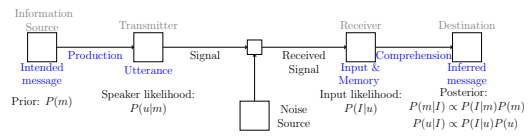
Deletion/insertion *Exchange*

Implausible **The cook baked a cake Lucy.**
The cook baked Lucy for a cake.

Yes Yes

Yes Yes

Predictions for implausible sentences



$$P(m | I) \propto \underline{P(I | m)} \underline{P(m)}$$

Noise operation Plausibility

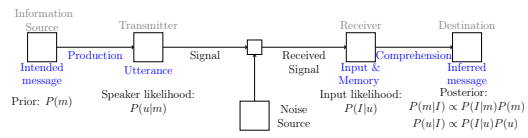
Non-literal interpretation?

Double Object/Benefactive-*for* alternation

Deletion/insertion *Exchange*

Implausible	[The cook baked a cake Lucy.	Yes	Yes
		The cook baked Lucy for a cake.	Yes	Yes
Plausible	[The cook baked Lucy a cake.	No	No
		The cook baked a cake for Lucy.	No	No

Predictions for implausible sentences



$$P(m | I) \propto \underline{P(I | m)} \underline{P(m)}$$

Noise operation Plausibility

Non-literal interpretation?

Double Object/Benefactive-*for* alternation

Deletion/insertion *Exchange*

Implausible

The cook baked a cake Lucy.

Yes Yes

The cook baked Lucy for a cake.

Yes Yes

Plausible

The cook baked Lucy a cake.

No No

The cook baked a cake for Lucy.

No No

Active/Passive alternation

Implausible

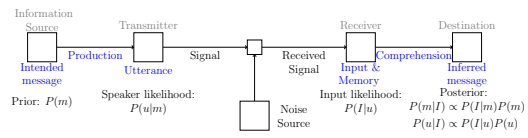
The ball kicked the girl.

No Yes

The girl was kicked by the ball.

No Yes

Predictions for implausible sentences



$$P(m | I) \propto \underline{P(I | m)} \underline{P(m)}$$

Noise operation Plausibility

Non-literal interpretation?

Double Object/Benefactive-*for* alternation

Deletion/insertion *Exchange*

Implausible	[The cook baked a cake Lucy.	Yes	Yes
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Plausible	[The cook baked Lucy a cake.	No	No
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Active/Passive alternation

Implausible	[The ball kicked the girl.	No	Yes
		The girl was kicked by the ball.	No	Yes
Plausible	[The girl kicked the ball.	No	Yes
		The ball was kicked by the girl.	No	Yes

Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

Insertion/Deletion

Exchange

Insertion/Deletion

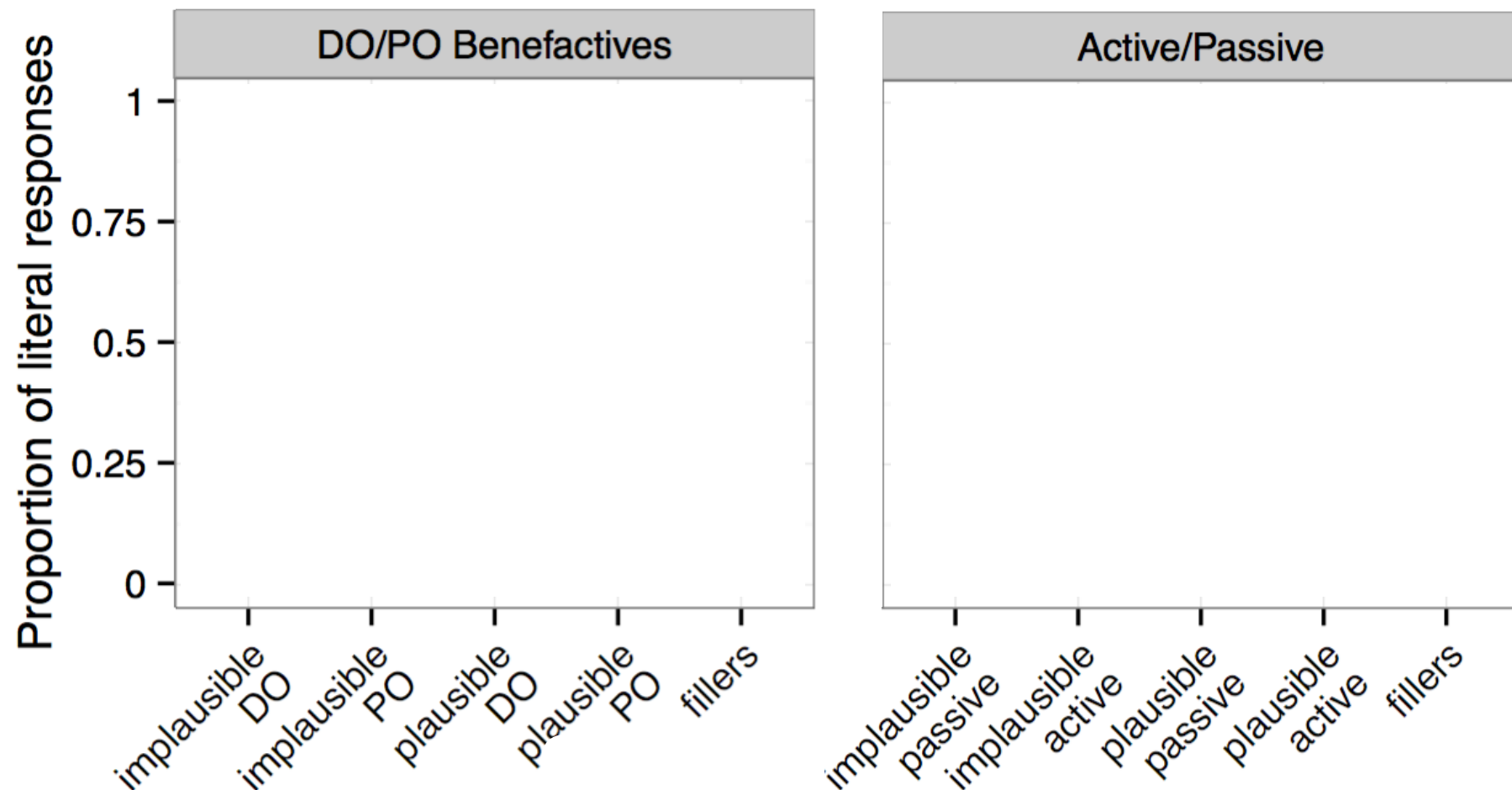
Exchange

Yes

Yes

No

Yes



Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

Insertion/Deletion

Exchange

Insertion/Deletion

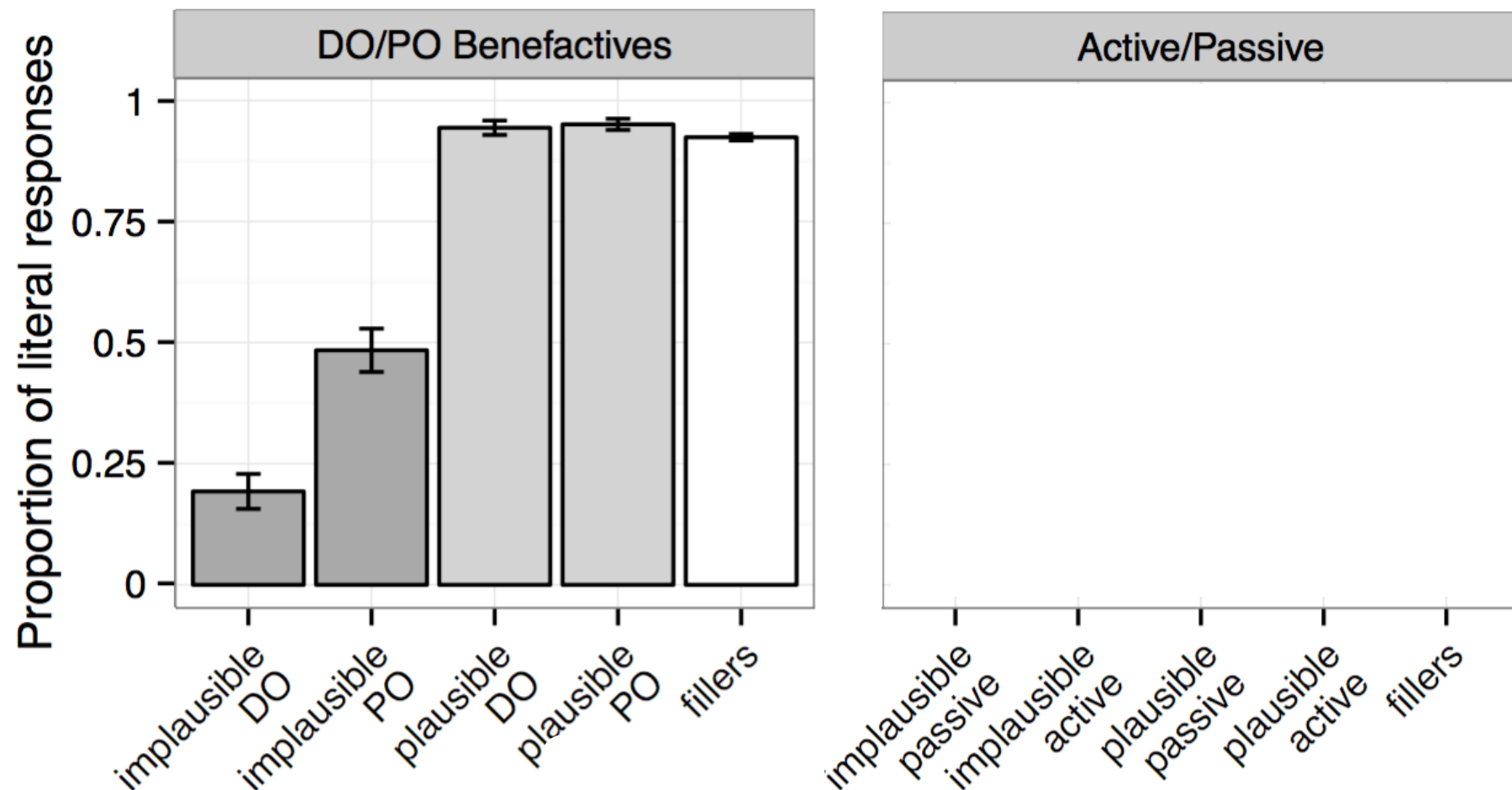
Exchange

Yes

Yes

No

Yes



Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

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Exchange

Insertion/Deletion

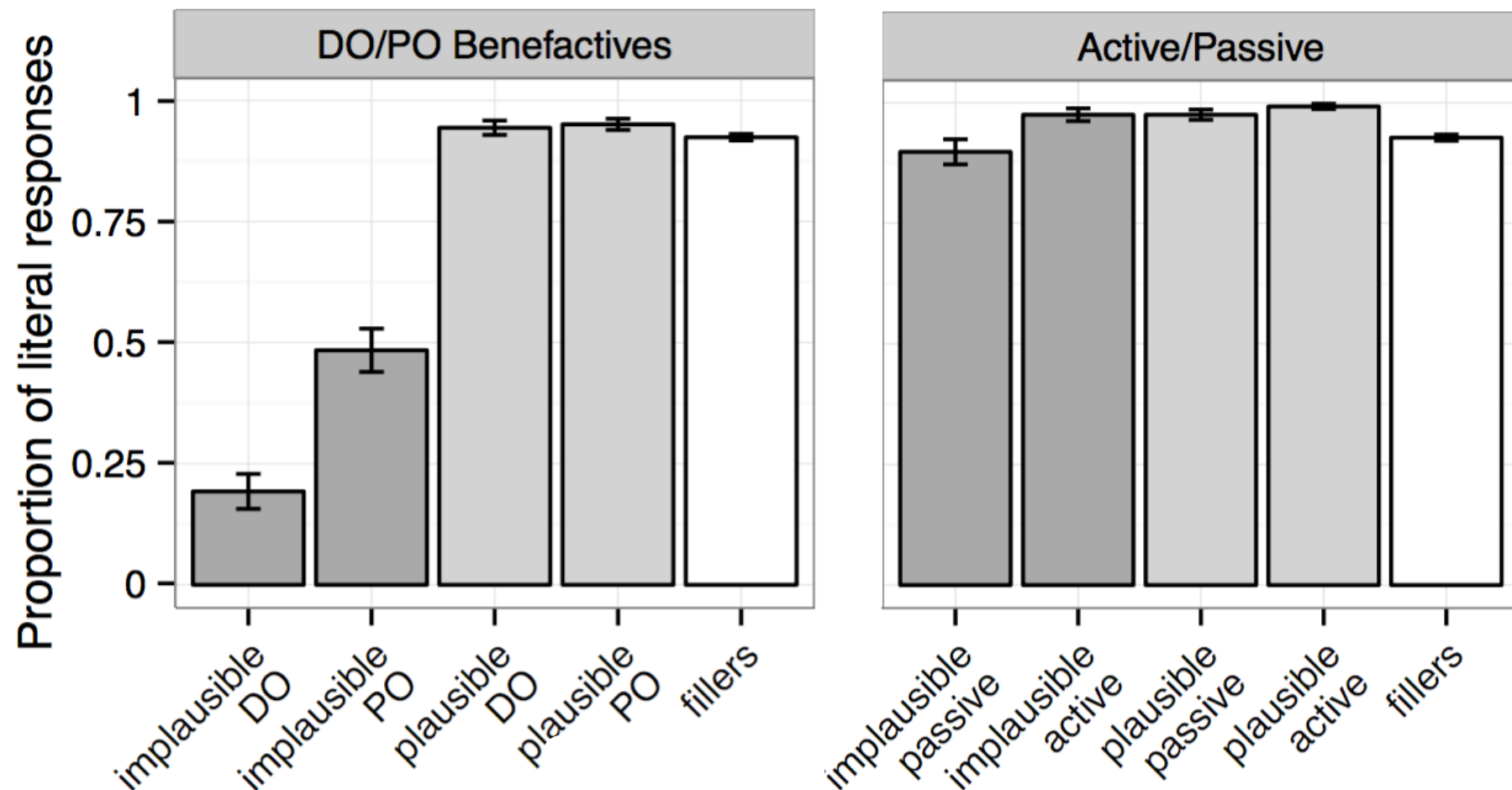
Exchange

Yes

Yes

No

Yes



Five alternations in an insertion/deletion model

English constructions	Change	Implausible version
1. Active/passive	Two insertions Two deletions	c. The girl <u>was</u> kicked <u>by</u> the ball. (passive) d. The ball kicked the girl. (active)
2. Subject-locative/ object-locative	One deletion, one insertion One insertion, one deletion	c. The table jumped <u>onto</u> a cat. (object-locative) d. <u>Onto</u> the cat jumped a table. (subject-locative)
3. Transitive/intransitive	One insertion One deletion	c. The tax law benefited <u>from</u> the businessman. (intransitive) d. The businessman benefited the tax law. (transitive)
4. DO/PO goal	One insertion One deletion	c. The mother gave the daughter <u>to</u> the candle. (PO-goal) d. The mother gave the candle the daughter. (DO-goal)
5. DO/PO benefactive	One insertion One deletion	c. The cook baked Lucy <u>for</u> a cake. (PO-benef) d. The cook baked a cake Lucy. (DO-benef)

c=inferred insertion **d=inferred deletion**

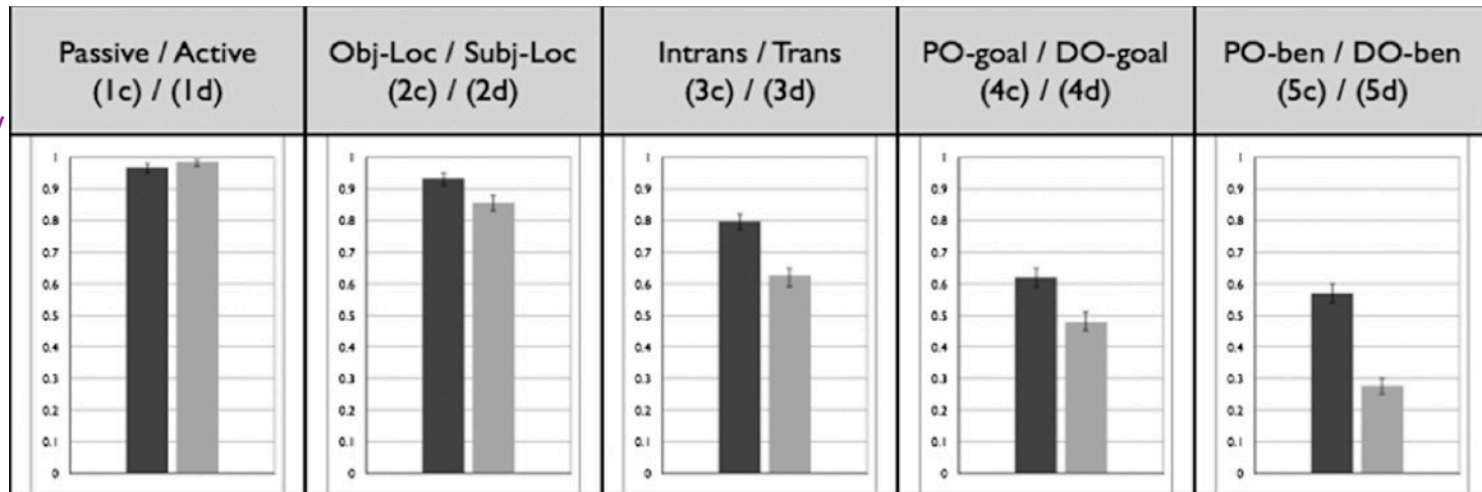
Five alternations in an insertion/deletion model

$$P(m|I) \propto \frac{P(I|m)P(m)}{\text{Noise operation} \quad \text{Plausibility}}$$

Noise operation Plausibility

Base experiment

20 experimental items,
60 plausible &
grammatically normal
fillers → 10/80
implausible trials



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Noise operation \nearrow
Plausibility \uparrow

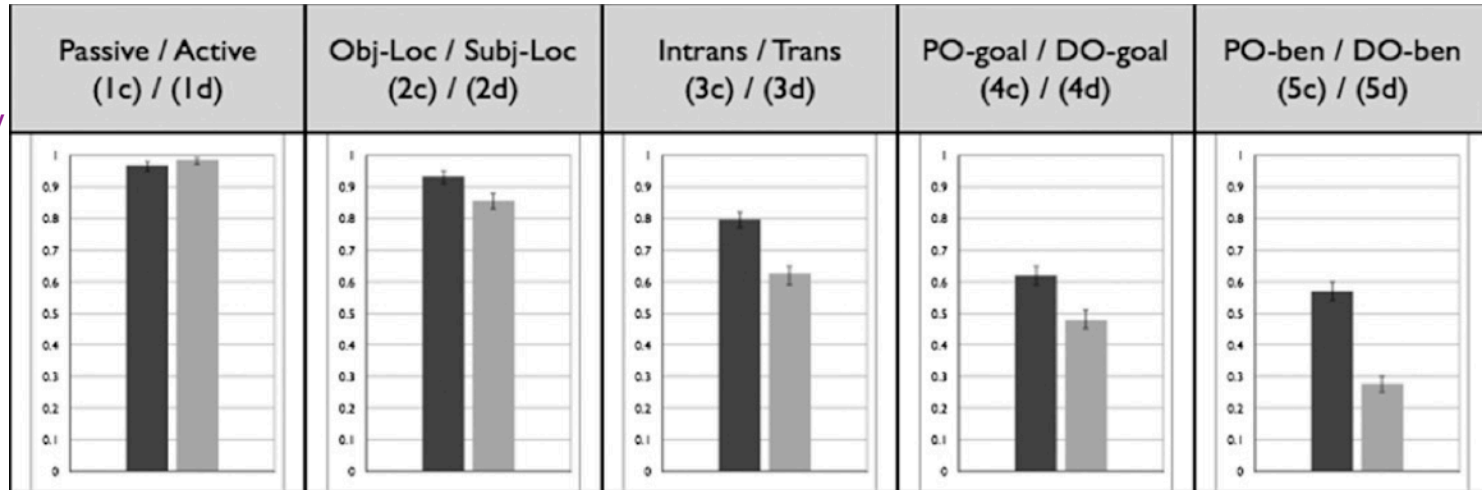
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Fillers with syntactic errors

