# Words

9.19: Computational Psycholinguistics 18 September 2023 Roger Levy

#### How do we learn so many words?

- The average 20-year-old native English speaker knows
   42,000 lemmas
- That is 5.75 lemmas per day, every day!
- The mystery:

The average seventh-grader...must have acquired most of them as a result of reading because (a) the majority of English words are used only in print, (b) she already knew well almost all the words she would have encountered in speech, and (c) she learned less than one word by direct instruction. Studies of children reading grade-school text find that about one word in every 20 paragraphs goes from wrong to right on a vocabulary test. The typical seventh grader would have read less than 50 paragraphs since yesterday, from which she should have learned less than three new words. Apparently, she mastered the meanings of [several] words that she did not encounter.

(Landauer & Dumais, 1997, Psychological Review)

We saw a cute, hairy wampimuk sleeping behind the tree

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  - "You shall know a word by the company it keeps" (Firth, 1957)
  - "...the linguistic meanings which the structure carries can only be due to the relations in which the elements of the structure take part" (Harris, 1968)

#### More complex examples

The degus was hermetically broamed.

(After McDonald & Ramscar, 2001)

#### Implicit distributional/contextual knowledge

# What word can appear in the context of all these words?

Word 1: drown, bathroom, shower, fill, fall, lie, electrocute, toilet, whirlpool, iron, gin

Word 2: eat, fall, pick, slice, peel, tree, throw, fruit, pie, bite, crab, grate

Word 3: advocate, overthrow, establish, citizen, ideal, representative, dictatorship, campaign, bastion, freedom

Word 4: spend, enjoy, remember, last, pass, end, die, happen, brighten, relive Implicit distributional/contextual knowledge

# What word can appear in the context of all these words?

Word 1: drown, ballindellin, shower, fill, fall, lie, electrocute, toilet, whirlpool, iron, gin

Word 2: eat, fall, pick, slice, peel, tree, throw, fruit, pie, bite, crab, grate

democracy

Word 3: advocate, democra overthrow, establish, citizen, ideal, representative, dictatorship, campaign, bastion, freedom

Word 4: spend, enjoy, remember, last, pass, end, die, happen, brighten, relive

day

# Word 5: eat, paint, peel, apple, fruit, juice, lemon, blue, grow

#### orange

# Word 5: eat, paint, peel, apple, fruit, juice, lemon, blue, grow

## A practical problem for *n*-gram modeling

- Consider the distributions on these contexts:
  - The soup was... 7402
  - The broth was... 1903
  - The chowder was... 231
  - The bisque was... 118
  - The soup will be... 815
  - The broth will be... 122

Google Web context counts

- *n*-gram models have no built-in ways of leveraging similarity among contexts
- Similar problems exist for conditioning on context for probabilistic grammars

• What can you *drive* someone...?

• What can you *drive someone...*?

mad

• What can you *drive someone...*?

mad

crazy

• What can you *drive someone...*?

mad

crazy

to distraction

• What can you *drive someone...*?

mad

crazy

#### to distraction

bananas

• What can you *drive someone...*?

mad

crazy

#### to distraction

bananas

insane

• What can you *drive someone...*?

#### mad

crazy

#### to distraction

#### bananas

insane

nuts



- These expressions do not come on the scene independently!
- There is lexical specificity, but innovation also spreads along lines of semantic similarity

#### Fundamental idea

- We have tens of thousands of words in our lexicon
- But semantic lexical knowledge mostly lives on a lowerdimensional subspace
- By learning that lower-dimensional subspace, we can:
  - Better handle data sparsity in practical NLP applications
  - Resolve the mystery of how we learn so many words so fast
  - Improve our understanding of human conceptual space
  - Better explain the full distribution of linguistic expressions

#### **Technical foundations**

• We want to go from sparse...

 $[dog] = [0,0,\ldots,0,1,0,\ldots,0]$ 

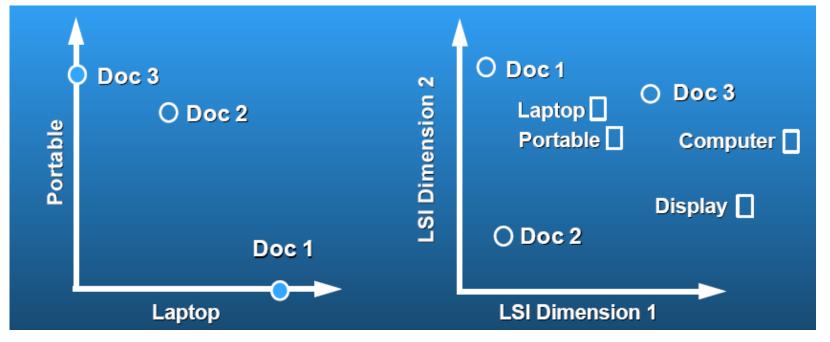
• ...to dense:

 $\llbracket dog \rrbracket = [-0.11, 0.81, \dots, 0.58, 0.07]$ 

• There are many ways proposed to do this!

#### Low-dimensional word meanings from contexts

• The general goal:



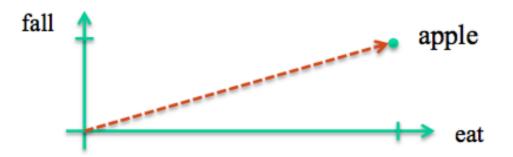
courtesy of Susan Dumais (via Chris Manning & Hinrich Schutze)

# How can we compare two context collections in their entirety?

Count how often "apple" occurs close to other words in a large text collection (corpus):

eat	fall	ripe	slice	peel	tree	throw	fruit	pie	bite	crab
<b>794</b>	244	47	221	208	160	145	156	109	104	88

#### Interpret counts as coordinates:



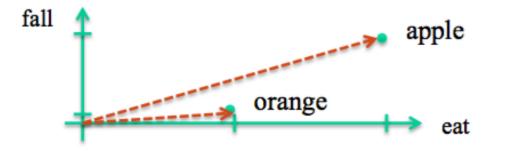
Every context word becomes a dimension.

(Slide from Yoav Goldberg)

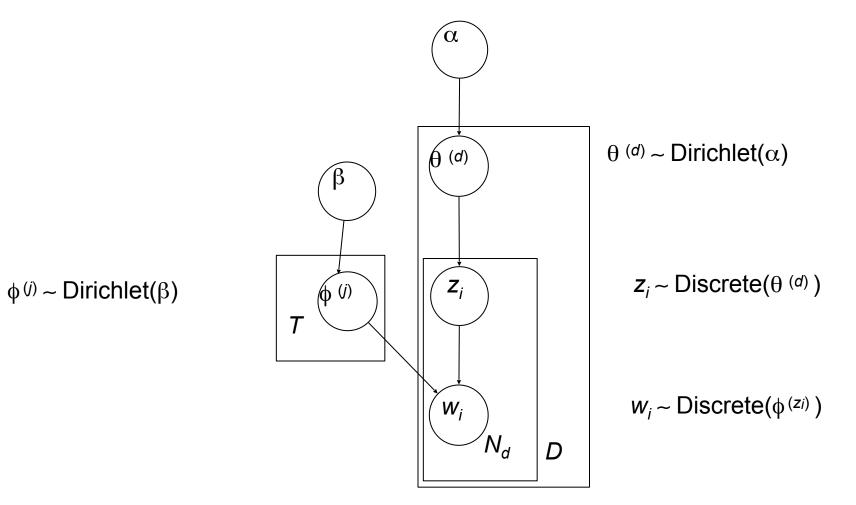
# How can we compare two context collections in their entirety?

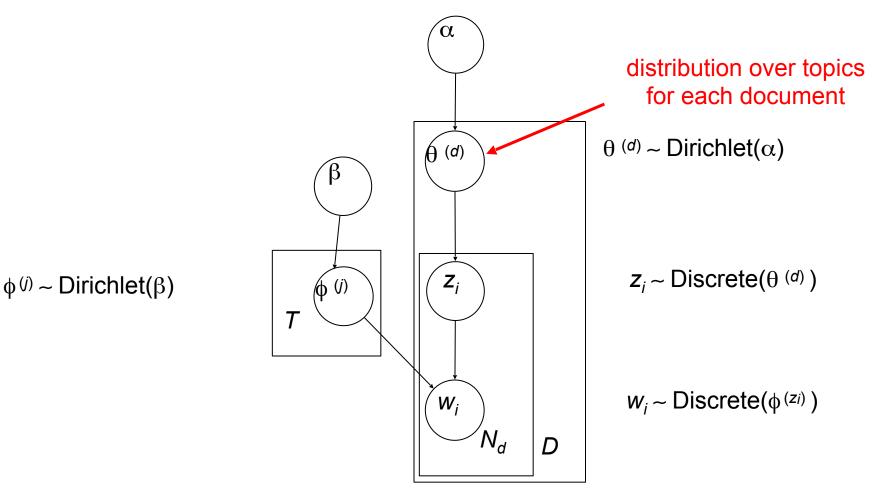
Then visualize both count tables as vectors in the same space:

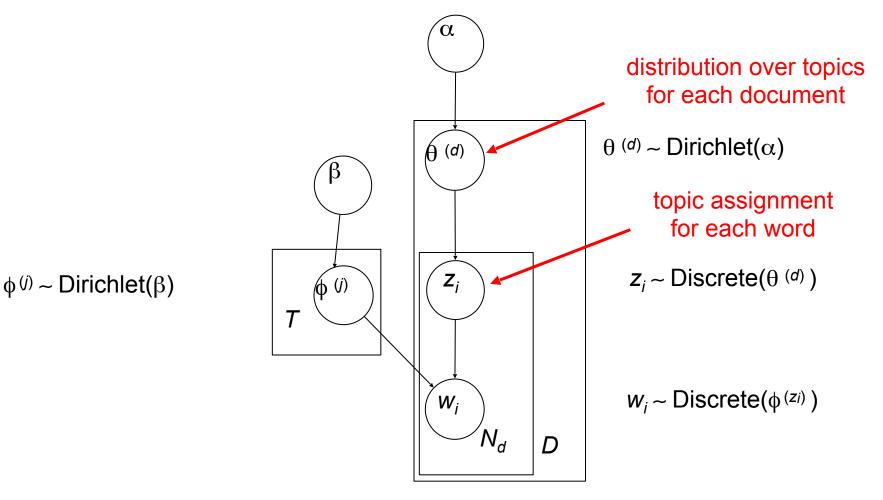
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265	22	25	62	220	64	74	111	4	4	8

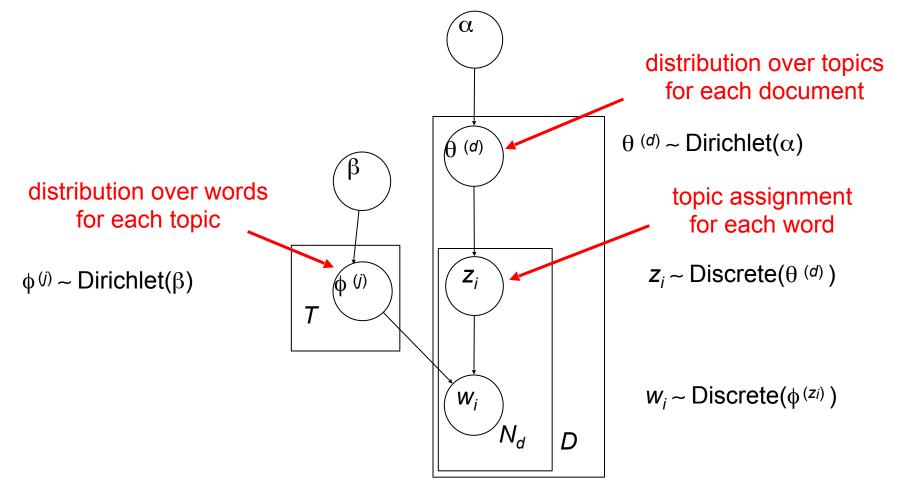


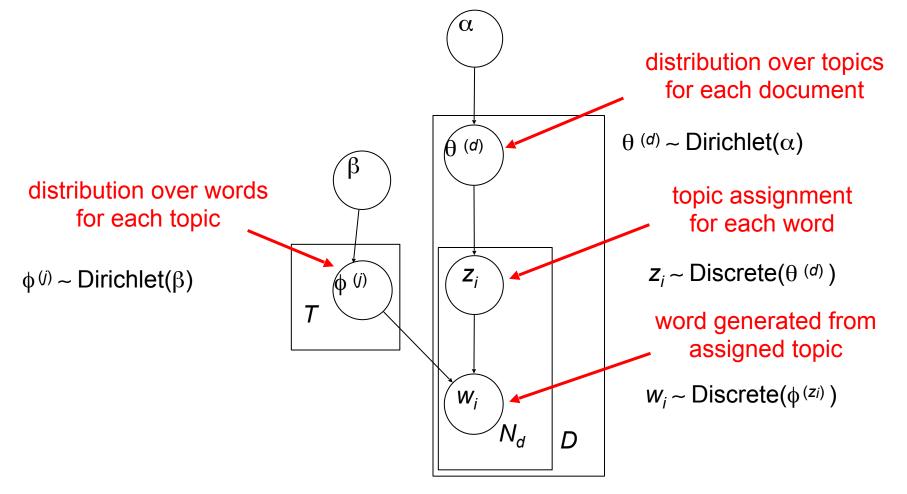
Similarity between two words as proximity in space