"A legislator lied to the
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"A bystander was the
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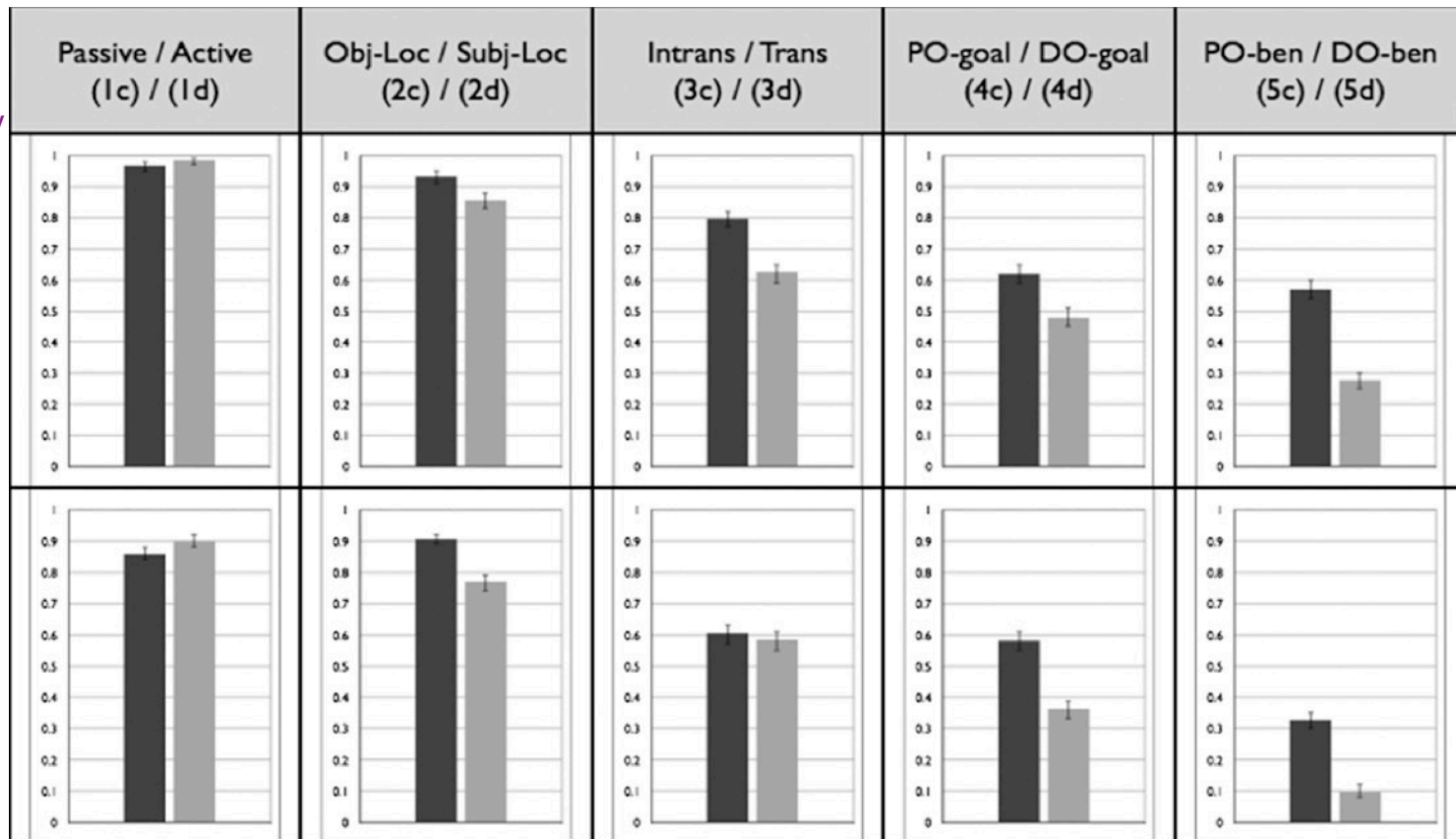
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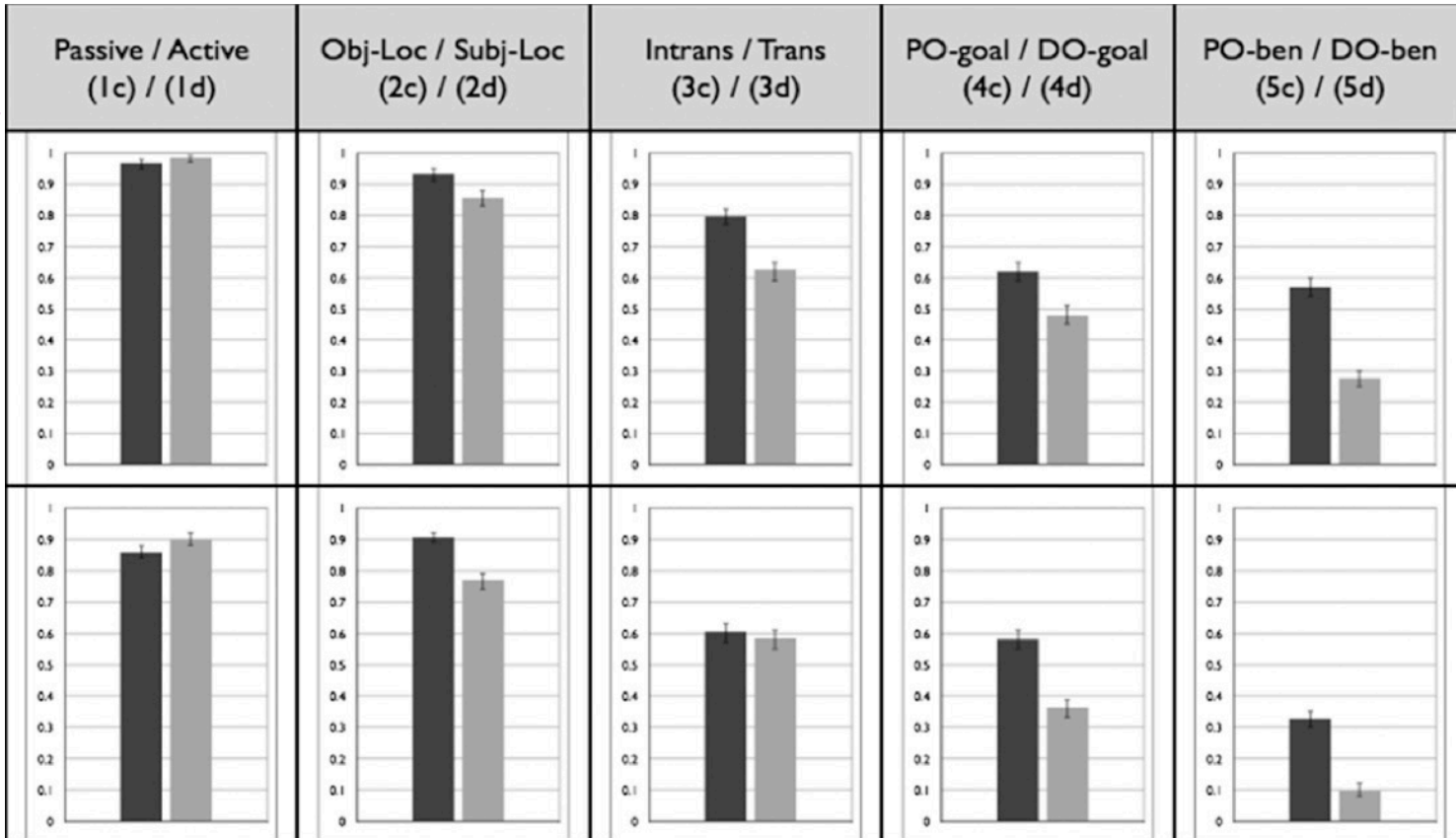
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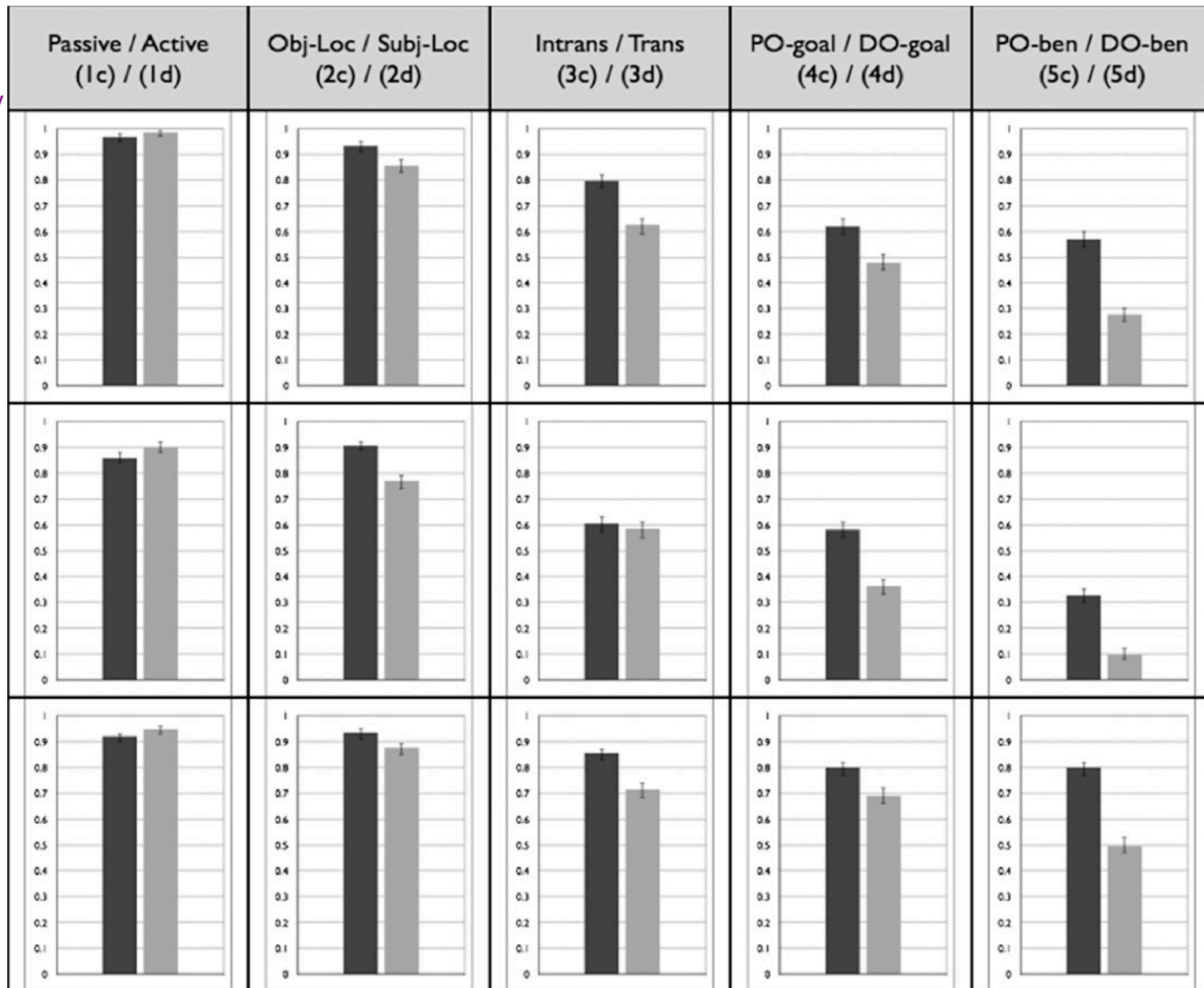
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Inferring deletions versus insertions

$$P(m | I) \propto \underbrace{P(I | m)}_{\text{Noise operation}} \underbrace{P(m)}_{\text{Plausibility}}$$

Noise operation Plausibility

The cook baked a cake for Lucy.



The cook baked a cake Lucy.

The cook baked Lucy a cake.



The cook baked Lucy for a cake.

Inferring deletions versus insertions

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①

Delete

②

Choose deletion location

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The cook baked a cake Lucy.

① Insert

② Choose insertion location

The cook baked Lucy a cake.

③ Choose what to insert

The cook baked Lucy *for* a cake.

Inferring deletions versus insertions

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①

Delete

②

Choose deletion location

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The cook baked a cake Lucy.

①

Insert

②

Choose insertion location

The cook baked Lucy a cake.



③

Choose what to insert

for

The cook baked Lucy for a cake.

Noisy-channel prediction: inferring deletions should be intrinsically easier than inferring insertions!

Five alternations in an insertion/deletion model

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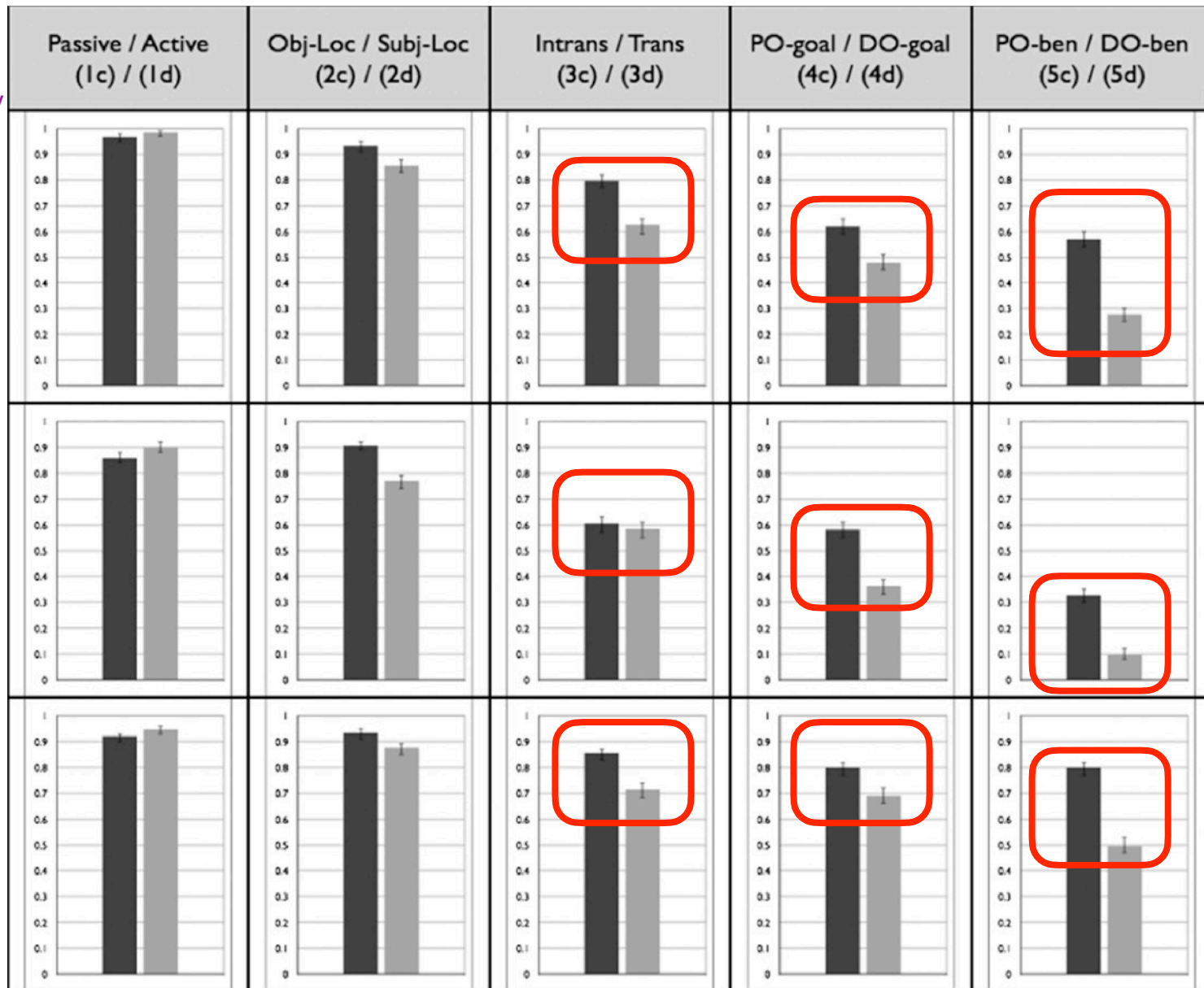
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In the real world (2008)



I'm not going to solely blame all of man's activities on changes in climate.

Sarah Palin (images credit Gage Skidmore)

 CC BY-SA

In the real world (2008)

I'm not going to solely blame all of man's activities on changes in climate.



Sarah Palin (images credit Gage Skidmore)

 CC BY-SA

I'm not one to attribute every activity of man to climate change.



Corpora of speech errors

Anticipations

John dropped his cuff of coffee

reek long race

Perseverations

John gave the goy (=gave the boy)

Spanish speaping people

teep a cape (=keep a tape)

Exchanges

the nipper is zarrow

Fancy getting your model renosed (=nose remodeled)

Revisiting the possibility of exchanges

This is a problem that I need to talk about Joe with.

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The package fell from the table to the floor. [plausible; canonical]

The package fell to the floor from the table. [plausible; non-canonical]

The package fell from the floor to the table. [implausible; canonical]

The package fell to the table from the floor. [implausible; non-canonical]

Revisiting the possibility of exchanges

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The package fell from the table to the floor. [plausible; canonical]

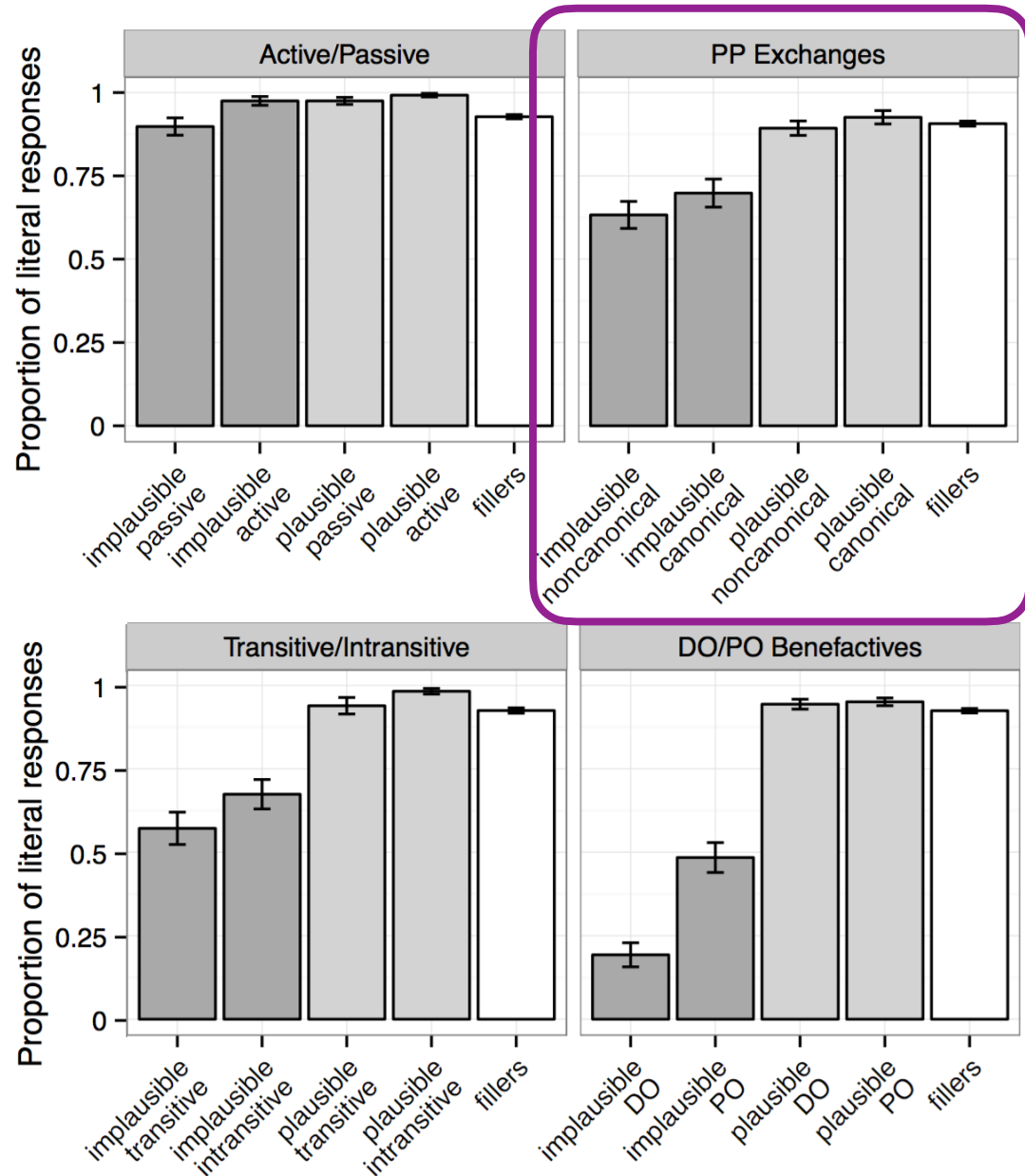
The package fell to the floor from the table. [plausible; non-canonical]

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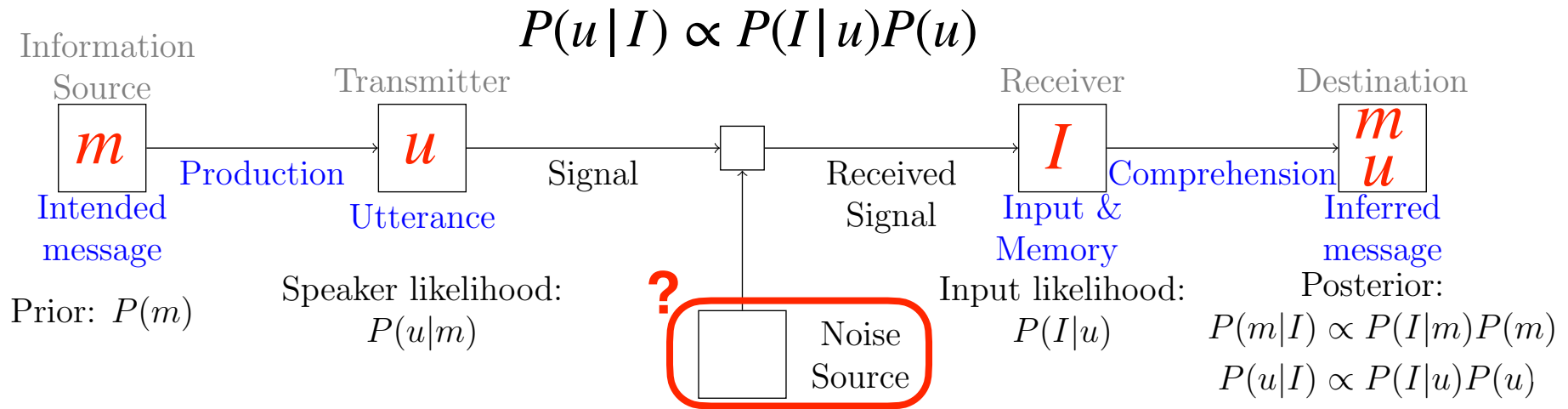
The package fell to the table from the floor. [implausible; non-canonical]

Did something fall to the floor?

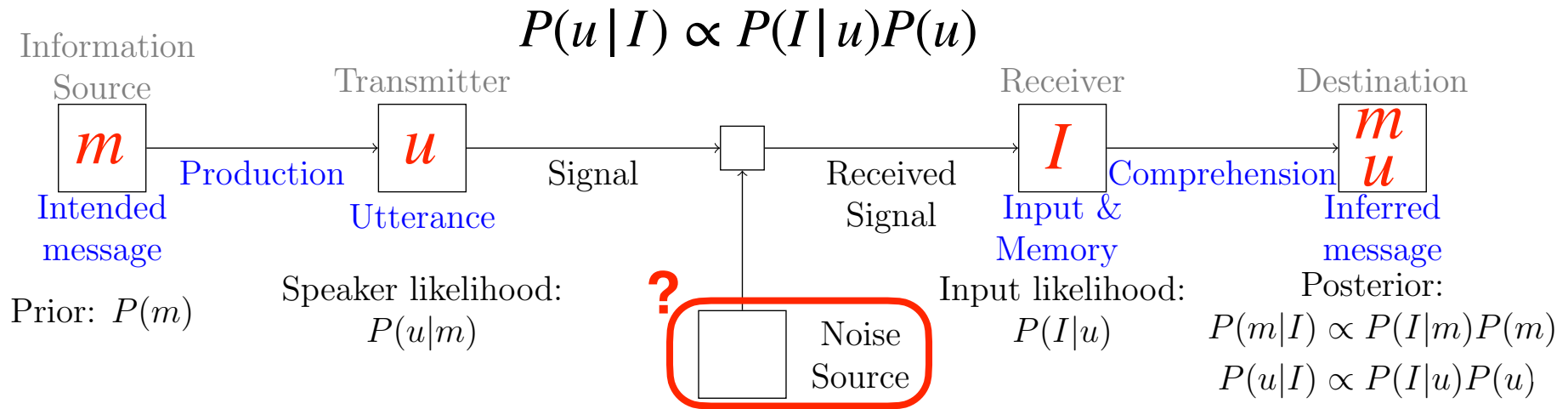
Exchanges in the noise model



Probing inferred intended utterances

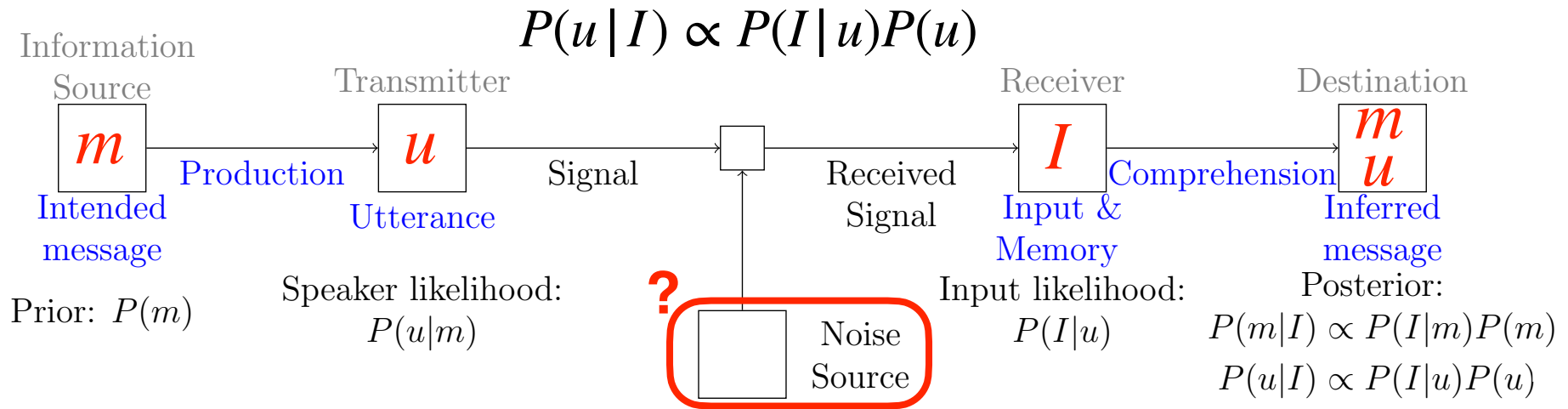


Probing inferred intended utterances



Experiment "cover story": read transcriptions of speech that might have errors, retype with edits if they think the speaker might have meant something else

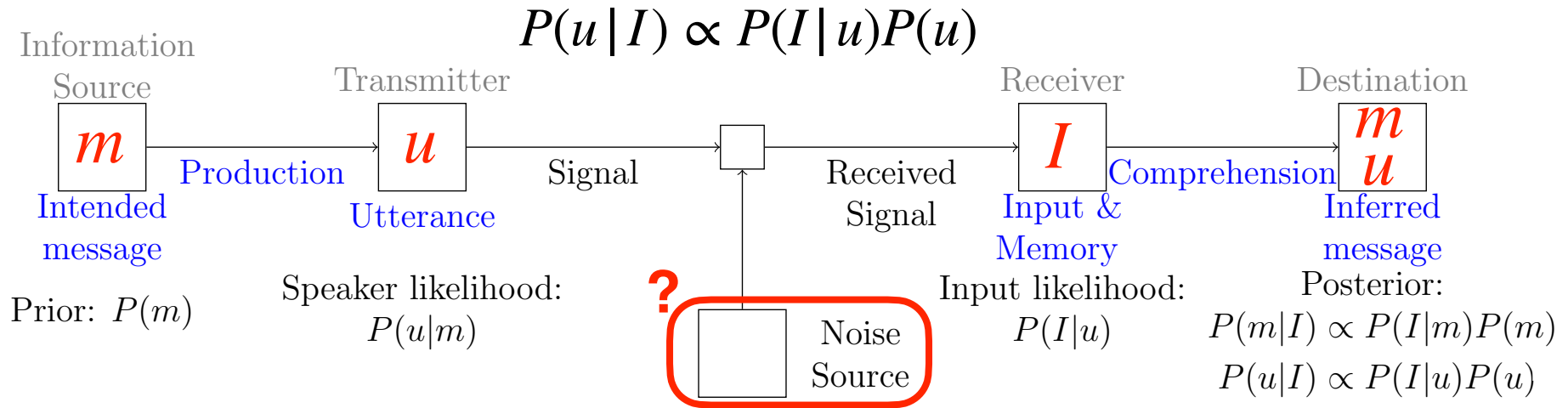
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The ball kicked the girl.

Probing inferred intended utterances



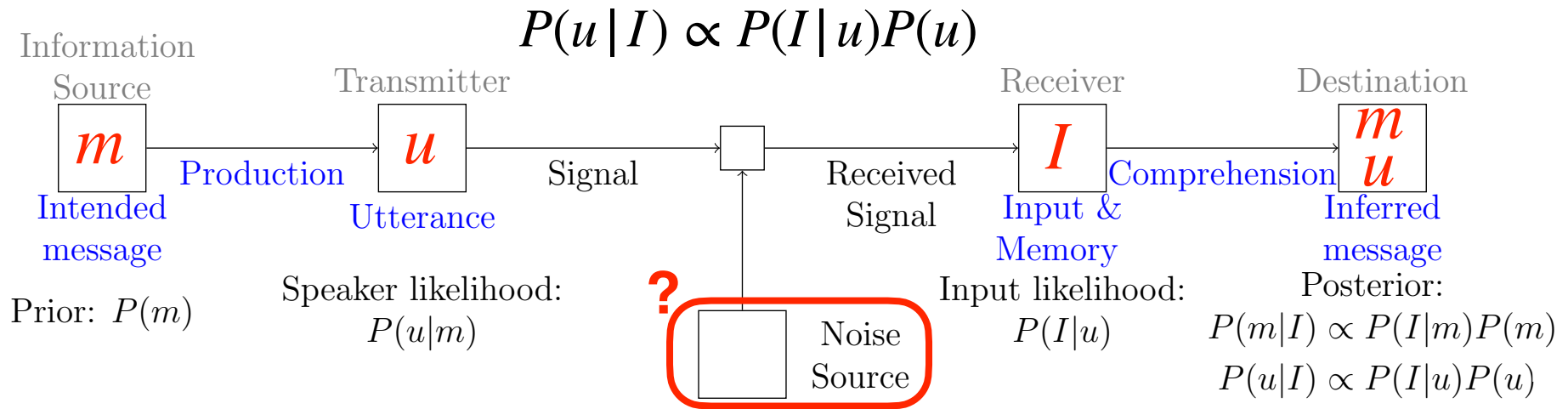
Experiment "cover story": read transcriptions of speech that might have errors, retype with edits if they think the speaker might have meant something else

The ball kicked the girl.

The ball kicked the girl.

No error

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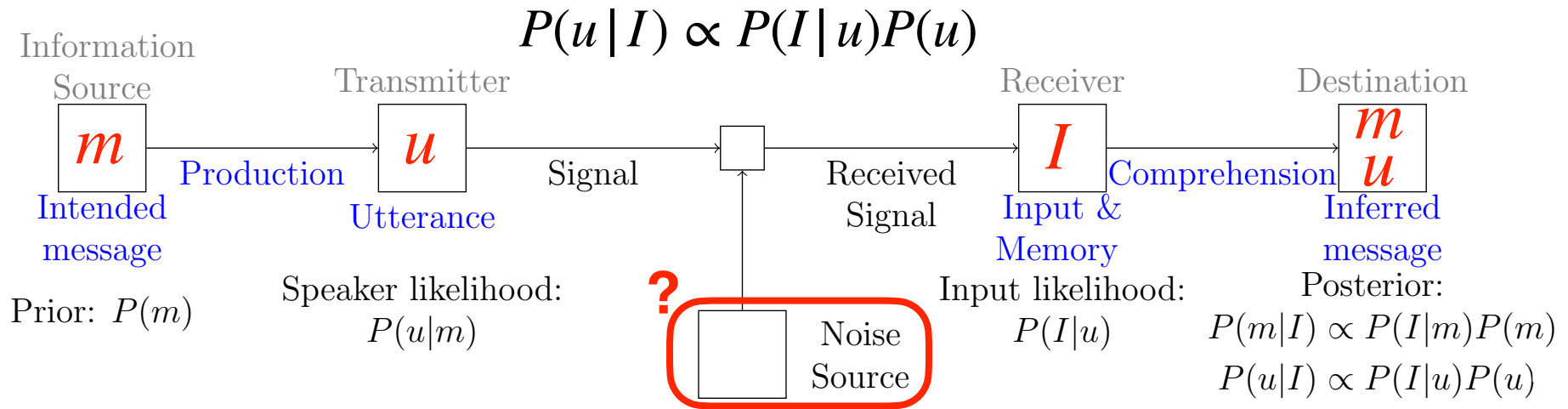
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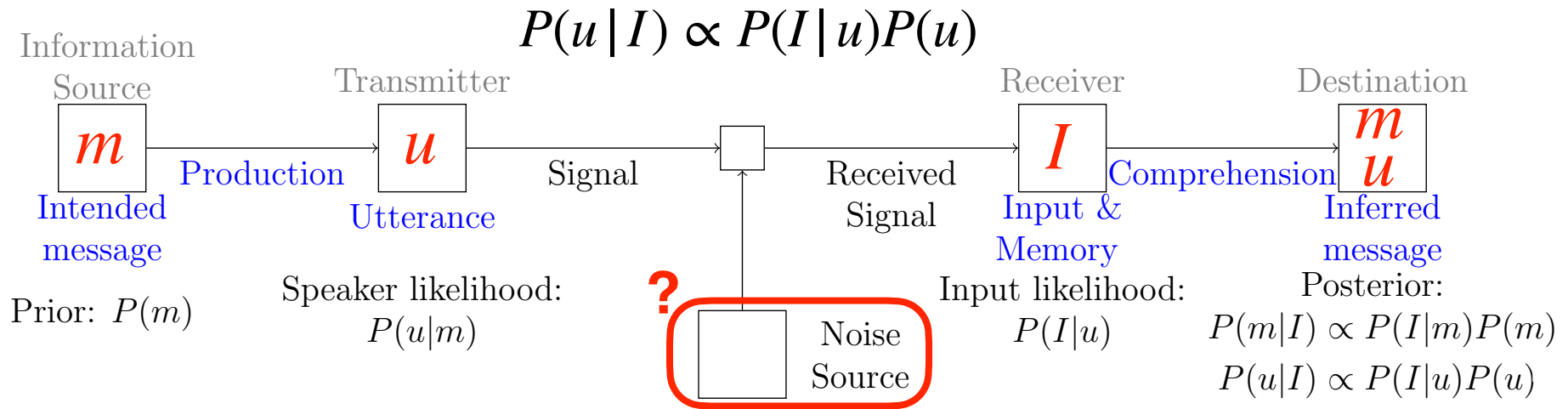
Exchange

The ball was kicked by the girl.

Deletion

(Ryskin et al., 2018)

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The ball kicked the girl. The judge gave the athlete to the prize.

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No error

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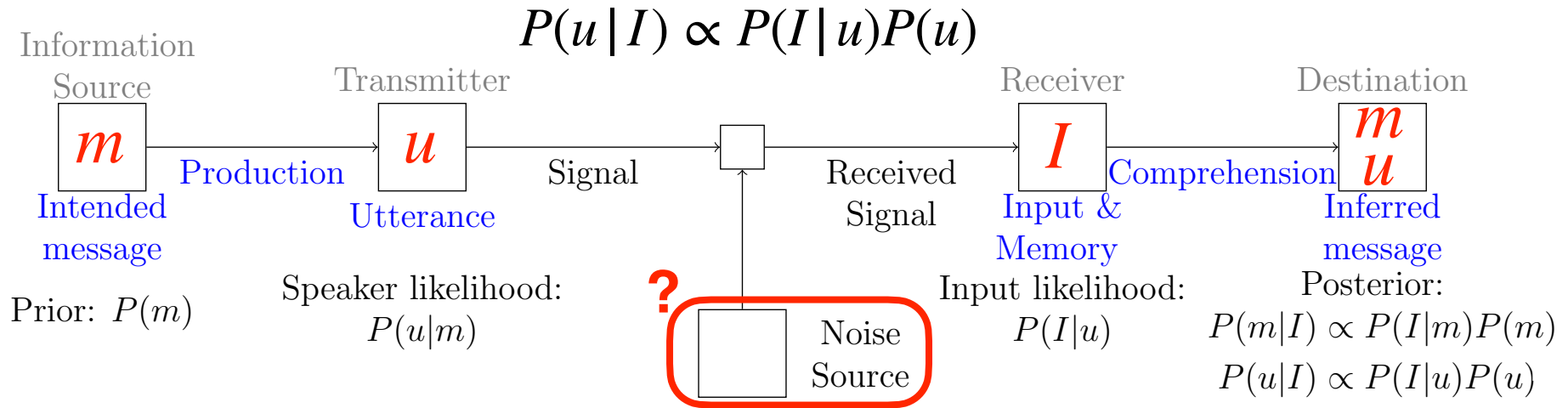
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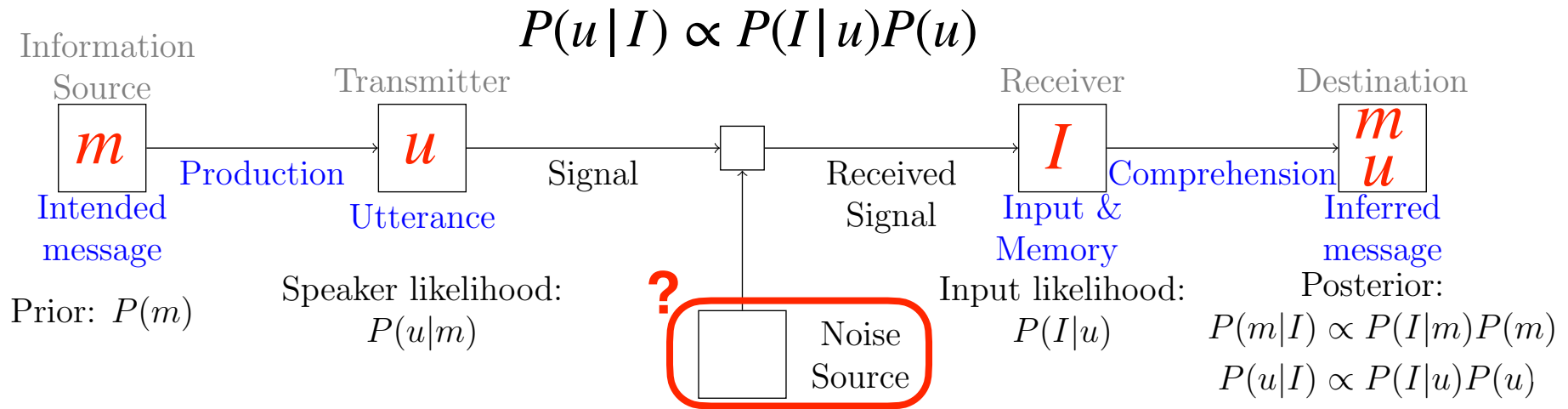
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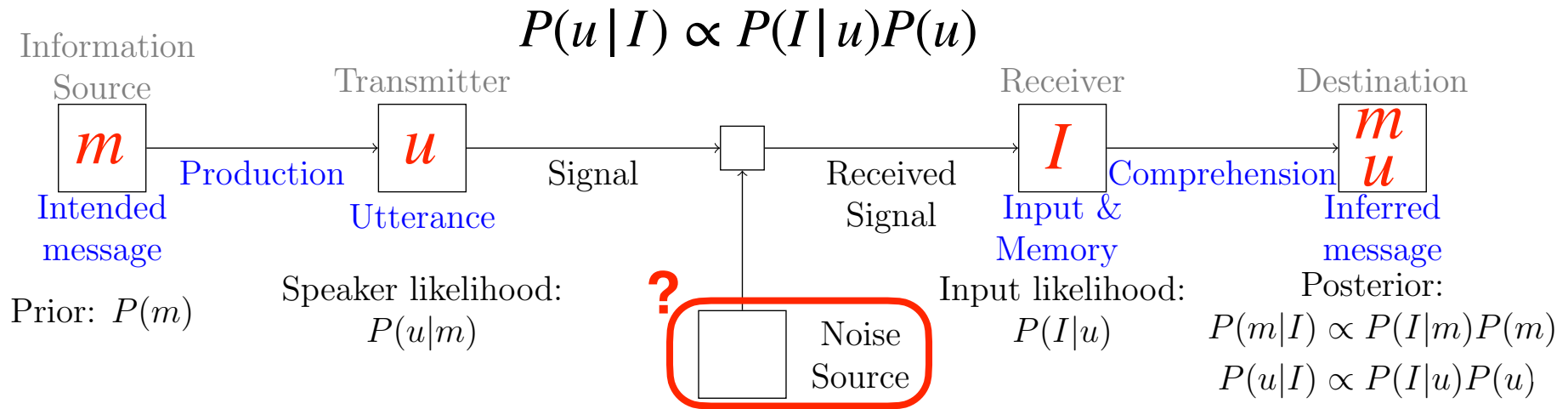
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Insertion

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Exchange

The judge gave the athlete a prize.

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Deletion

The judge gave the prize to the athlete.