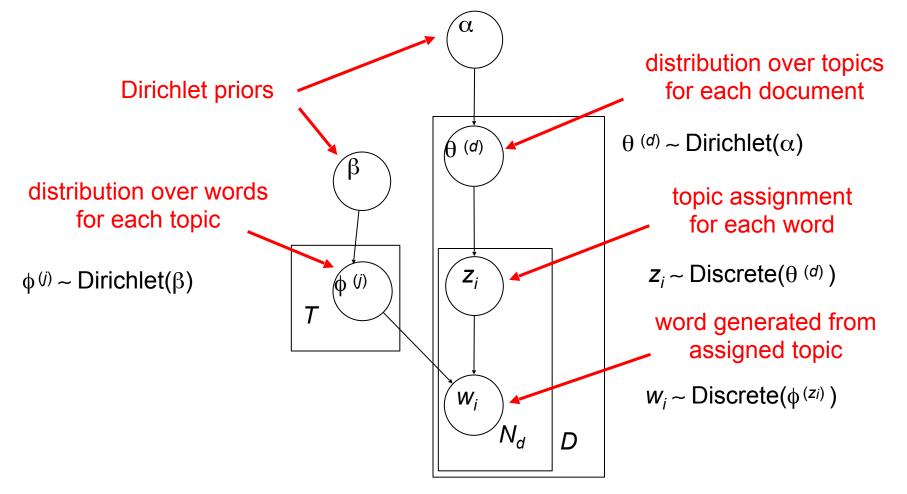












#### Interpretable topics

DISEASE BACTERIA DISEASES	WATER FISH SEA	MIND WORLD DREAM	STORY STORIES TELL	FIELD MAGNETIC MAGNET	SCIENCE STUDY SCIENTISTS	BALL GAME TEAM	JOB WORK JOBS
GERMS	SWIM	DREAMS	CHARACTER	WIRE	SCIENTIFIC	FOOTBALL	CAREER EXPERIENCE
FEVER	SWIMMING		CHARACTERS	NEEDLE	KNOWLEDGE WORK	BASEBALL PLAYERS	EMPLOYMENT
CAUSE	POOL	IMAGINATION	AUTHOR	CURRENT COIL	RESEARCH	PLATERS	OPPORTUNITIES
CAUSED	LIKE	MOMENT	READ	POLES	CHEMISTRY	FIELD	WORKING
SPREAD	SHELL	THOUGHTS OWN	TOLD SETTING	IRON	TECHNOLOGY		TRAINING
VIRUSES INFECTION	SHARK	REAL	TALES	COMPASS		BASKETBAL	L SKILLS
VIRUS	TANK SHELLS	LIFE	PLOT	LINES	MATHEMATICS	COACH	CAREERS
MICROORGANISM		IMAGINE	TELLING	CORE	BIOLOGY	PLAYED	POSITIONS
PERSON	DIVING	SENSE	SHORT	ELECTRIC	FIELD	PLAYING	FIND
INFECTIOUS	DOLPHINS	CONSCIOUSNES	SS FICTION	DIRECTION	PHYSICS	HIT	POSITION
COMMON	SWAM	STRANGE	ACTION	FORCE	LABORATORY	TENNIS	FIELD
CAUSING	LONG	FEELING	TRUE	MAGNETS	STUDIES	TEAMS	OCCUPATIONS
SMALLPOX	SEAL	WHOLE	EVENTS	BE	WORLD	GAMES	REQUIRE
BODY	DIVE	BEING	TELLS	MAGNETISM		SPORTS	
INFECTIONS	DOLPHIN	MIGHT	TALE	POLE	STUDYING	BAT	EARN ABLE
CERTAIN	UNDERWATER	e HOPE	NOVEL	INDUCED	SCIENCES	TERRY	ADLE

each column shows words from a single topic, ordered by P(w|z)

(Slide from Tom Griffiths)

#### The first neural embedding: word2vec

word2vec implements several different algorithms:

Two training methods

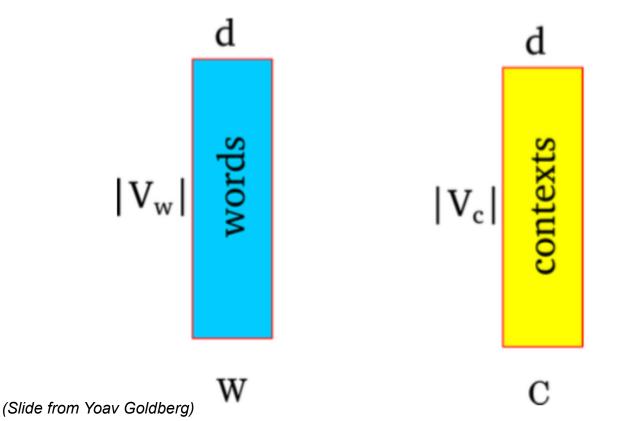
- Negative Sampling
- Hierarchical Softmax

Two context representations

- Continuous Bag of Words (CBOW)
- Skip-grams

#### How does word2vec work?

- Represent each word as a *d* dimensional vector.
- Represent each context as a *d* dimensional vector.
- Initalize all vectors to random weights.
- Arrange vectors in two matrices, W and C.



## How does word2vec work?

While more text:

Extract a word window:
A springer is [ a cow or heifer close to calving ].
 C<sub>1</sub> C<sub>2</sub> C<sub>3</sub> W C<sub>4</sub> C<sub>5</sub> C<sub>6</sub>

Try setting the vector values such that:

 $\sigma(\mathbf{w} \cdot \mathbf{c}_1) + \sigma(\mathbf{w} \cdot \mathbf{c}_2) + \sigma(\mathbf{w} \cdot \mathbf{c}_3) + \sigma(\mathbf{w} \cdot \mathbf{c}_4) + \sigma(\mathbf{w} \cdot \mathbf{c}_5) + \sigma(\mathbf{w} \cdot \mathbf{c}_6)$ 

is **high** 

- Create a corrupt example by choosing a random word w' [ a cow or comet close to calving ] c<sub>1</sub> c<sub>2</sub> c<sub>3</sub> w' c<sub>4</sub> c<sub>5</sub> c<sub>6</sub>
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## How does word2vec work?