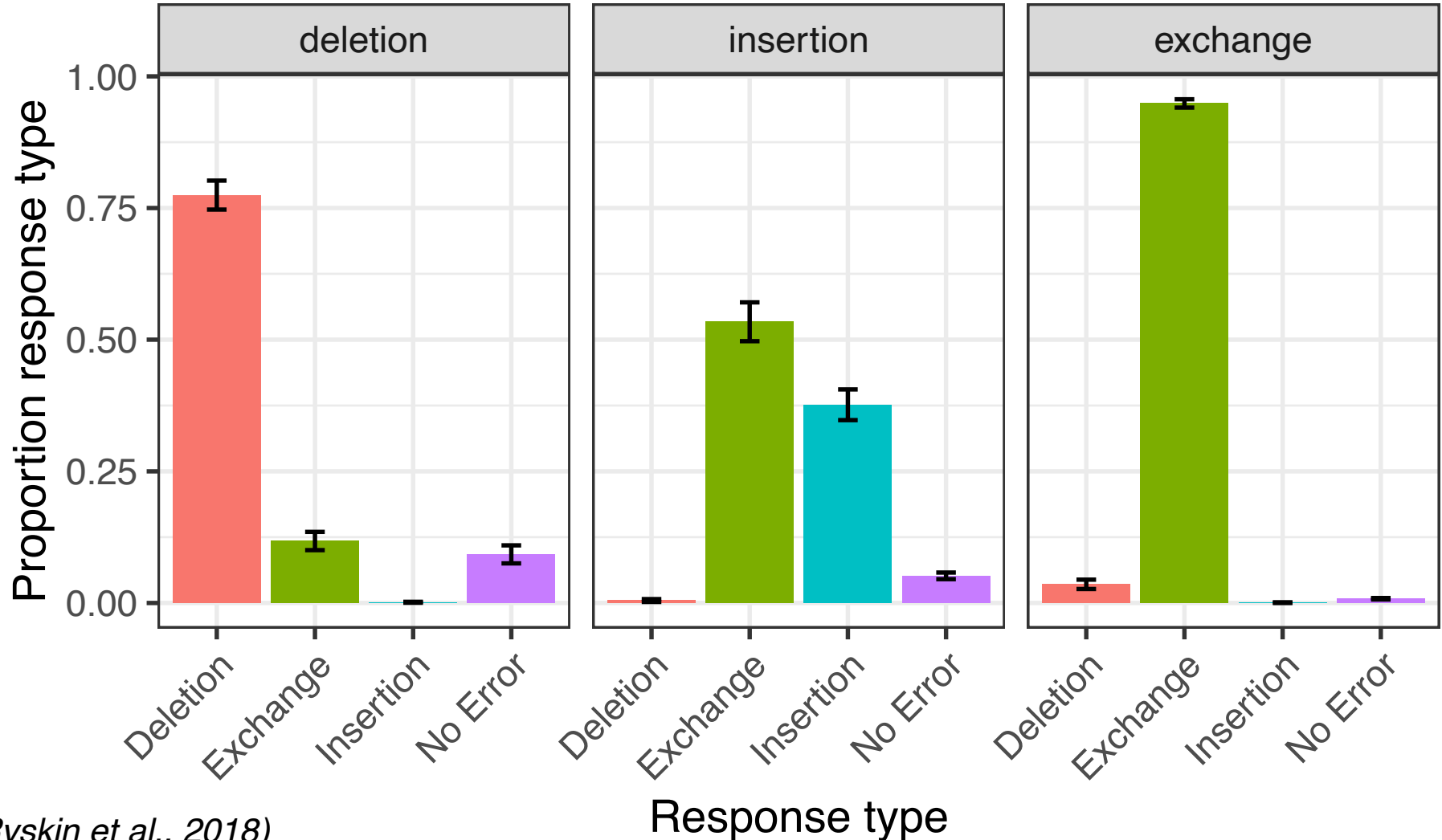
Exchange

Probing inferred intended utterances

"The corrupt politicians profited the bribes."

"The actor handed the director to the script."

"The bowl broke the grandfather."



Noisy-channel interpretation summary

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- *However*, status of exchange errors in the noise model remains a mystery

Structural Forgetting and the Noisy Channel

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1. The apartment that the maid who the cleaning service sent over was well-decorated.

Structural Forgetting and the Noisy Channel

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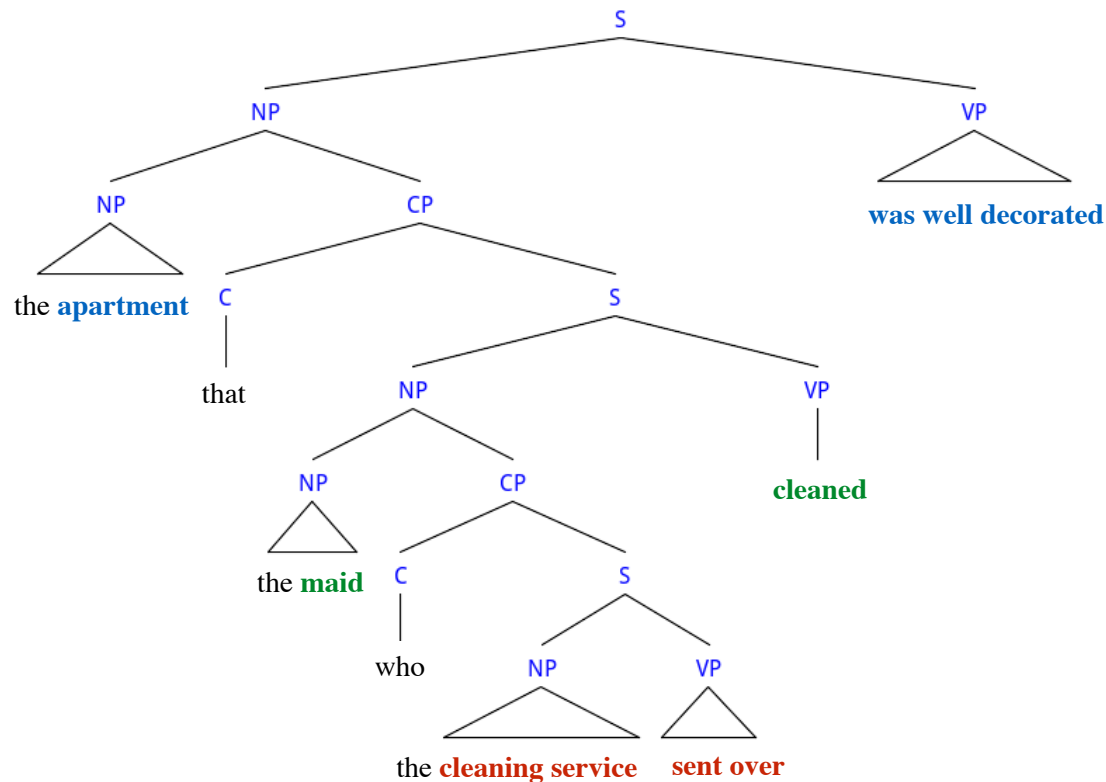
Structural Forgetting

1. *The **apartment** that the **maid** who the **cleaning service sent over was well-decorated.** 👍
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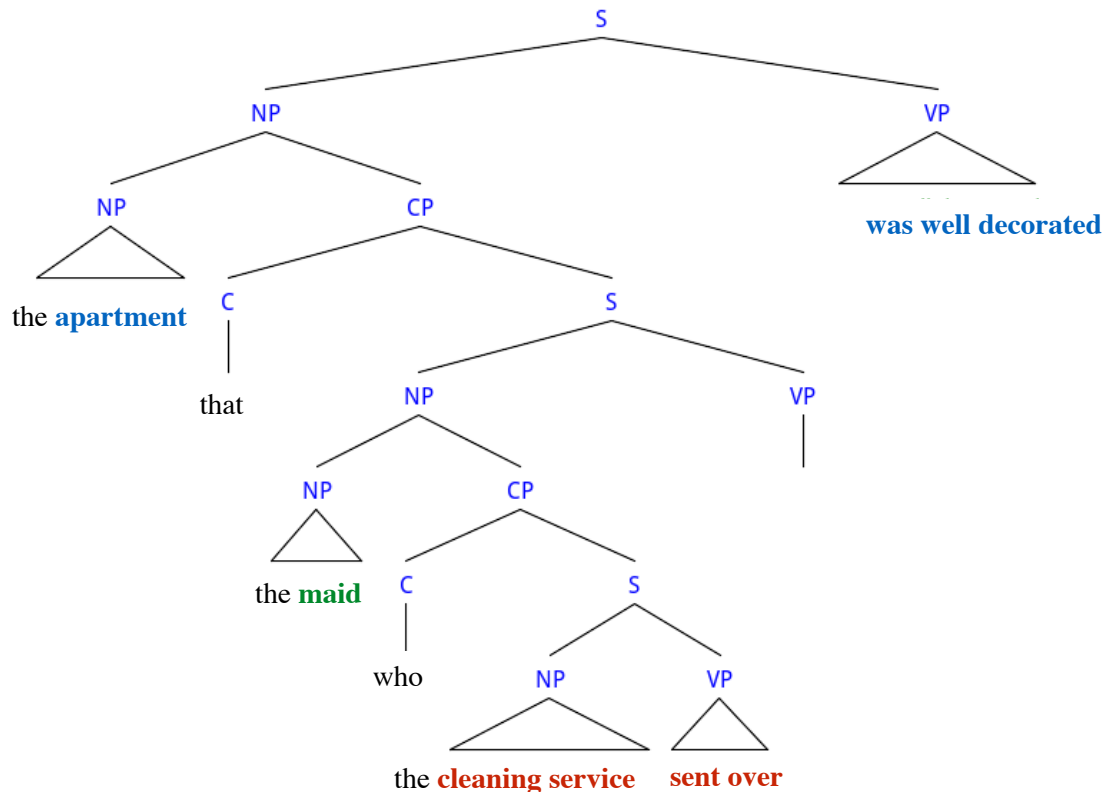
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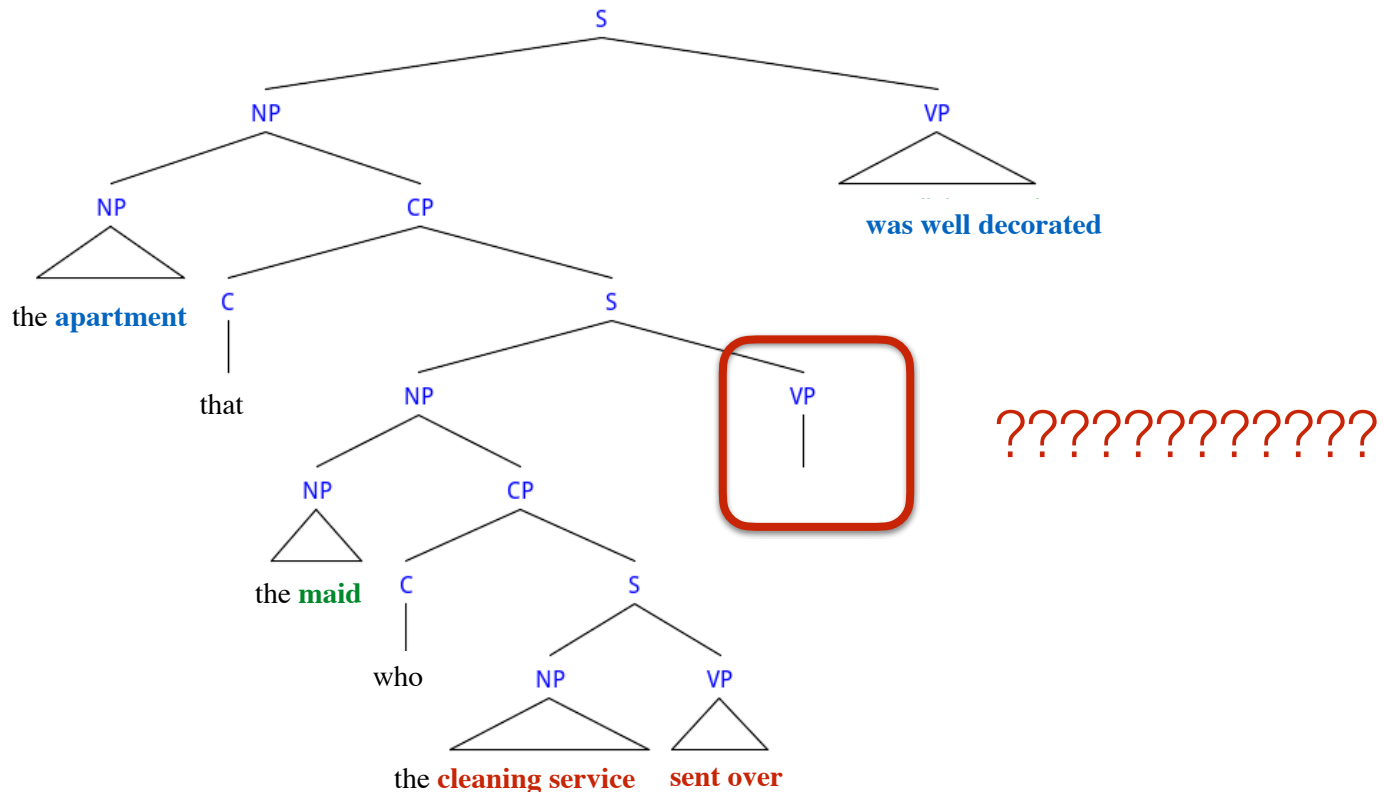
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- **Structural forgetting effect:** part of the sentence is forgotten by the time you get to the end (Gibson & Thomas, 1999; Frazier, 1985; Fodor, p.c.)

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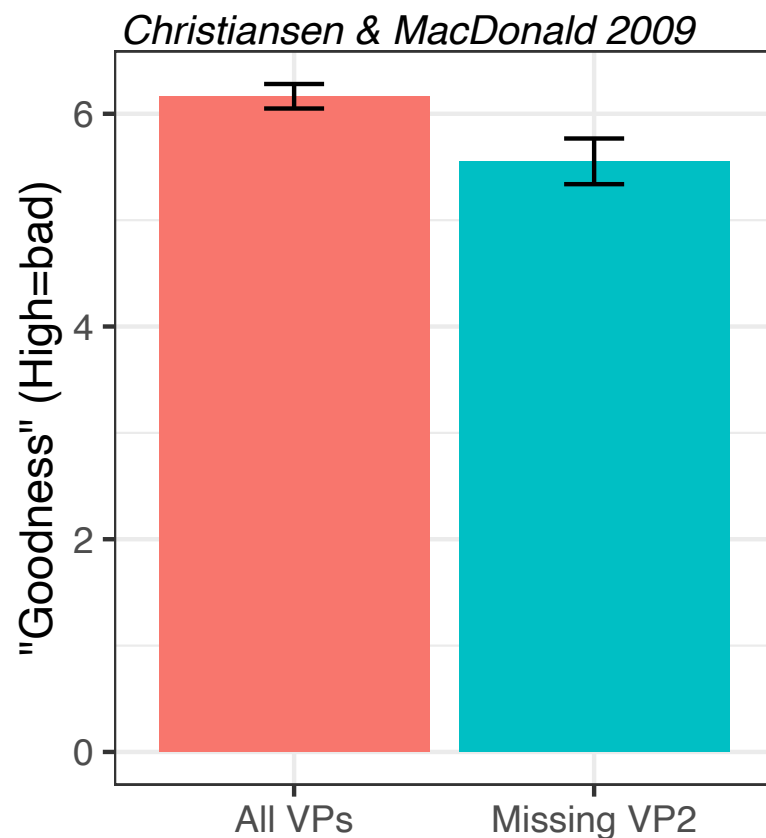
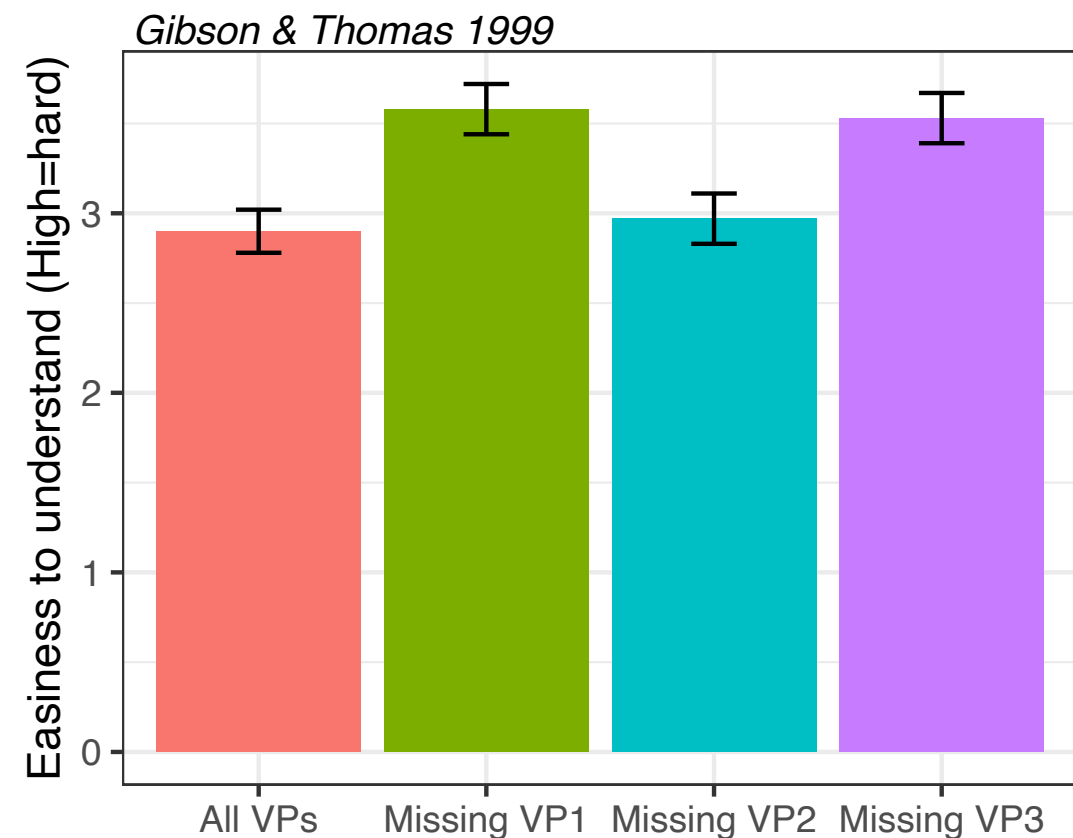
- **Structural forgetting effect:** part of the sentence is forgotten by the time you get to the end (Gibson & Thomas, 1999; Frazier, 1985; Fodor, p.c.)
- The ungrammatical sentence seems better than the grammatical one.
 - A "**grammaticality illusion**": how could we define grammaticality in this case?

Gibson & Thomas 1999: whole-sentence reading

The ancient manuscript that the graduate student who the new card catalog had confused a great deal was studying in the library was missing a page.

Christiansen & MacDonald 2009: word-by-word self-paced reading, follows by rating

The chef who the waiter who the busboy offended appreciated admired the musicians.



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- But the effect is **language-dependent** (Vasishth et al., 2010; Frank et al., 2016).

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 - In German (and Dutch), people prefer 2 over 1.
- What is the difference between English and German?
- Frank et al. (2016) show that a recurrent neural network gives higher probability to (1) in English, but (2) in German.
 - But why?

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- These contexts are more common in German than English (Roland et al., 2007).

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 - English: the maid [that cleaned the apartment]
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 - English: the maid [that cleaned the apartment] **80%**
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 - English: the maid [that cleaned the apartment] **80%**
the apartment [that the maid cleaned] **20%**
 - German: das Dienstmädchen, [das die Wohnung reinigte]
die Wohnung, [die das Dienstmädchen reinigte]

Noisy-Context Surprisal Account of Structural Forgetting

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context

key word

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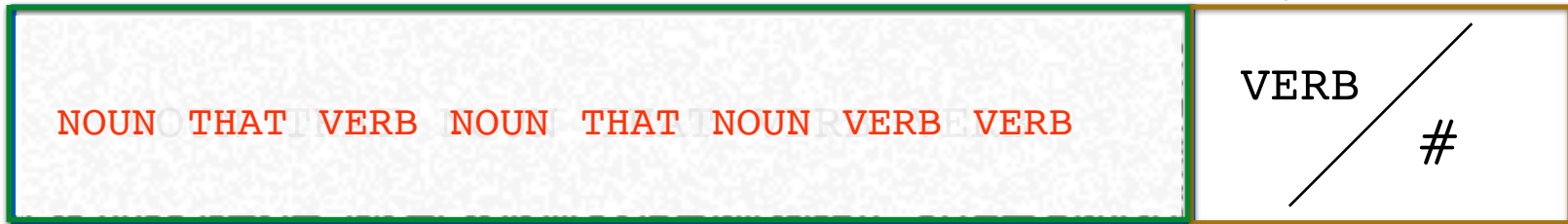
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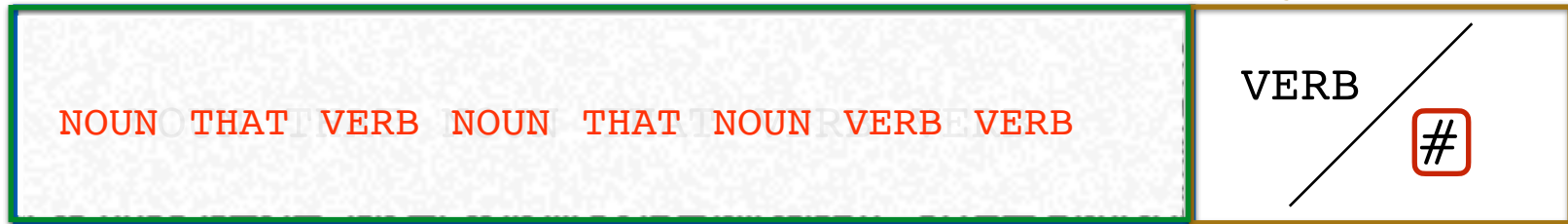
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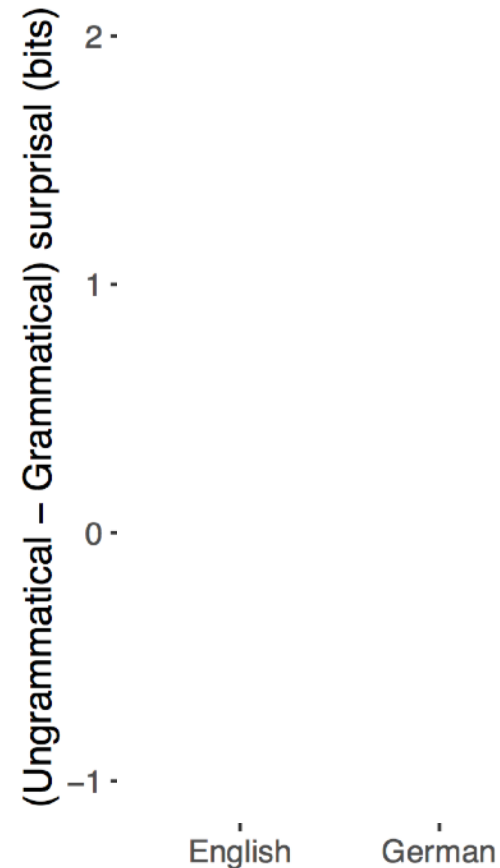
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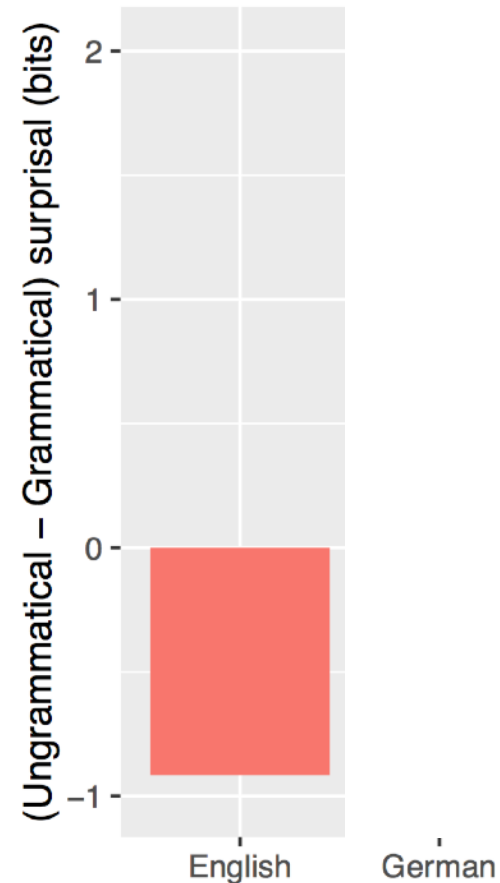
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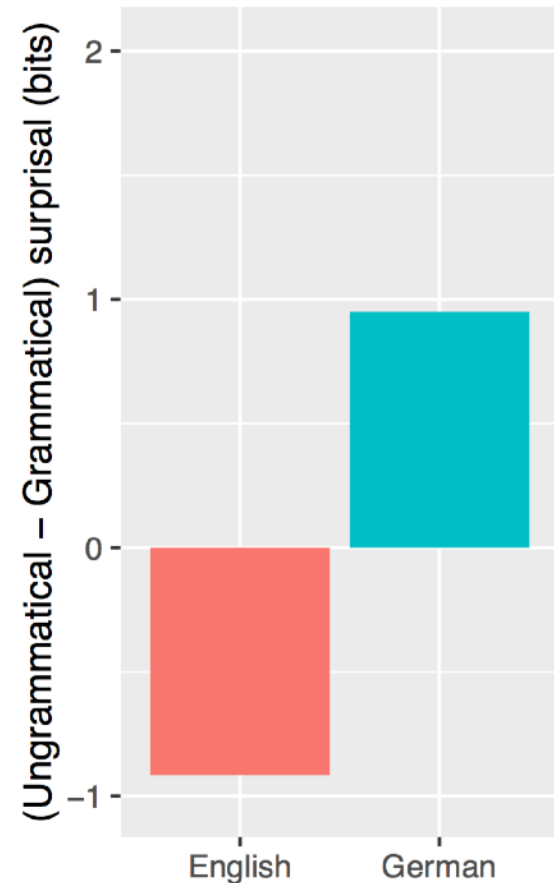
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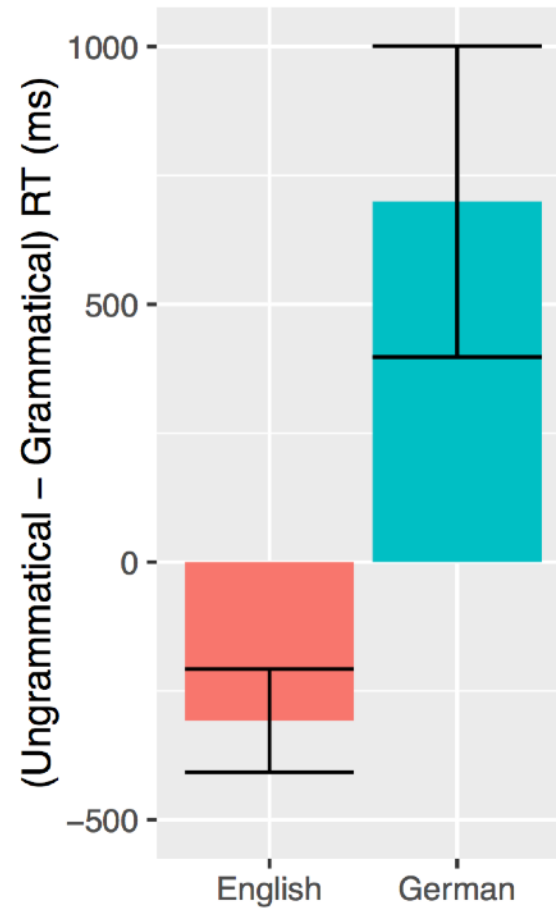
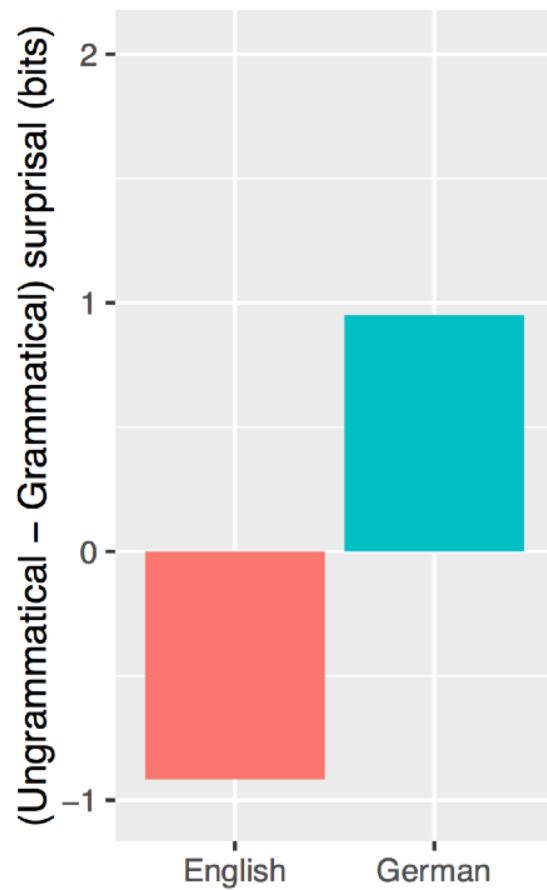
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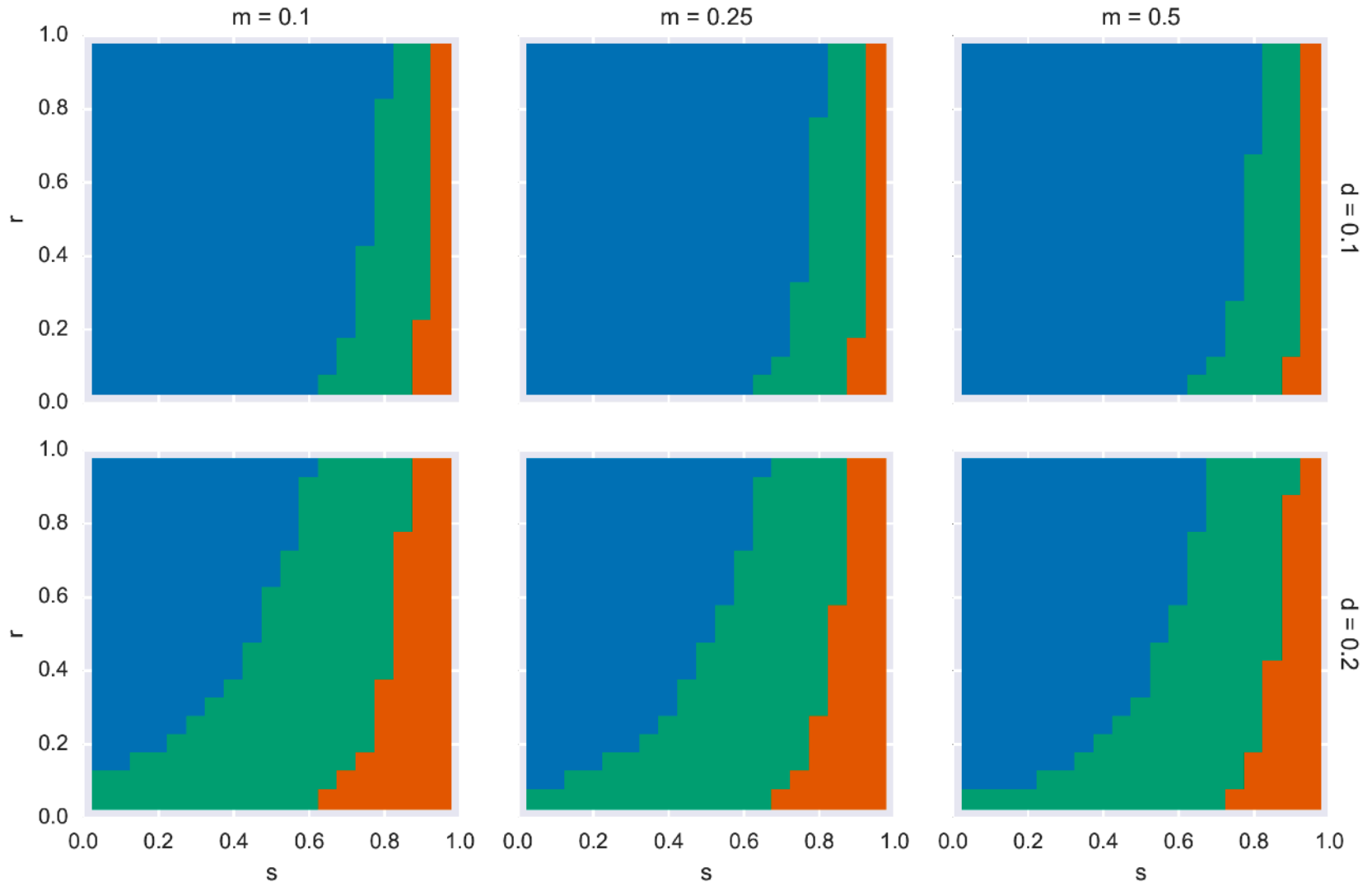
Robustness to choice of model parameters

m Modifier probability

s Probability of English RC being verb-final

d Probability of context token deletion

 = English+German-like pattern



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Structural Forgetting and the Noisy Channel



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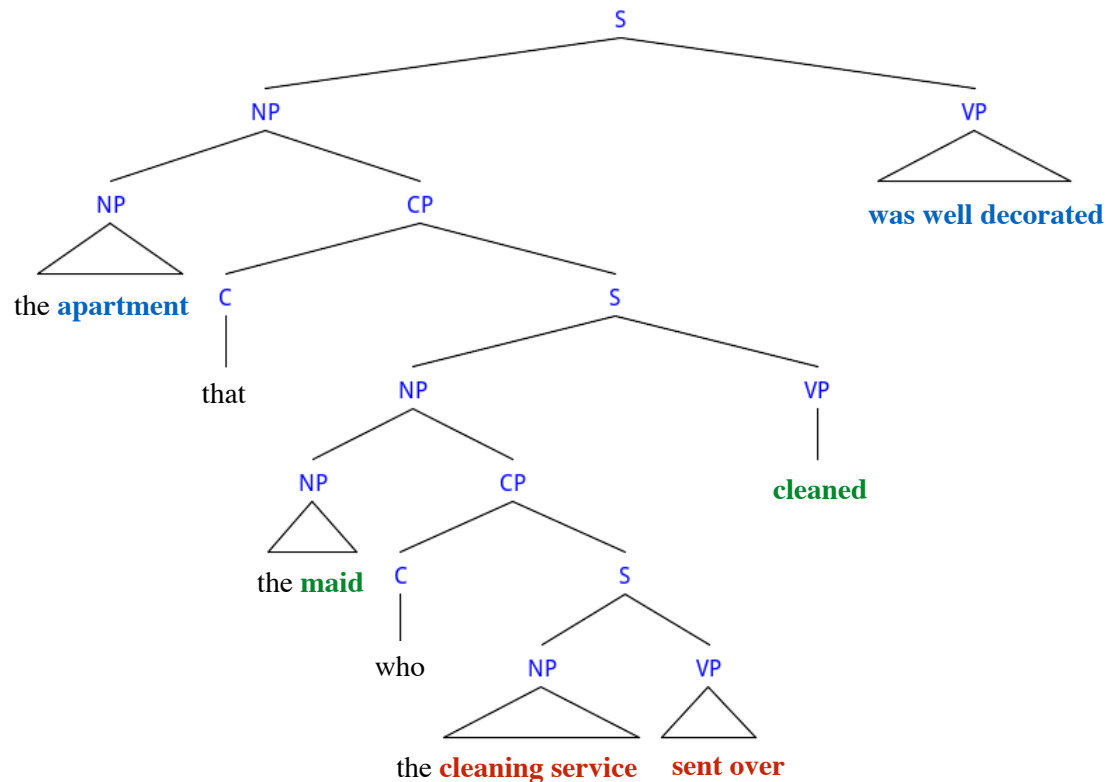
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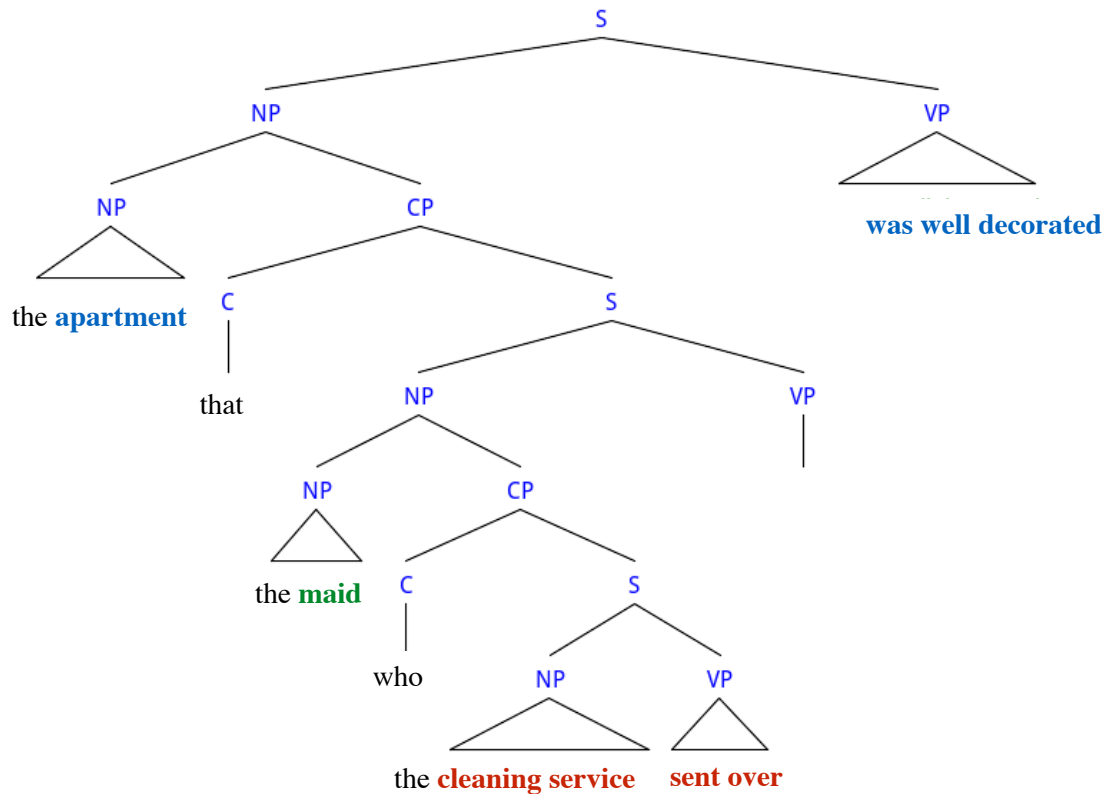
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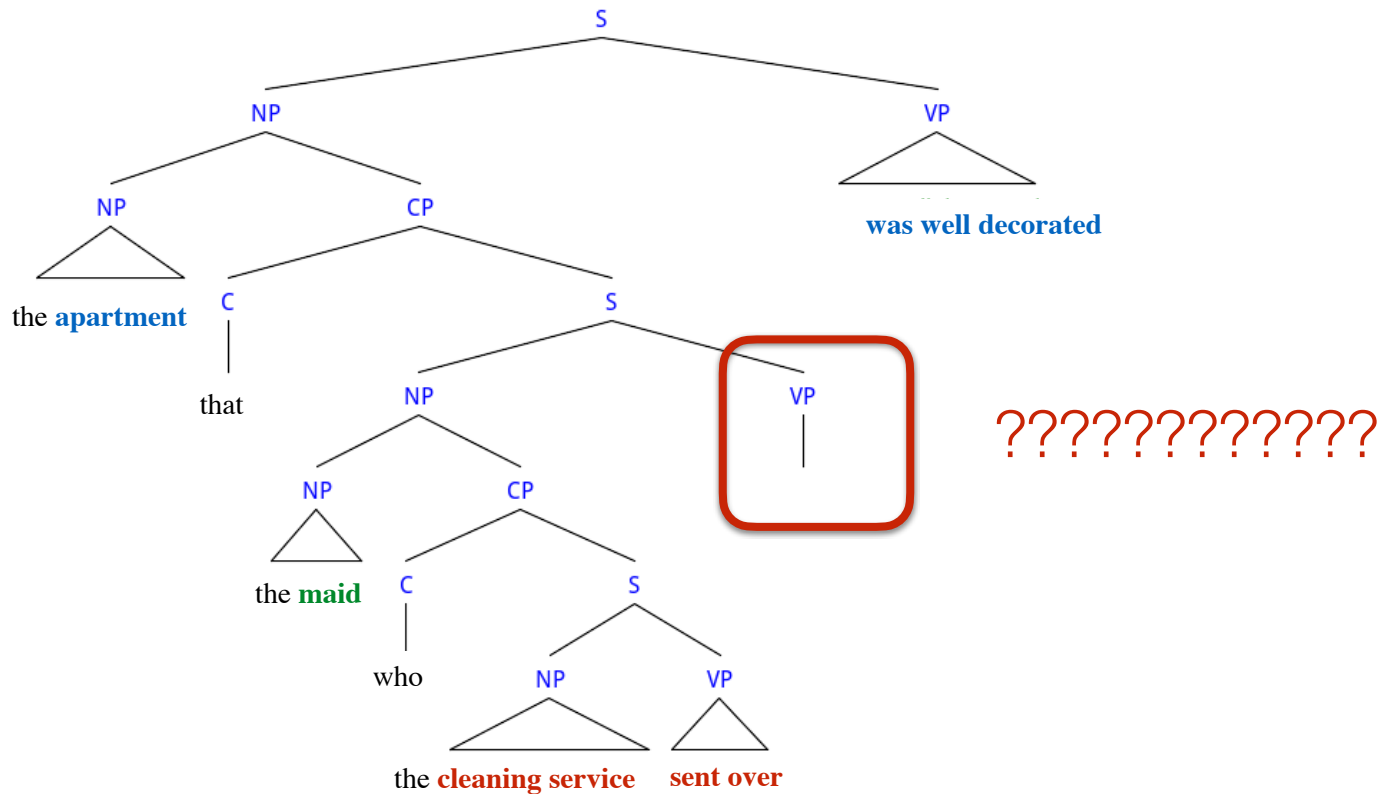
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- The ungrammatical sentence seems better than the grammatical one.
 - A "**grammaticality illusion**": how could we define grammaticality in this case?