The training procedure results in:

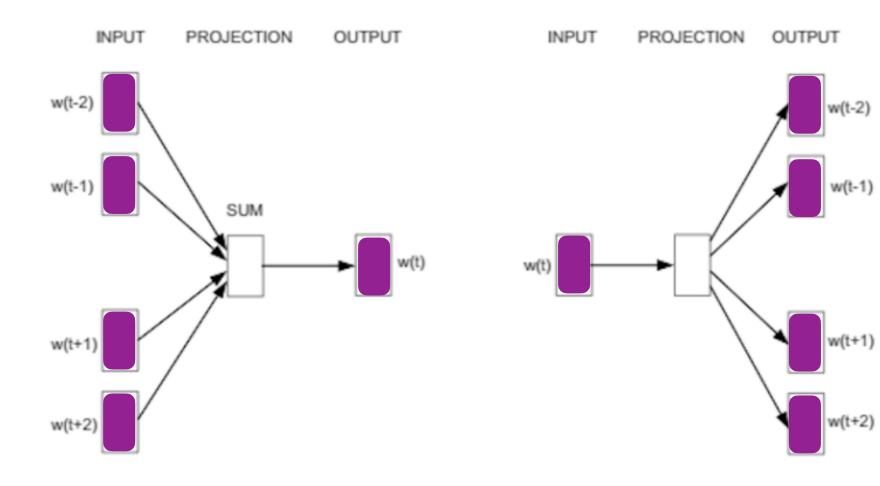
- $\blacktriangleright$  *w* · *c* for **good** word-context pairs is **high**.
- $w \cdot c$  for **bad** word-context pairs is **low**.
- $w \cdot c$  for **ok-ish** word-context pairs is **neither high nor low**.

As a result:

- Words that share many contexts get close to each other.
- Contexts that share many words get close to each other.

At the end, word2vec throws away C and returns W.

### word2vec architecture visualized



#### **Continuous bag of words**

Skip-gram

• The basic intuition: *ratios of conditional probabilities might give us a handle on meaning components* 

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Probability and Ratio	k = solid	k = gas	k = water	k = fashion
P(k ice)	$1.9 \times 10^{-4}$	$6.6 \times 10^{-5}$	$3.0 \times 10^{-3}$	$1.7 \times 10^{-5}$
P(k steam)	$2.2 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.2 \times 10^{-3}$	$1.8 \times 10^{-5}$
P(k ice)/P(k steam)	8.9	$8.5 \times 10^{-2}$	1.36	0.96

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		1		
		/		

Highly imbalanced; argued to pick out distinctive difference in meaning component of **ice** versus **steam** 

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Highly im	led to pick	Balanced: ard	ued not to pick	

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		1	1	1
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$$\frac{P(w_k|w_i)}{P(w_k|w_j)} = \frac{P(w_k, w_i)}{P(w_j, w_i)} \approx_{RFE} \frac{X_{ik}}{X_{jk}}$$

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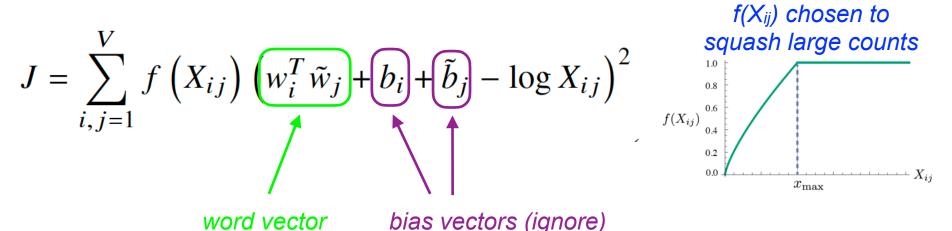
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count of  $w_i, w_j$ 

# Deriving the GloVe word vector model

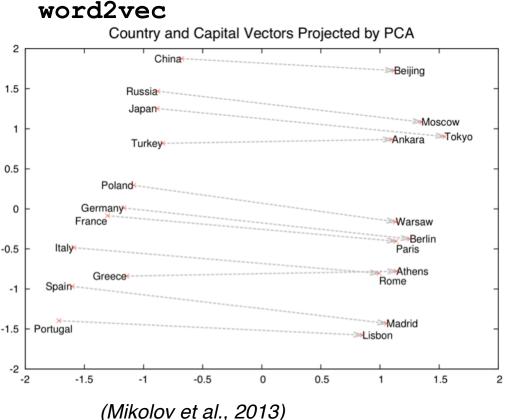
• We enforce probability ratios to be the ratio of dotproducts of the target word to context words

$$F\left((w_i - w_j)^T \tilde{w}_k\right) = \frac{P_{ik}}{P_{jk}}$$

• With a lot more simplification and argumentation we get the following objective function to minimize:



## Word meanings reflected in embeddings



fat breakfast fragrance broiler dryer seashore bake kettle bayou ginsena alcohol opium bottle bamboo coffee còrn cacaoconfectionery mint alder banana almond combine clover bloom sauce fawn cappuccinc jockey clov bagel colt chive nburaer celeriac roas chicorv carp cutlet chowde crayfish

GloVe Word Embedding (6B.300d) - Food Related Area

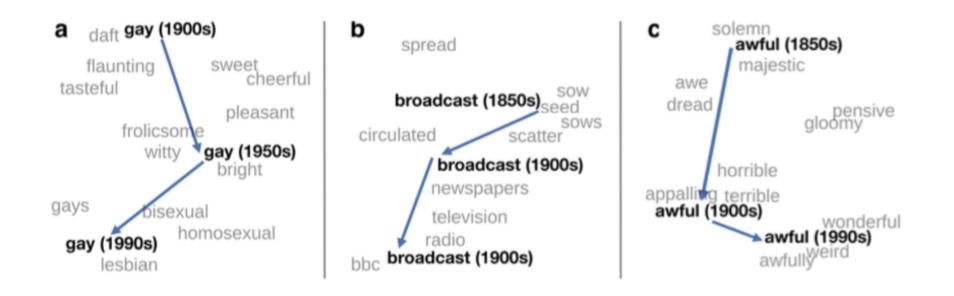
vineyard crate laundry

## Exploring GLoVE meaning spaces & analogies

#### *Try playing with this fun visualization tool!*

#### https://lamyiowce.github.io/word2viz/

## word2vec embeddings over time



**Figure 1:** Two-dimensional visualization of semantic change in English using SGNS vectors.<sup>2</sup> **a**, The word *gay* shifted from meaning "cheerful" or "frolicsome" to referring to homosexuality. **b**, In the early 20th century *broadcast* referred to "casting out seeds"; with the rise of television and radio its meaning shifted to "transmitting signals". **c**, *Awful* underwent a process of pejoration, as it shifted from meaning "full of awe" to meaning "terrible or appalling" (Simpson et al., 1989).