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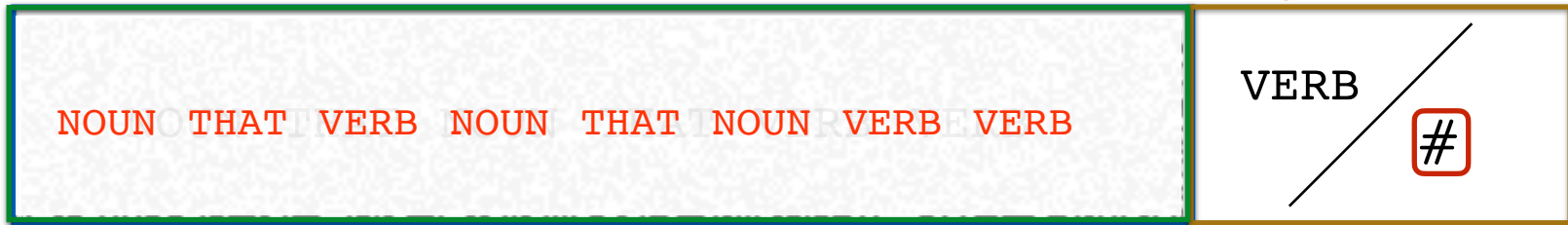
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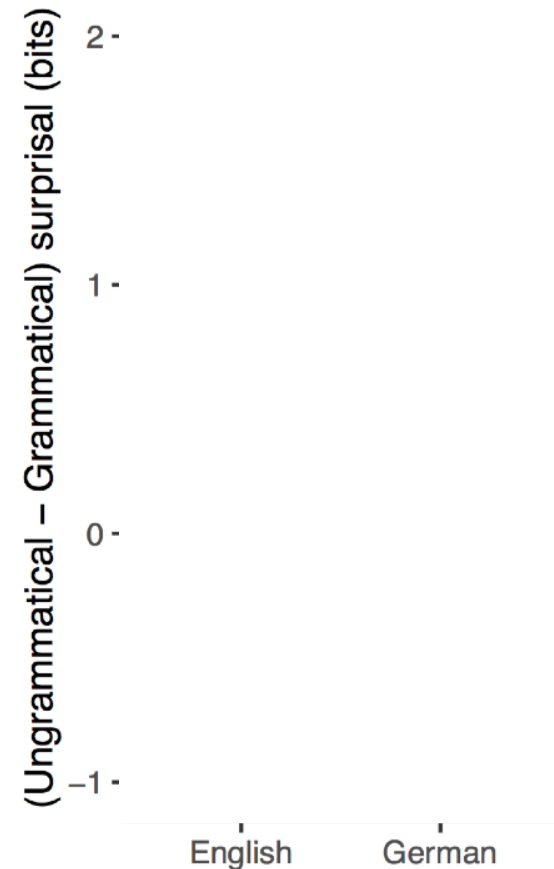
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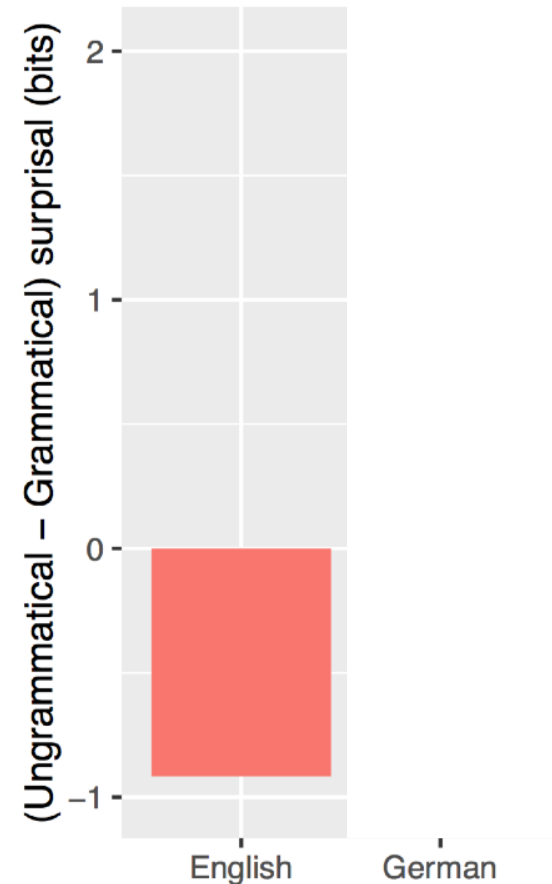
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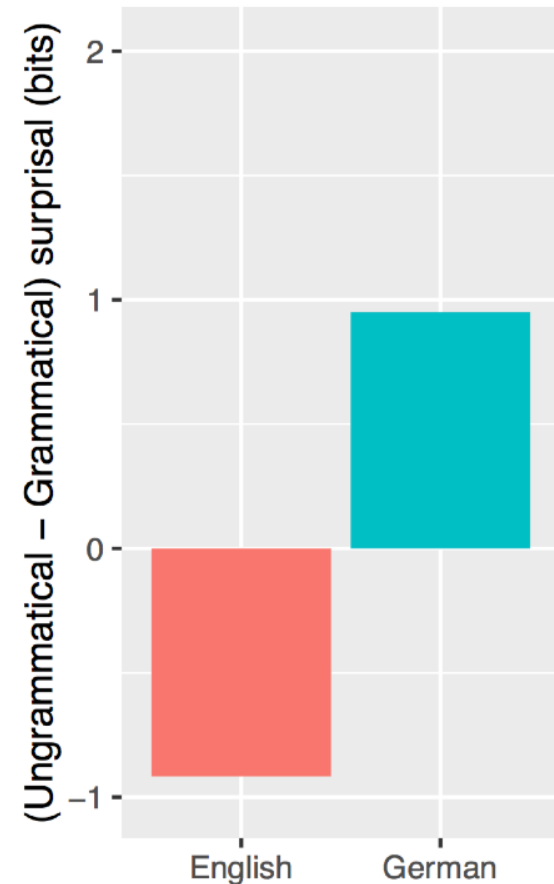
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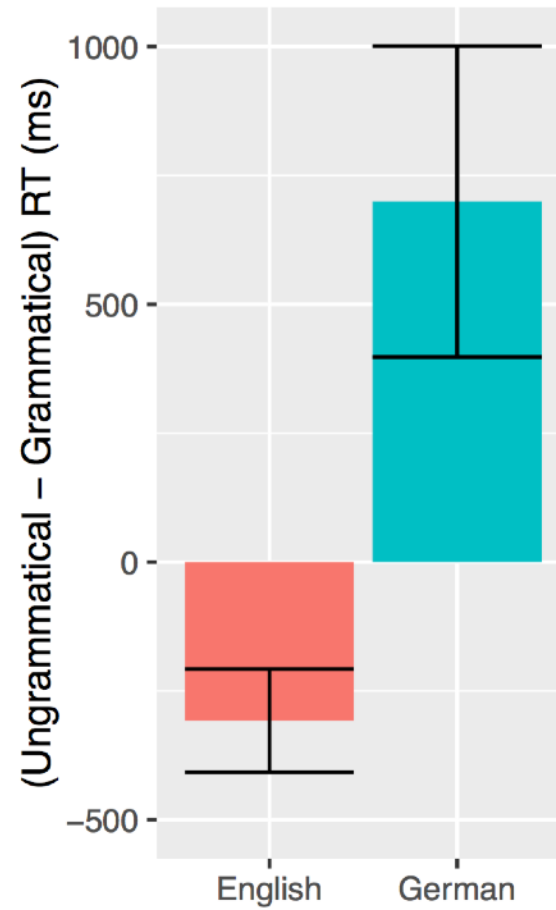
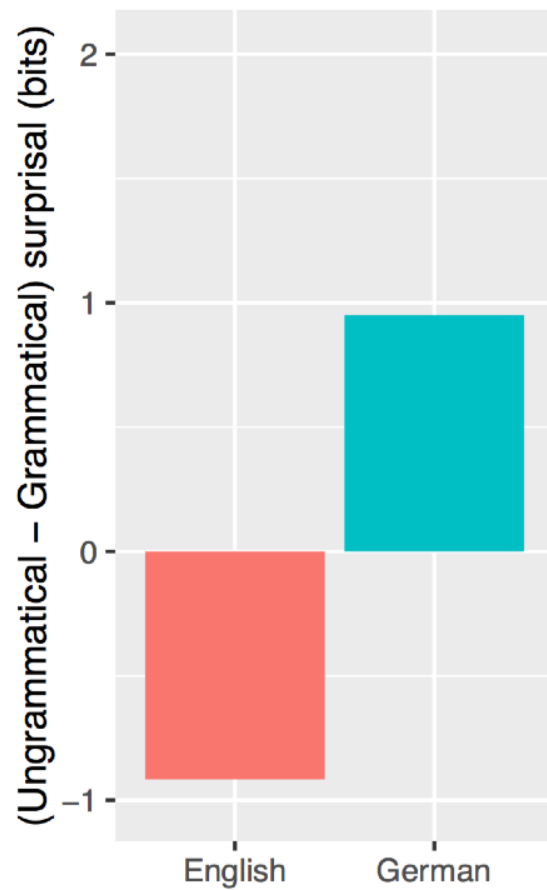
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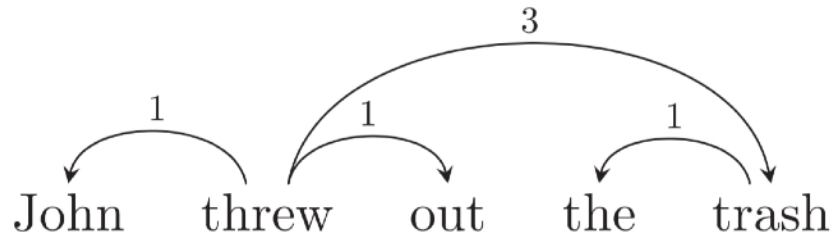
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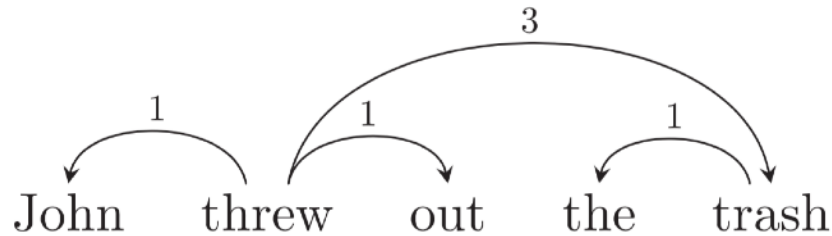
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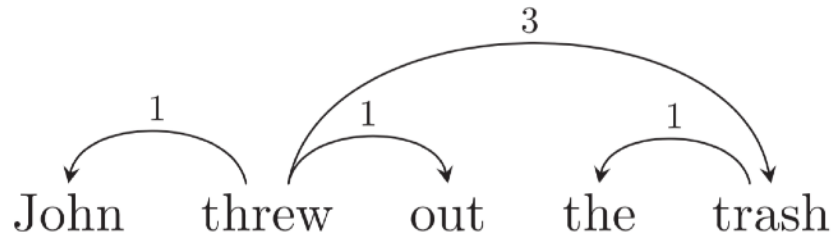
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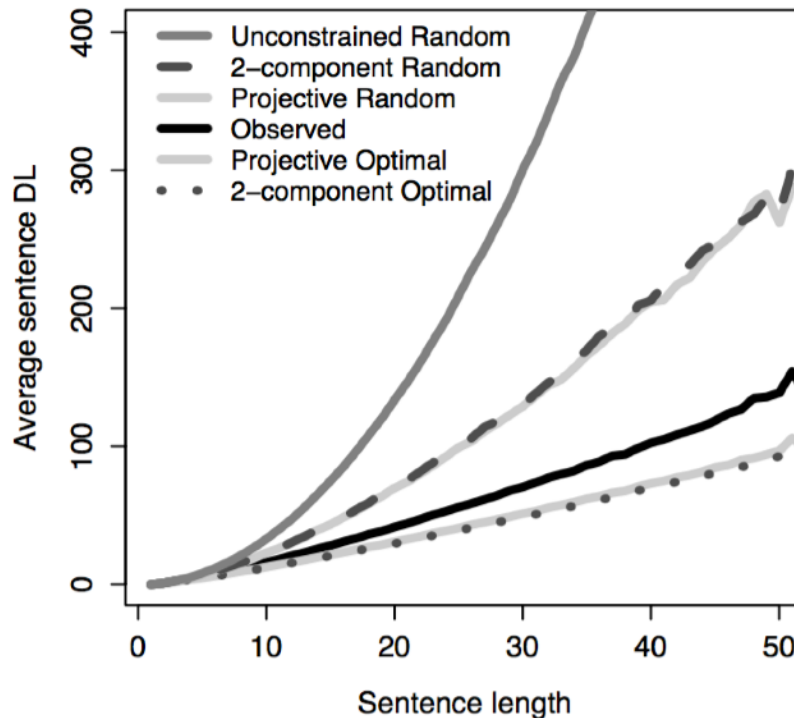
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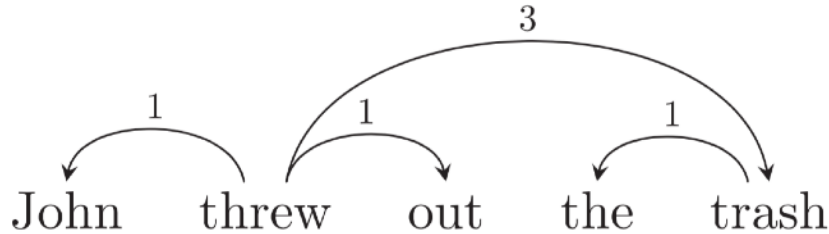


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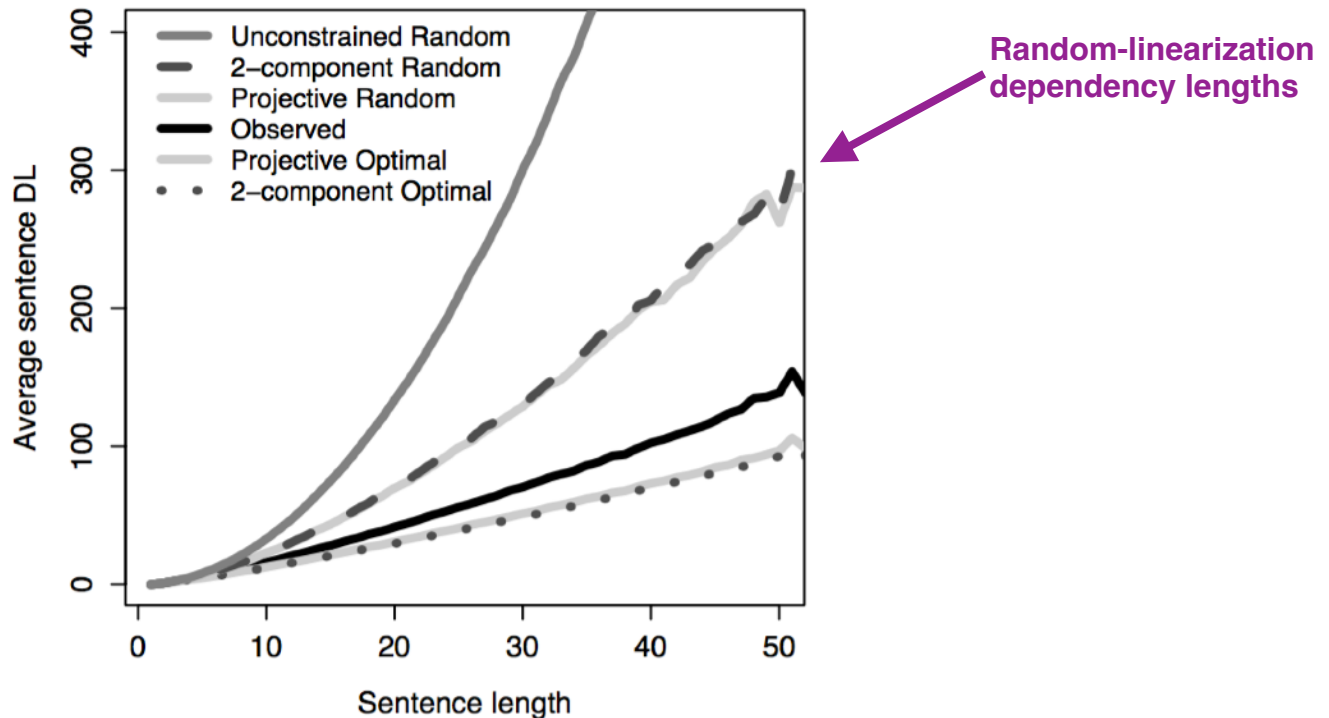


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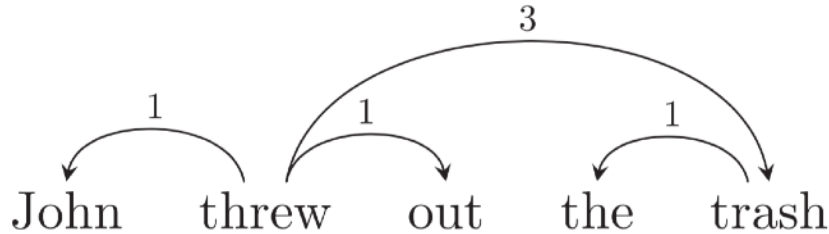


- Idea with long history: short dependencies preferred

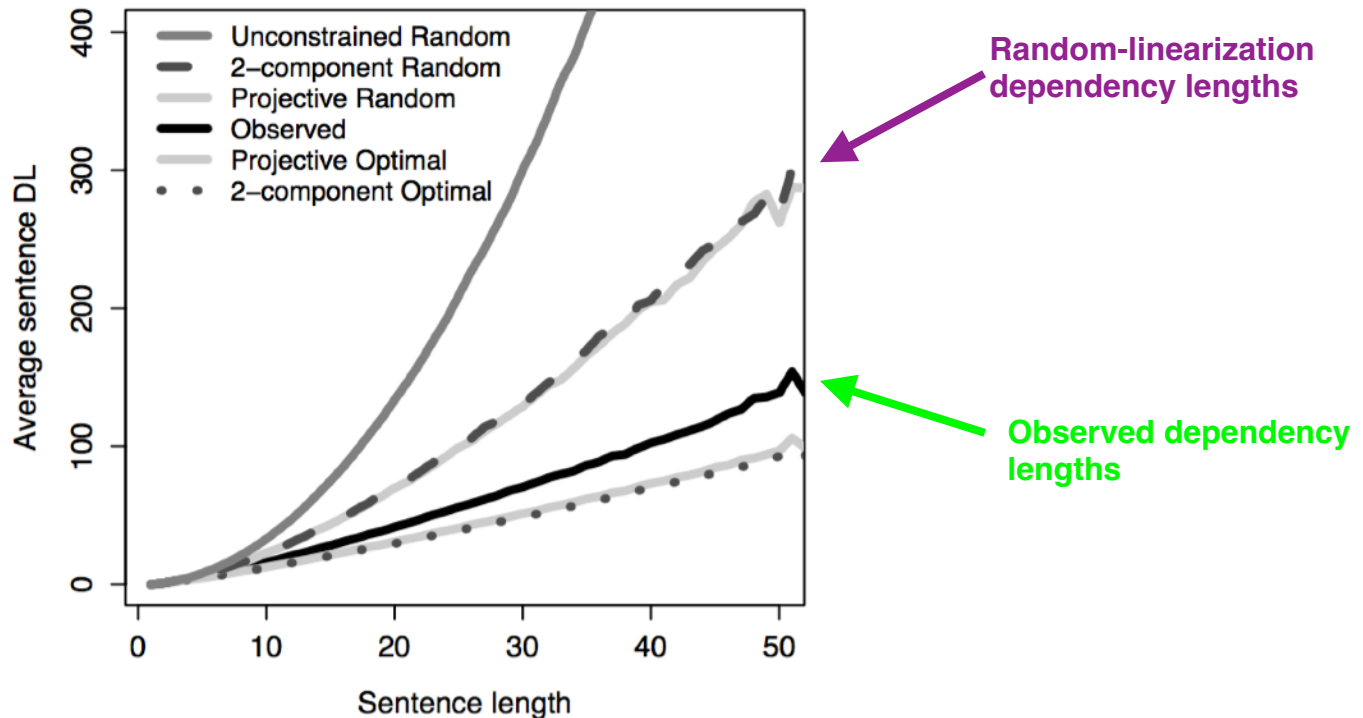


Dependency length and noisy-channel surprisal

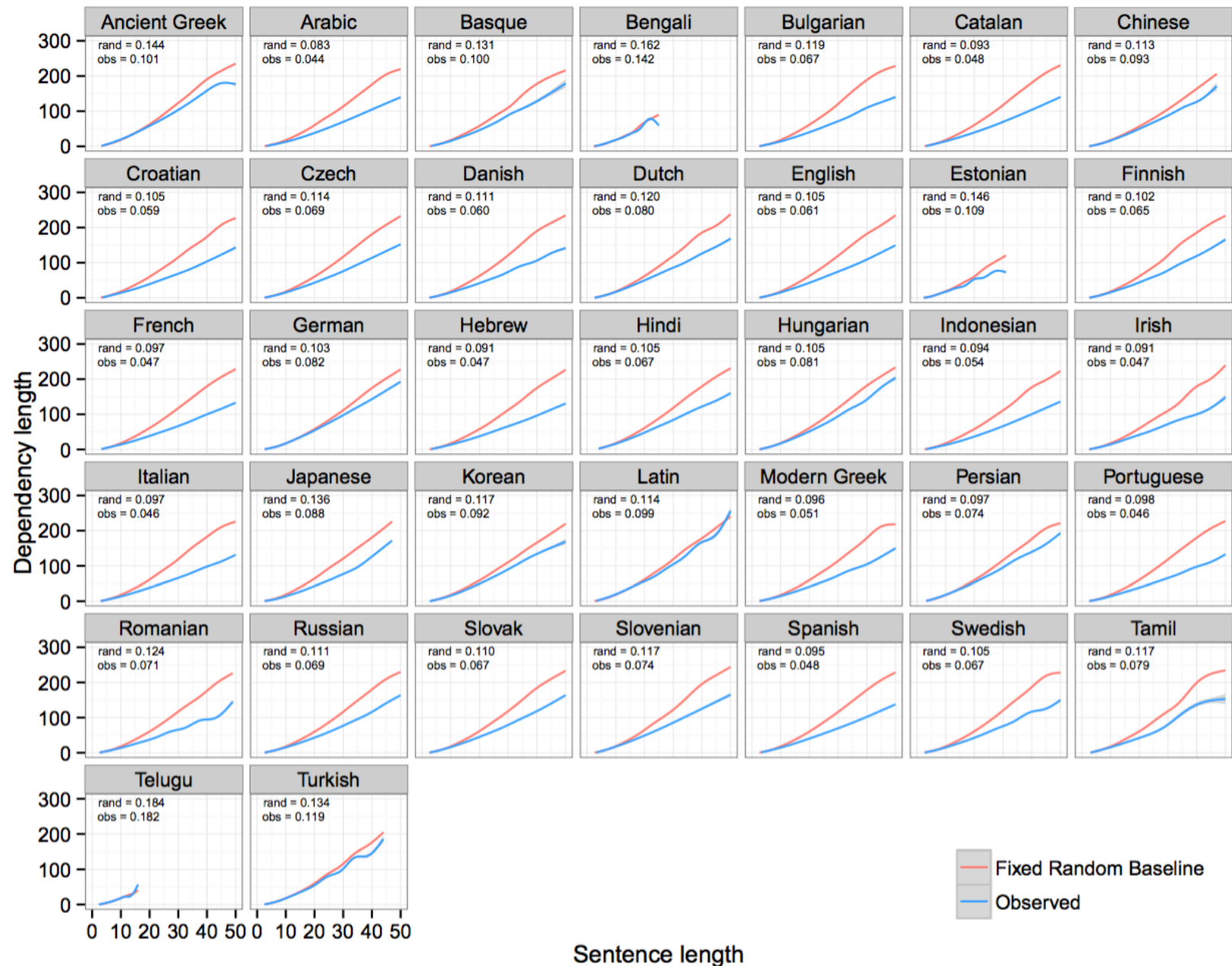
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Dependency lengths are short across languages!