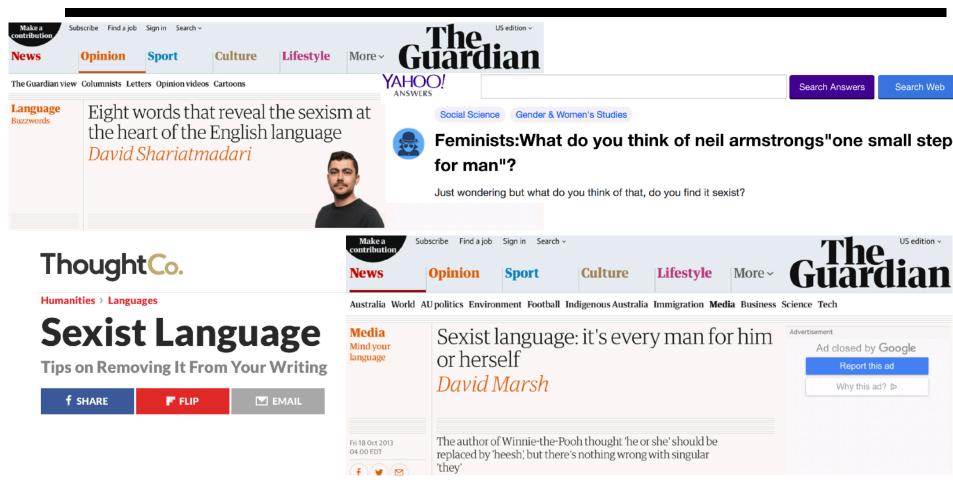
#### ThoughtCo.

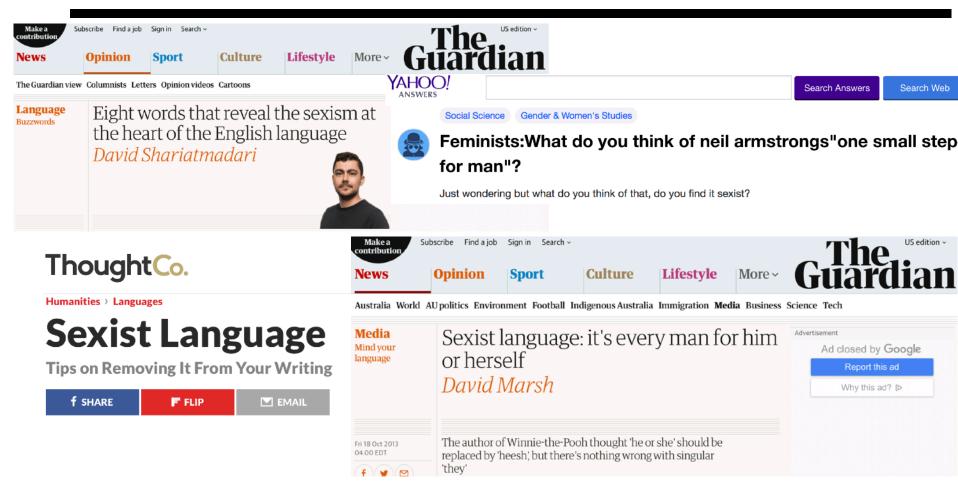
Humanities > Languages



**Tips on Removing It From Your Writing** 







#### How do we bring this question into our scientific reach?

# Electrophysiological responses



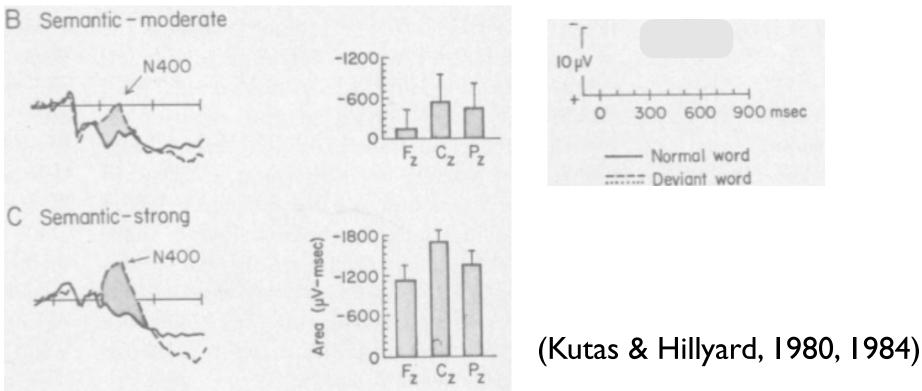
# **Rapid Serial Visual Presentation**

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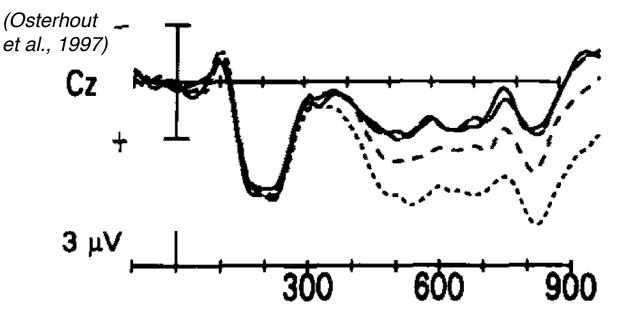
# **Rapid Serial Visual Presentation**

# The N400 in language comprehension

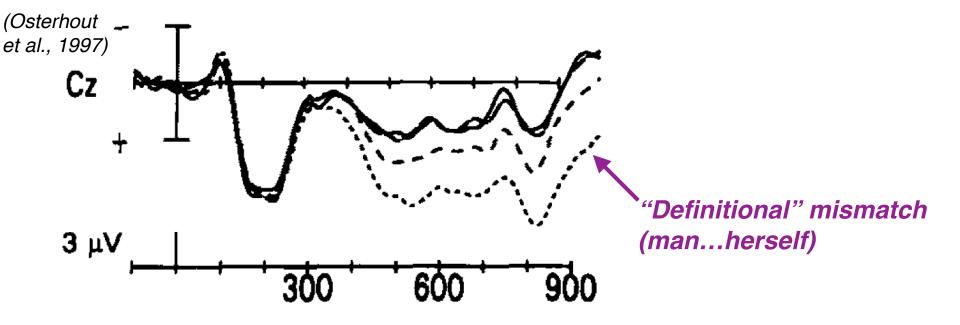
- Differing degrees of semantic congruity:
  - He took a sip from the *drink*. (normal)
  - He took a sip from the *waterfall*. (moderate incongruity)
  - He took a sip from the *transmitter*. (strong incongruity)



 Mismatches to lexically specified (*definitional*\*) semantic properties induce measurable expectation violations