Dependency lengths and the noisy channel

- Here: dependency length minimization can be derived from a combination of surprisal & noisy-channel theory



Richard Futrell

From noisy-channel & surprisal to dependency length minimization

context

John threw the old trash sitting in the kitchen

out

From noisy-channel & surprisal to dependency length minimization

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- Suppose we have an **increasing noise rate** the longer a word has been in memory.

From noisy-channel & surprisal to dependency length minimization

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- We call this **information locality** (following Gildea & Jaeger, 2015).

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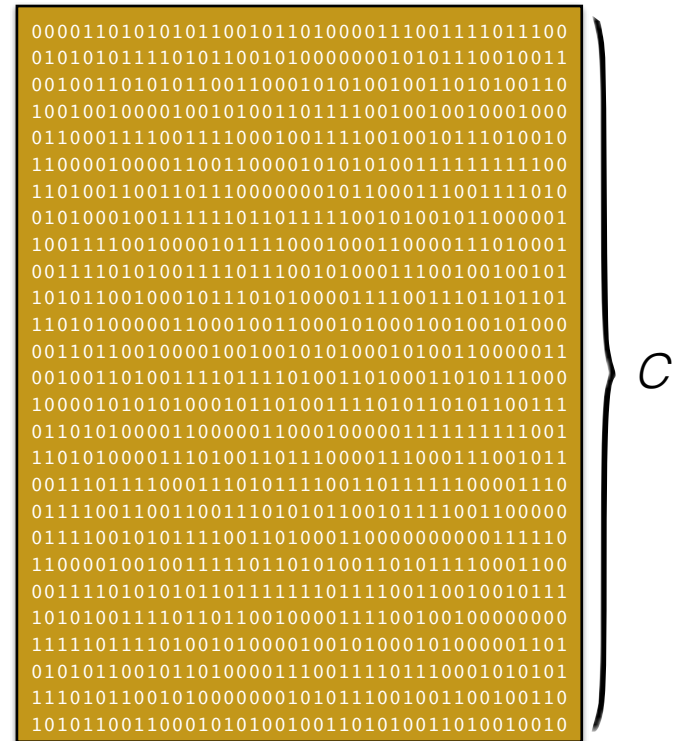
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$h(\text{out})$



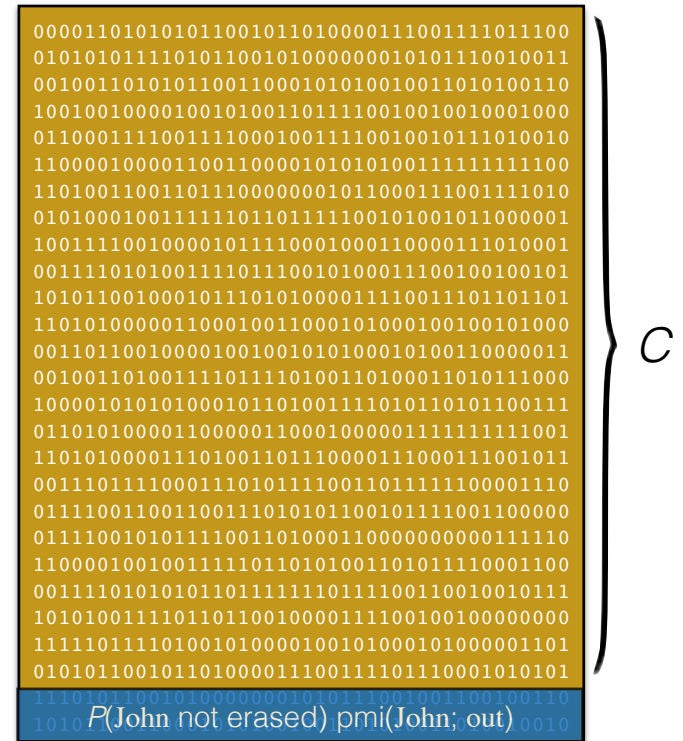
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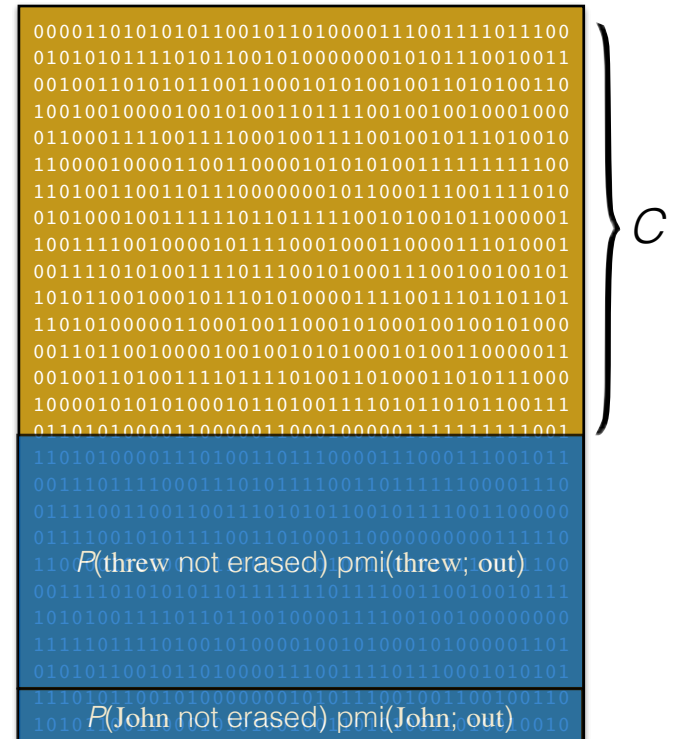
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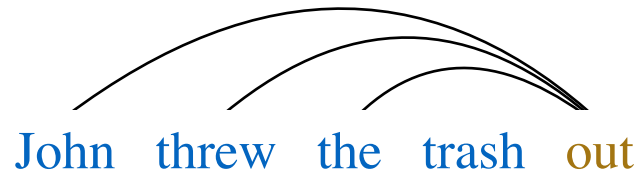
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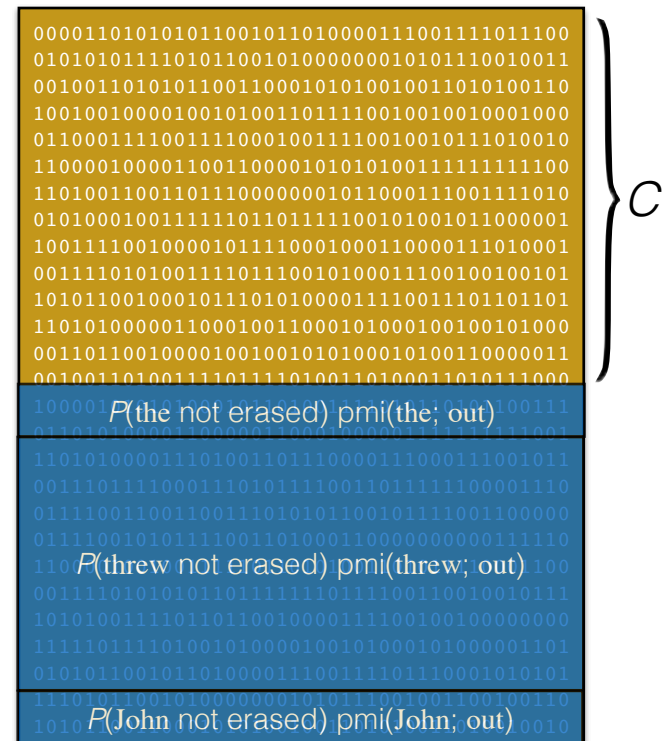
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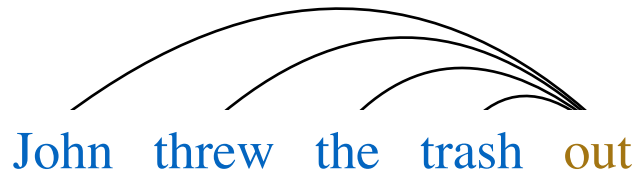
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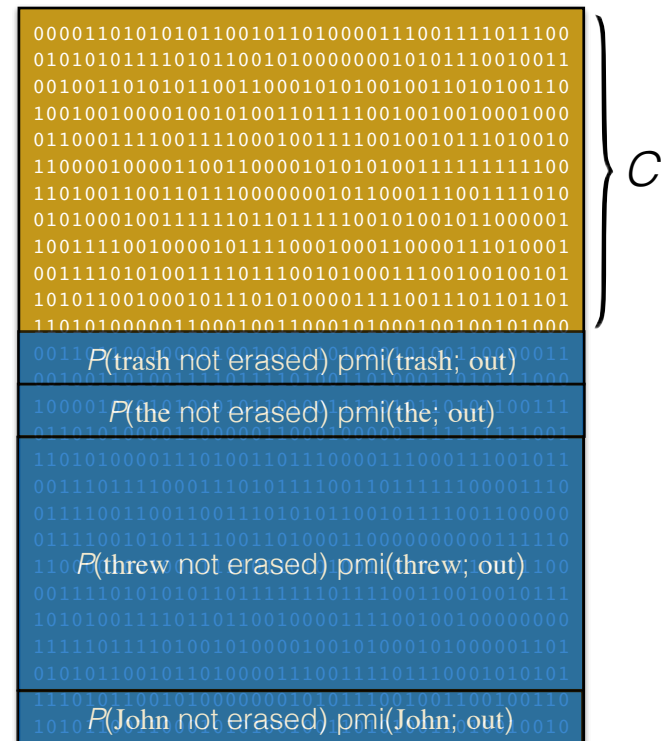
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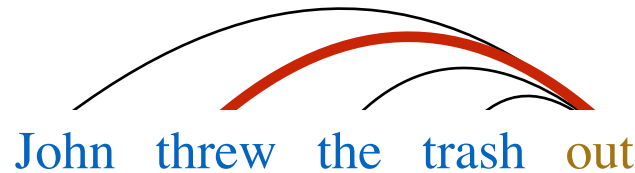
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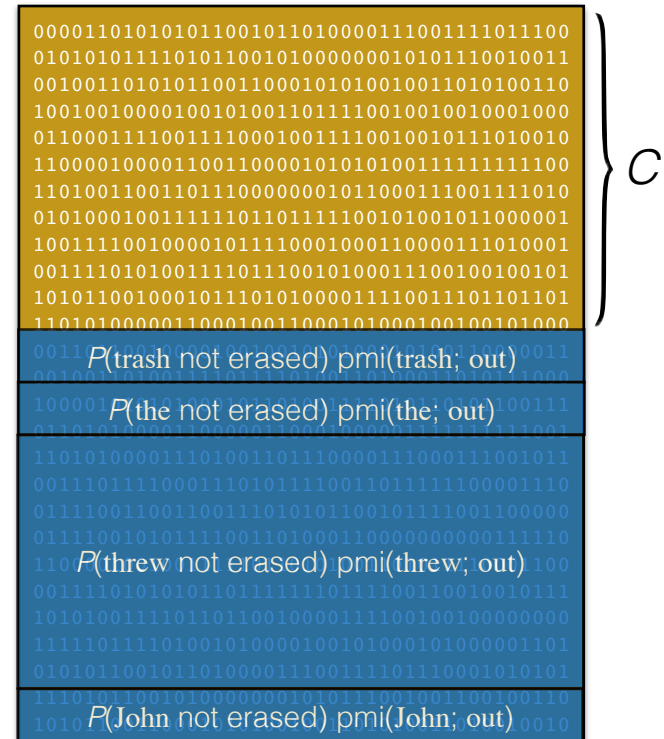


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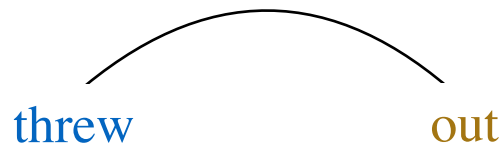
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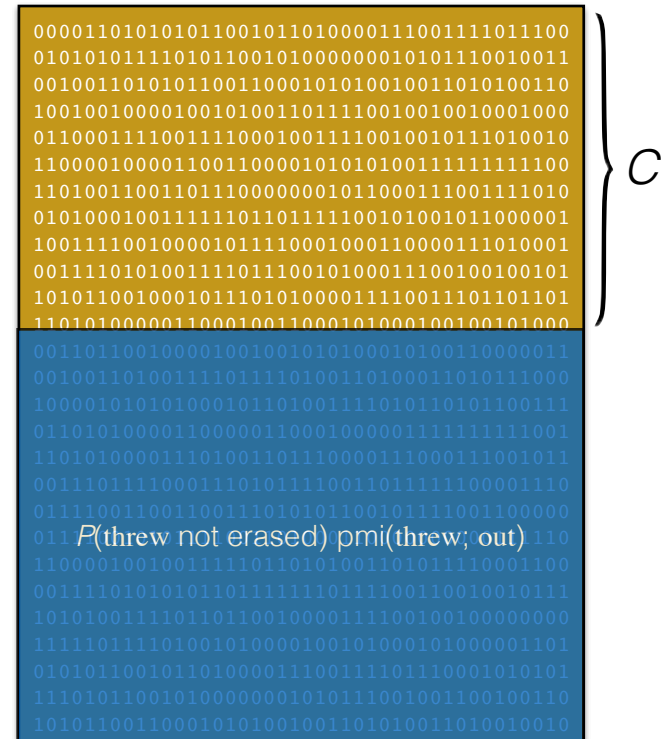
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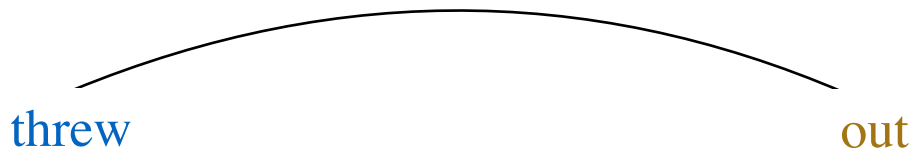
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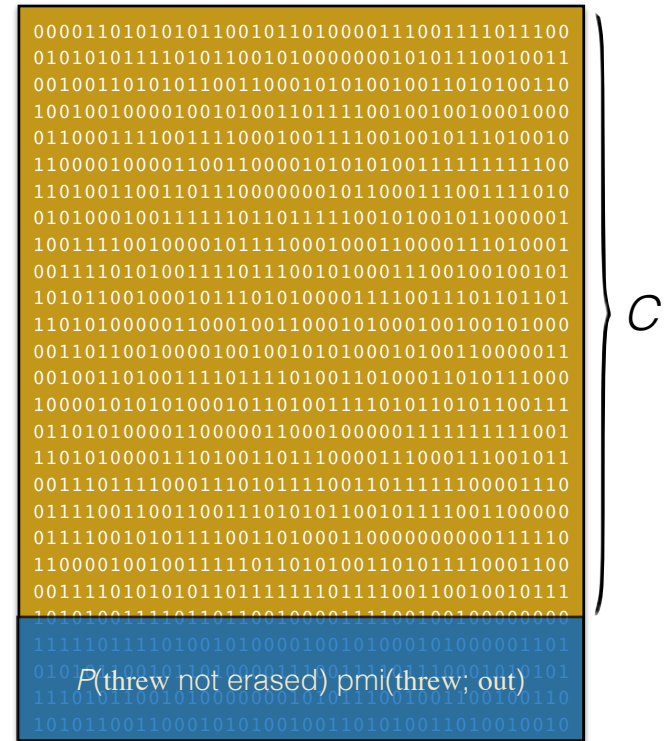
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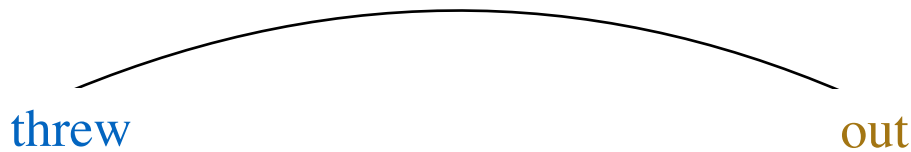
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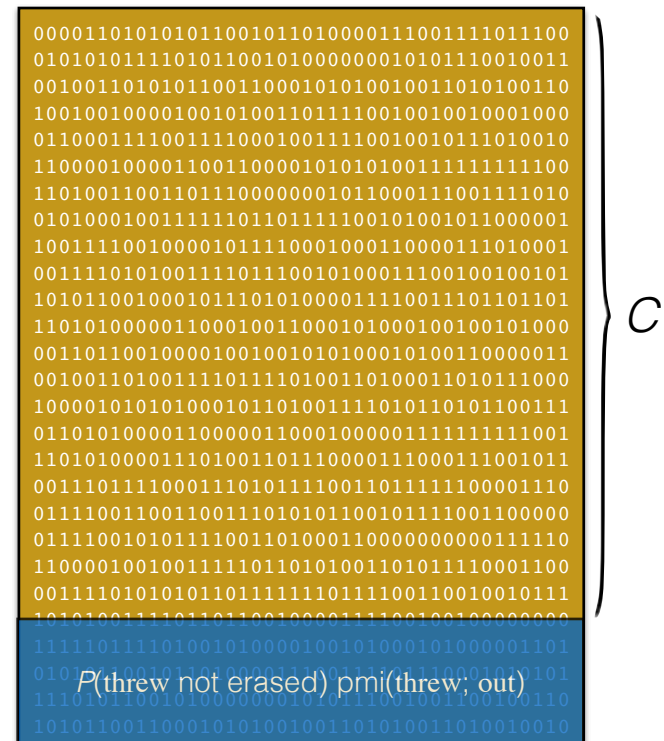
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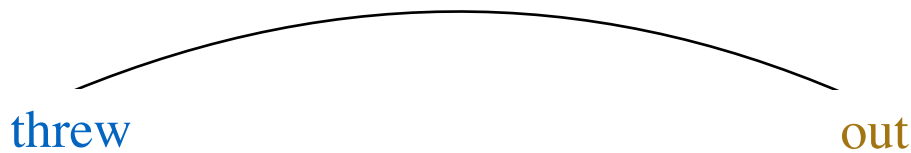
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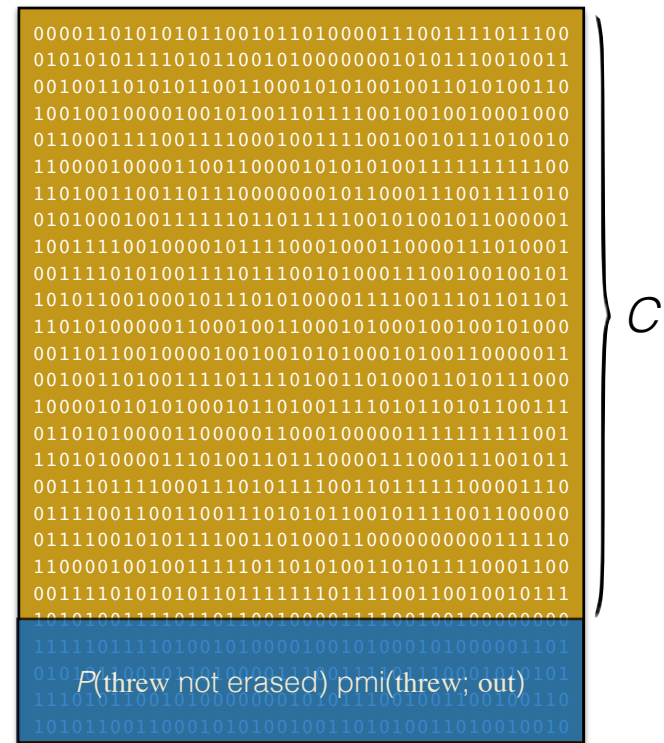
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- When context items are far, their cost-reducing influence decreases.
 - Similar to the concept of decay in cue effectiveness (Qian & Jaeger, 2012)



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- We will show that the hypothesis is true in dependency corpora.

Do Dependencies Have High Mutual Information?

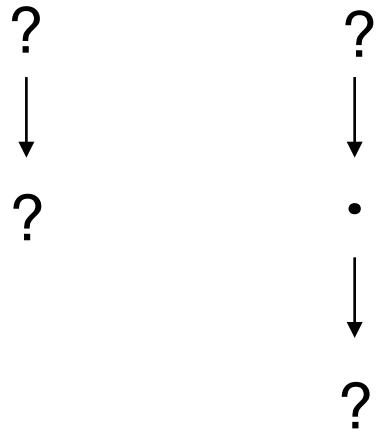
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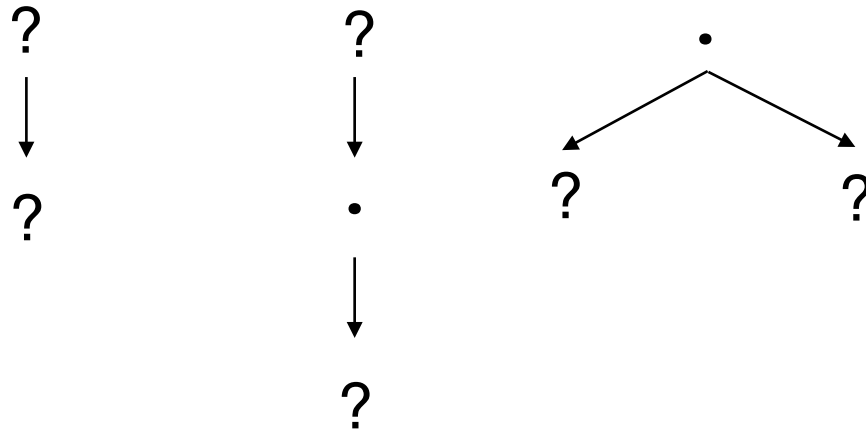


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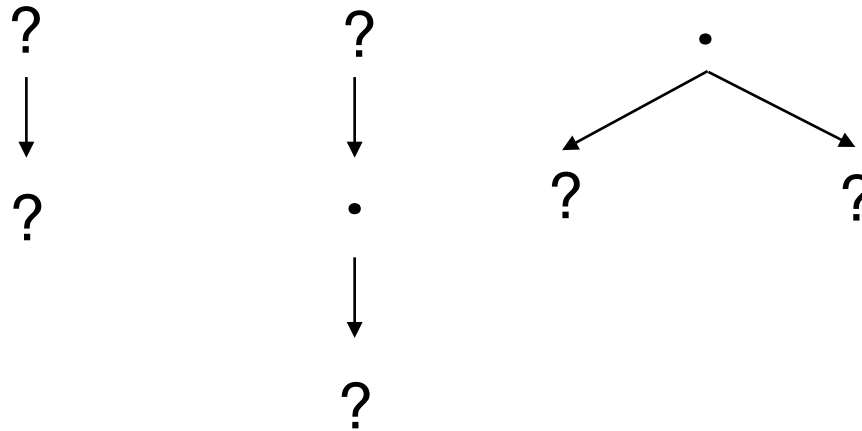
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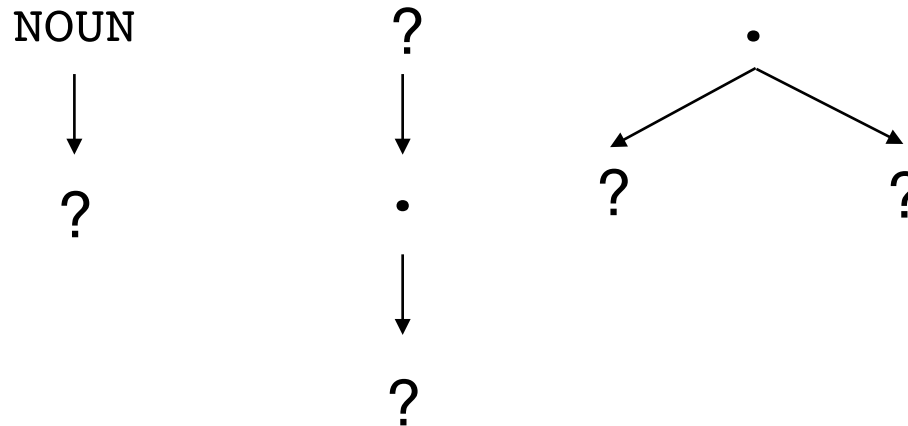


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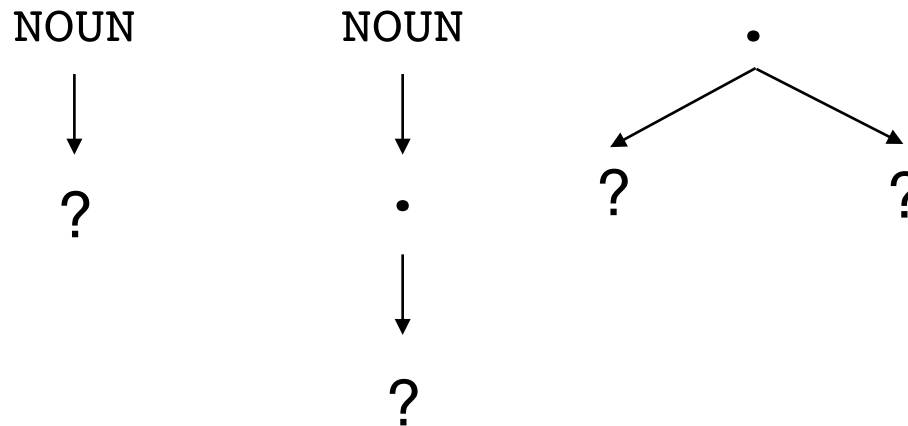
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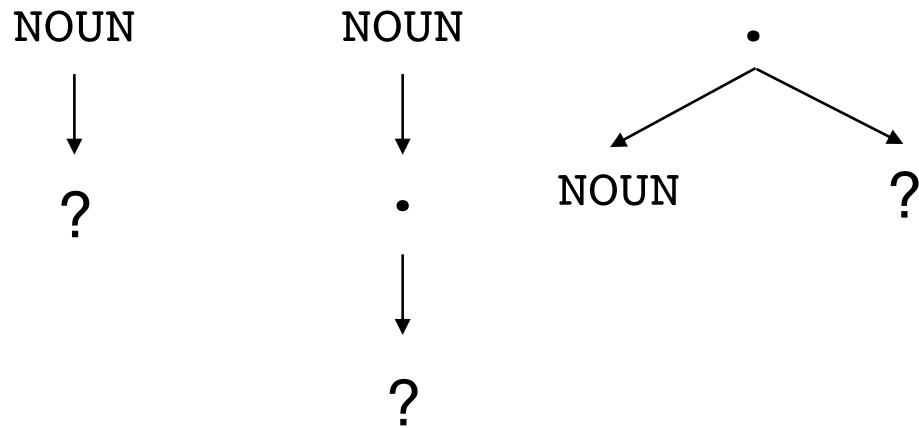
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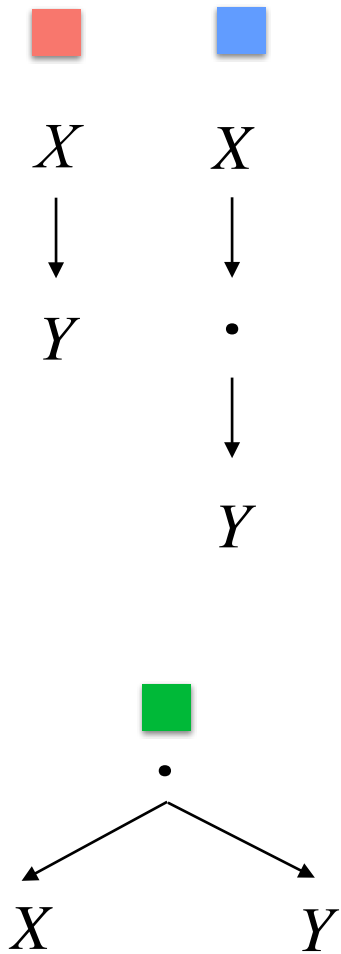


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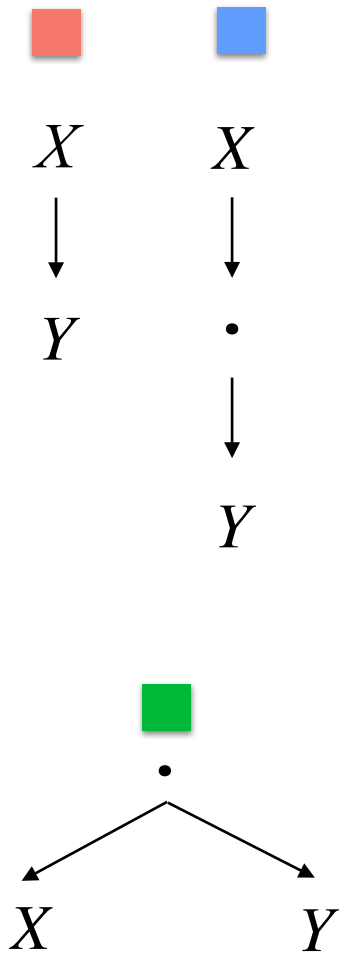
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Comprehension as exploration of input

- Broader ongoing goal: develop eye-movement control model integrating the insights discussed thus far:
 - Probabilistic linguistic knowledge
 - Uncertain input representations
 - Principles of adaptive, rational action
- *Reinforcement learning* is an attractive tool for this

A rational reader

- Very simple framework:
 - Start w/ prior expectations for text (linguistic knowledge)
 - Move eyes to get perceptual input
 - Update beliefs about text as visual arrives (Bayes' Rule)
- Add to that:
 - Set of *actions* the reader can take in discrete time
 - A *behavior policy*: how the model decides between actions

A first-cut behavior policy

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- Actions: *keep fixating*; *move the eyes*; or *stop reading*
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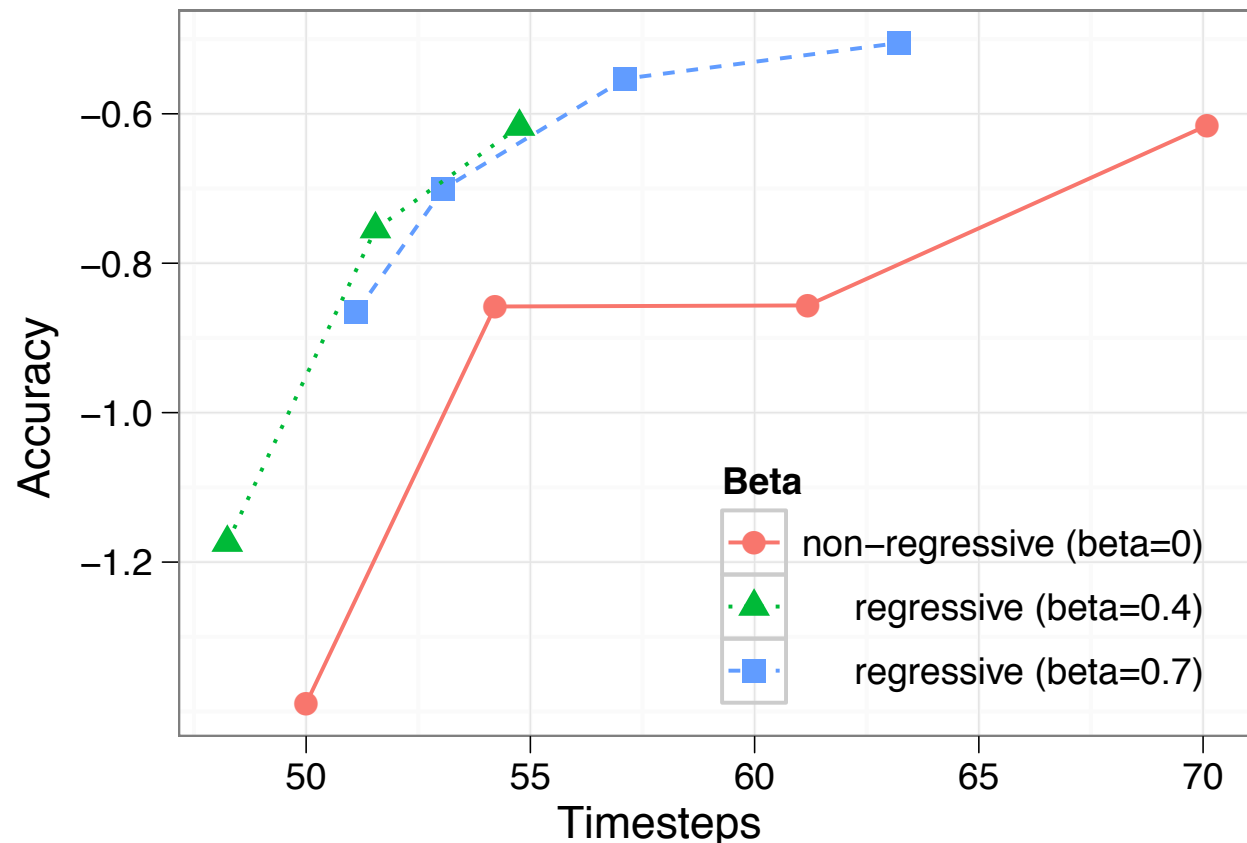
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...

- Move left to right, bringing up confidence in each character position until it reaches α
- If confidence in a previous character position drops below β , regress to it
- Finish reading when you're confident in everything

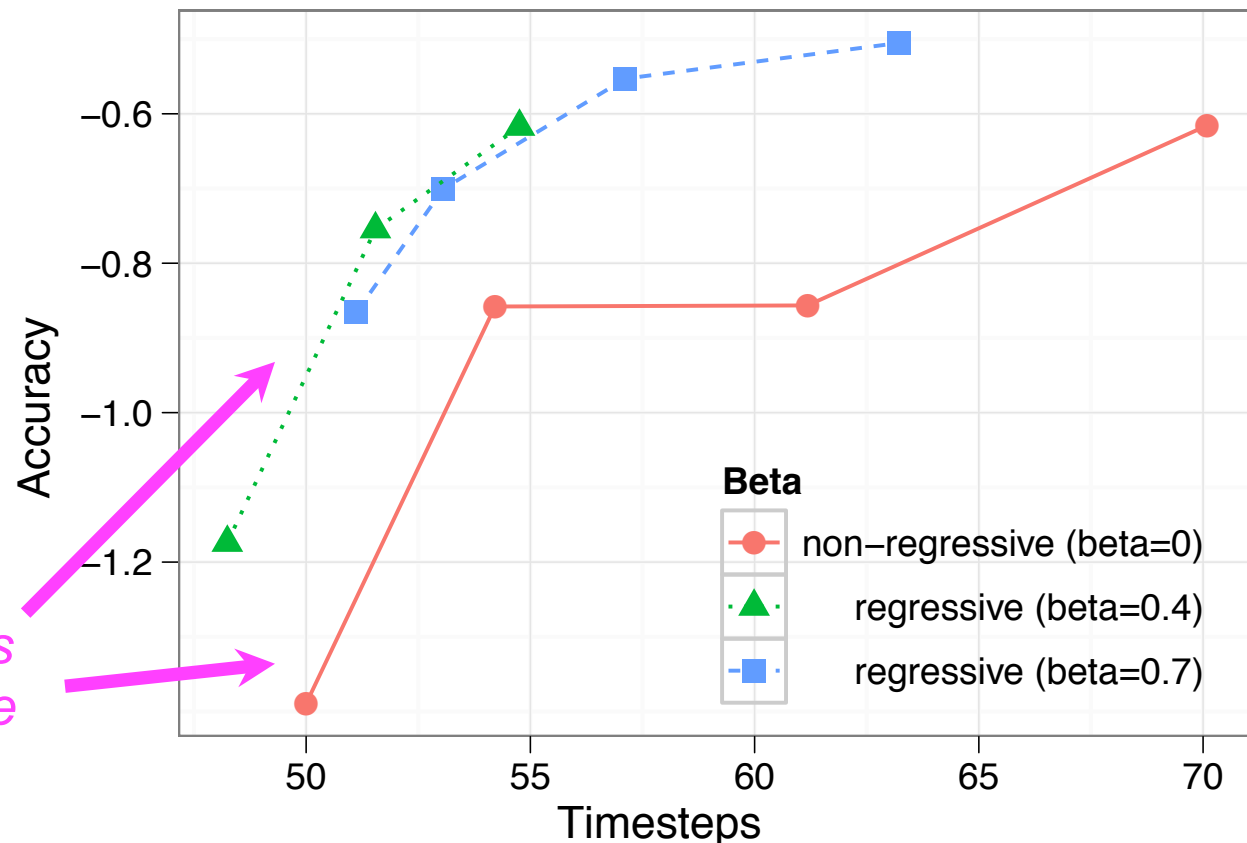
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*Non-regressive policies
always beaten by some
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Goal-based adaptation

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- Open frontier: modeling the adaptation of eye movements to specific reader goals
- We set a *reward function*: relative value γ of speed (finish reading in T timesteps) versus accuracy (guess correct sentence with probability L)
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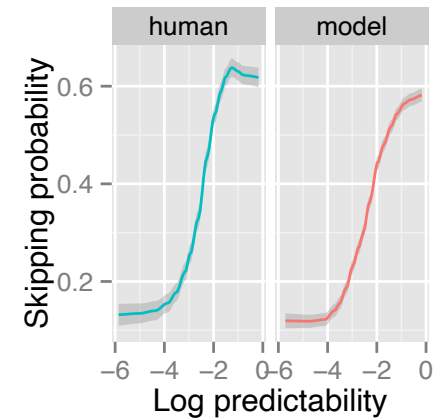
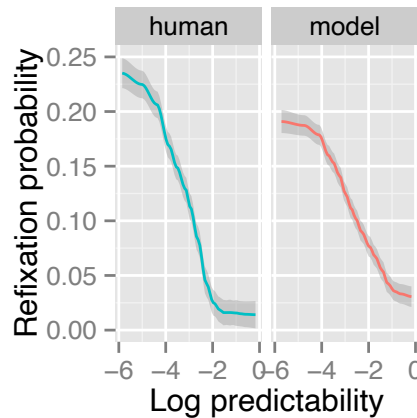
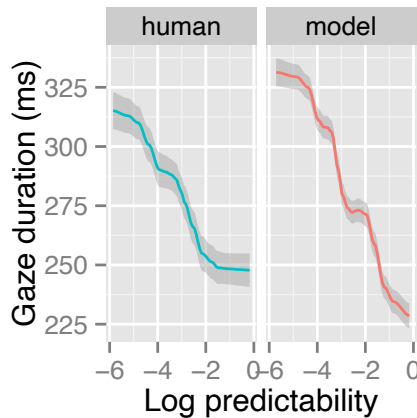
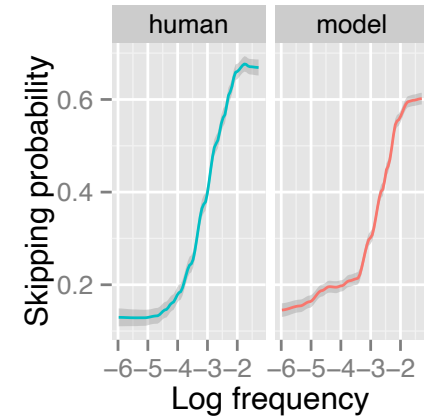
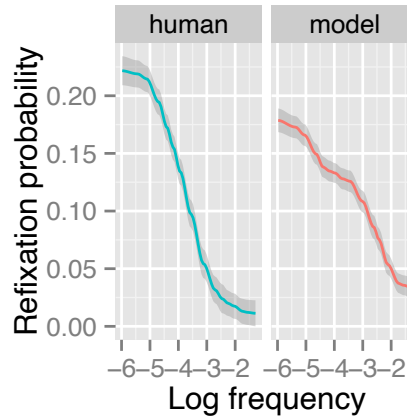
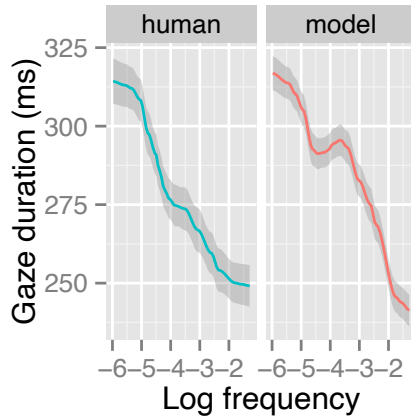
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- The method works, and gives intuitive results

Empirical match with human reading

- Benchmark measures in eye-movement modeling:

frequency



predicts size and shape of all effects

predictability

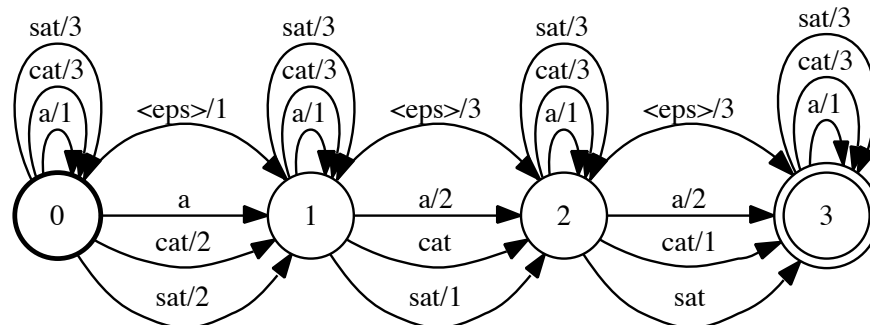
Bicknell & Levy (2012)

Success at empirical benchmarks





- Other models (E-Z Reader, SWIFT) get these too, but *stipulate* rel'nship between word properties & “processing rate”
- We *derive* these relationships from simple principles of noisy-channel perception and rational action

Noisy-channel processing: summary





- Noisy-channel models help us understand
 - Basic capabilities of human language comprehension
 - Outstanding puzzles in syntactic processing
- These models open up a rich typology of new sentence processing effects
- There is growing evidence for these effects
- These models pose new theoretical opportunities and architectural challenges for the study of human linguistic cognition



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