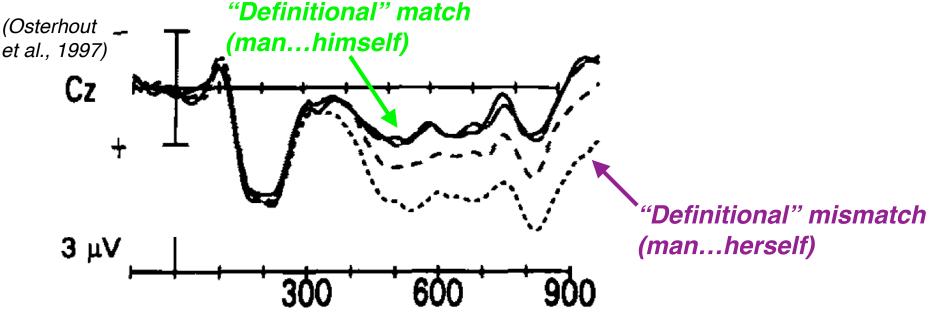


(Osterhout et al., 1997; see also reading time studies by Sturt, 2003; Duffy & Keir, 2004, inter alia) 32



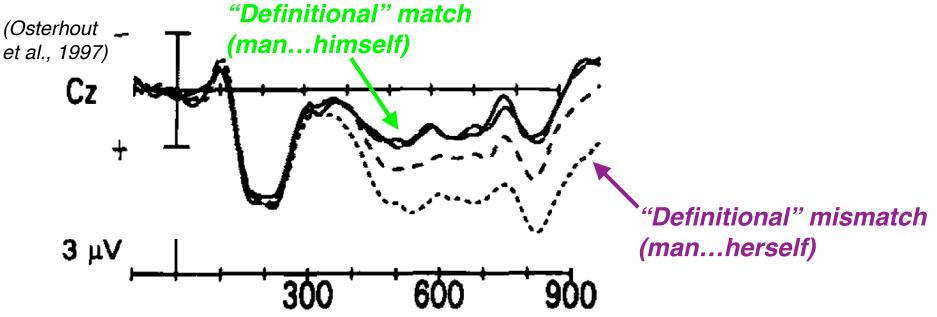
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The man prepared herself for the interview.



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 Mismatches to stereotypical semantic properties induce similar violations

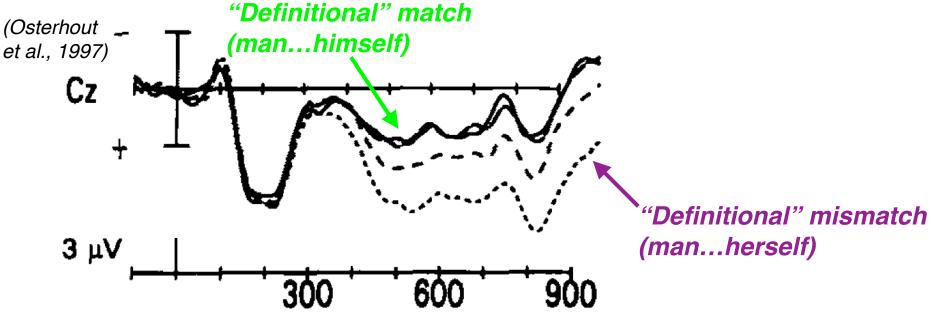
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#### Categorical & stereotypical semantic knowledge

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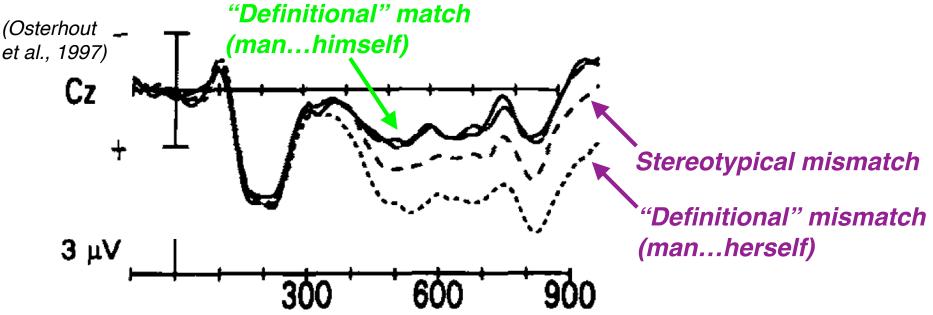
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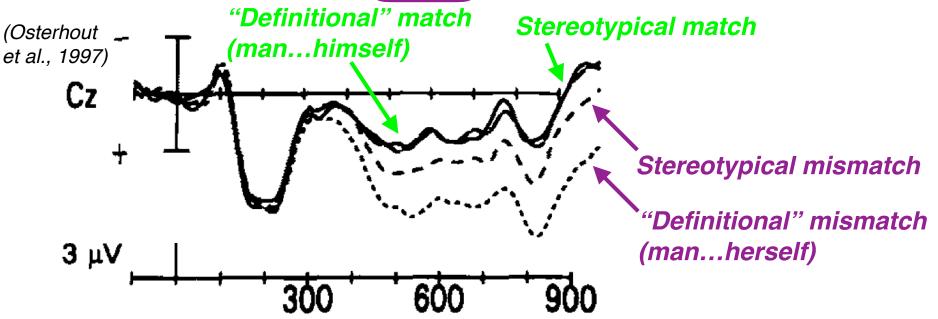
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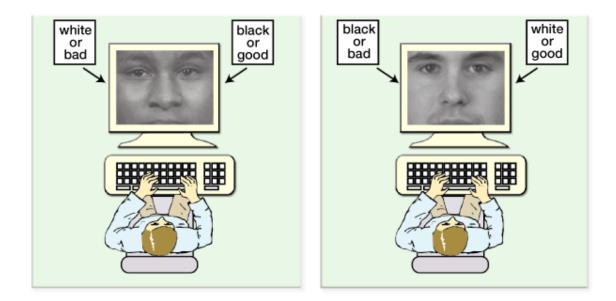
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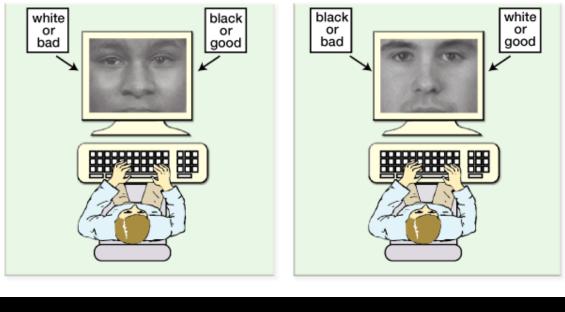
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#### Stereotypes as implicit associations among concepts

#### Stereotypes as implicit associations among concepts



#### Stereotypes as implicit associations among concepts



Female<br/>CareerMale<br/>FamilySalary

Might stereotypes manifest in distributed linguistic representations too, *biasing* them?

Might stereotypes manifest in distributed linguistic representations too, *biasing* them?

How could we tell?

Group 1 words

he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews

**Group 1 words** *he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews* 

**Group 2 words** she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces

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Group "M" words

janitor, statistician, midwife, bailiff, auctioneer, photographer, geologist, shoemaker, athlete, cashier, dancer, housekeeper, accountant, physicist, gardener, dentist, weaver, blacksmith, psychologist, supervisor, mathematician, surveyor, tailor, designer, economist, mechanic, laborer, postmaster, broker, chemist, librarian, attendant, clerical, musician, porter, scientist, carpenter, sailor, instructor, sheriff, pilot, inspector, mason, baker, administrator, architect, collector, operator, surgeon, driver, painter, conductor, nurse, cook, engineer, retired, sales, lawyer, clergy, physician, farmer, clerk, manager, guard, artist, smith, official, police, doctor, professor, student, judge, teacher, author, secretary, soldier

<b>Group 1 words</b> Mean vector: $v_1$	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews
Group 2 words	she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces
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<b>Group 1 words</b>	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers,
Mean vector: $v_1$	men, boys, males, brothers, uncle, uncles, nephew, nephews
<b>Group 2 words</b>	she, daughter, hers, her, mother, woman, girl, herself, female, sister,
Mean vector: $v_2$	daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces
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smith, official, police, doctor, professor, student, judge, teacher, author,

35

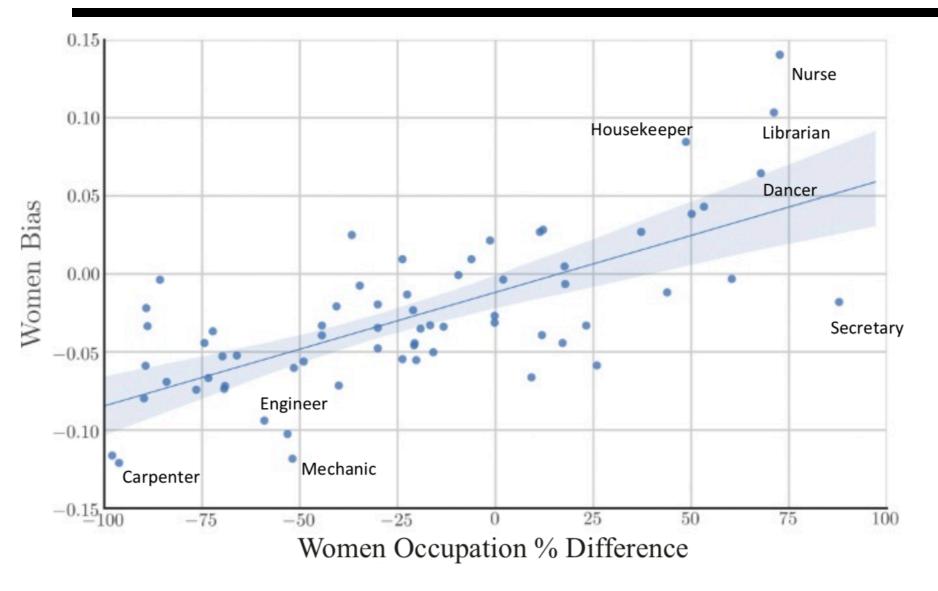
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Gender  $Bias(w_m) = Dist(v_1, w_m) - Dist(v_2, w_m)$ 

(Garg et al., 2018)

# Word embeddings vs. ground truth



<sup>(</sup>Garg et al., 2018)

Group 1 words

baptism, messiah, catholicism, resurrection, christianity, salvation, protestant, gospel, trinity, jesus, christ, christian, cross, catholic, church

Group 1 words	baptism, messiah, catholicism, resurrection, christianity, salvation, protestant, gospel, trinity, jesus, christ, christian, cross, catholic, church
Group 2 words	allah, ramadan, turban, emir, salaam, sunni, koran, imam, sultan, prophet, veil, ayatollah, shiite, mosque, islam, sheik, muslim, muhammad

**Group 1 words** baptism, messiah, catholicism, resurrection, christianity, salvation, protestant, gospel, trinity, jesus, christ, christian, cross, catholic, church

#### **Group 2 words** allah, ramadan, turban, emir, salaam, sunni, koran, imam, sultan, prophet, veil, ayatollah, shiite, mosque, islam, sheik, muslim, muhammad

**Group "M" words** *terror, terrorism, violence, attack, death, military, war, radical, injuries, bomb, target, conflict, dangerous, kill, murder, strike, dead, violence, fight, death, force, stronghold, wreckage, aggression, slaughter, execute, overthrow, casualties, massacre, retaliation, proliferation, militia, hostility, debris, acid, execution, militant, rocket, guerrilla, sacrifice, enemy, soldier, terrorist, missile, hostile, revolution, resistance, shoot* 

<b>Group 1 words</b> Mean vector: $v_1$	baptism, messiah, catholicism, resurrection, christianity, salvation, protestant, gospel, trinity, jesus, christ, christian, cross, catholic, church
Group 2 words	allah, ramadan, turban, emir, salaam, sunni, koran, imam, sultan, prophet, veil, ayatollah, shiite, mosque, islam, sheik, muslim, muhammad
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Group 1 words

Mean vector:  $v_1$ 

Group 2 words Mean vector:  $v_2$  baptism, messiah, catholicism, resurrection, christianity, salvation, protestant, gospel, trinity, jesus, christ, christian, cross, catholic, church

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#### Group "M" words

 $\{w_m\}$ 

terror, terrorism, violence, attack, death, military, war, radical, injuries, bomb, target, conflict, dangerous, kill, murder, strike, dead, violence, fight, death, force, stronghold, wreckage, aggression, slaughter, execute, overthrow, casualties, massacre, retaliation, proliferation, militia, hostility, debris, acid, execution, militant, rocket, guerrilla, sacrifice, enemy, soldier, terrorist, missile, hostile, revolution, resistance, shoot

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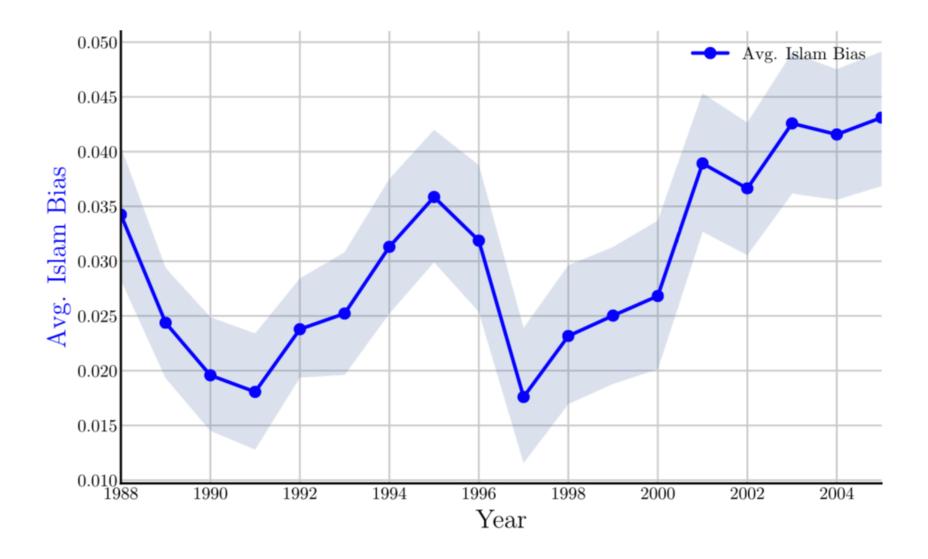
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# Group "M" words $\{w_m\}$

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Overall Bias = 
$$\sum \text{Dist}(v_1, w_m) - \text{Dist}(v_2, w_m)$$

(Garg et al., 2018)



(Garg et al., 2018)

(Caliskan et al., 2017; "WEFAT")

Group 1 words

he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews

- **Group 1 words** *he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews*
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Group 1 words	he, son, his, him, father, man, boy, himself, male, brother, sons,
	fathers, men, boys, males, brothers, uncle, uncles, nephew,
	nephews

- **Group 2 words** she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces
- **Group A words** career, office, salary, ...

<b>Group 1 words</b> $\{w_1\}$	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews
Group 2 words	she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces
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<b>Group A words</b> $\{w_A\}$	career, office, salary,
Group B words	family, home, children,

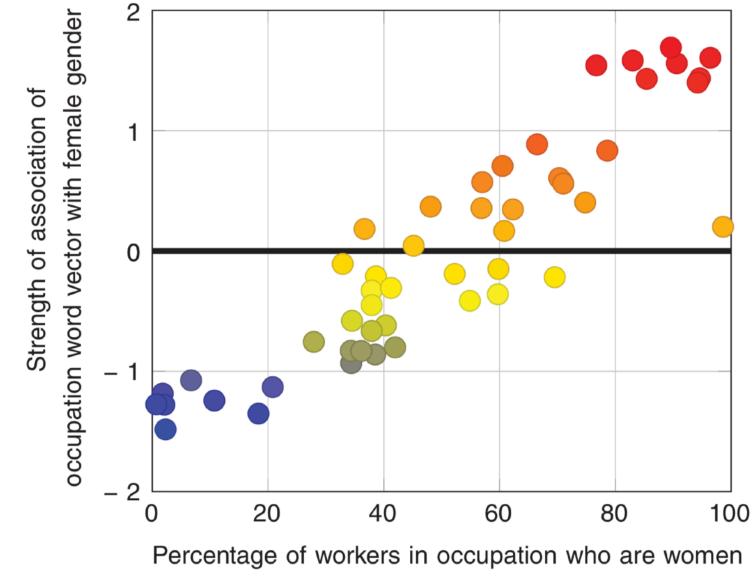
<b>Group 1 words</b> $\{w_1\}$	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews
<b>Group 2 words</b> $\{w_2\}$	she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces
Group A words	career, office, salary,
$\{w_A\}$	
Group B words	family, home, children,
$\{w_B\}$	

<b>Group 1 words</b> $\{w_1\}$	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews
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Group A words	career, office, salary,
$\{w_A\}$	
Group B words	family, home, children,
$\{w_B\}$	
Overall Bias:	
Average <sub>w1,w2,wA,w</sub>	$\sum_{w_B} \left[ Dist(v_1, w_A) - Dist(v_2, w_A) - Dist(v_1, w_B) + Dist(v_2, w_B) \right]$

# An alternative bias-quantifying method

<b>Group 1 words</b> $\{w_1\}$	he, son, his, him, father, man, boy, himself, male, brother, sons, fathers, men, boys, males, brothers, uncle, uncles, nephew, nephews									
Group 2 words $\{w_2\}$	she, daughter, hers, her, mother, woman, girl, herself, female, sister, daughters, mothers, women, girls, females, sisters, aunt, aunts, niece, nieces									
Group A words	career, office, salary,									
$\{w_A\}$										
Group B words	family, home, children,									
$\{w_B\}$										
Overall Bias:										
Average	$_{v_B}\left[Dist(v_1, w_A) - Dist(v_B)\right]$	$(v_2, w_A) - I$	$Dist(v_1, w_B) + Dist(v_2, w_B)$							
GloVe cosine s	similarities:	career o	children							
	woman	0.29	0.42							
(Caliskan et al., 2017; "	WEFAT") <b>man</b>	0.32	0.27	39						

#### **WEFAT Results**



(Caliskan et al., 2017)

#### WEFAT results: many stereotypes

<b>T</b>	Attribute words	Original finding				Our finding			
Target words		Ref.	N	d	Р	N <sub>T</sub>	N <sub>A</sub>	d	Р
Flowers vs. insects	Pleasant vs. unpleasant	(5)	32	1.35	10 <sup>-8</sup>	25 × 2	25 × 2	1.50	10-7
Instruments vs. weapons	Pleasant vs. unpleasant	(5)	32	1.66	10 <sup>-10</sup>	25 × 2	25 × 2	1.53	10 <sup>-7</sup>
European-American vs. African-American names	Pleasant vs. unpleasant	(5)	26	1.17	10 <sup>-5</sup>	32 × 2	25 × 2	1.41	10 <sup>-8</sup>
European-American vs. African-American names	Pleasant vs. unpleasant from (5)	(7)	Not applicable			16 × 2	25 × 2	1.50	10-4
European-American vs. African-American names	Pleasant vs. unpleasant from (9)	(7)	Not applicable			16 × 2	8 × 2	1.28	10-3
Male vs. female names	Career vs. family	(9)	39k	0.72	<10 <sup>-2</sup>	8 × 2	8 × 2	1.81	10 <sup>-3</sup>
Math vs. arts	Male vs. female terms	(9)	28k	0.82	<10 <sup>-2</sup>	8 × 2	8 × 2	1.06	.018
Science vs. arts	Male vs. female terms	(10)	91	1.47	10 <sup>-24</sup>	8 × 2	8 × 2	1.24	10-2
Mental vs. physical disease	Temporary vs. permanent	(23)	135	1.01	10-3	6 × 2	7 × 2	1.38	10-2
Young vs. old people's names	Pleasant vs. unpleasant	(9)	43k	1.42	<10 <sup>-2</sup>	8 × 2	8 × 2	1.21	10 <sup>-2</sup>

• **Embed** size-*V* vocabulary in a *D*-dimensional space; *D*<<*V* 

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- Since corpus statistics reflect the world, word embeddings implicitly encode biases
- **Open question:** do these biases simply reflect information about the world, or does language present distorted representations of that information?